

Recap - Chapter 1

1

1. Introduction to concepts of basic variables in an electric circuit >> **current**, **voltage** & **power**.
2. Distinguished between **power absorbed** ($p = +Vi$) and **power supplied** ($p = -Vi$).

2

EEEB 113 CIRCUIT ANALYSIS I

Chapter 2 Basic Laws

Materials from Fundamentals of Electric Circuits, Alexander & Sadiku 4e, The McGraw-Hill Companies, Inc.

Basic Laws - Chapter 2

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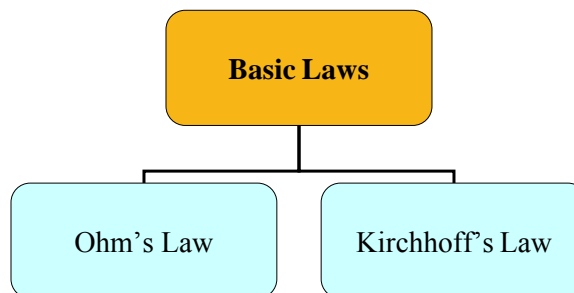
- 2.1 Introduction.
- 2.2 Ohm's Law.
- 2.3 Nodes, Branches & Loops.
- 2.4 Kirchhoff's Laws.
- 2.5 Series Resistors & Voltage Division.
- 2.6 Parallel Resistors & Current Division.
- 2.7 Wye-Delta Transformations.

2.1 Introduction

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How to determine values of the basic variables in an electric circuit? What are the Basic Laws?

- Fundamental laws that govern the electric circuit.



2.2 Ohm's Law (1)

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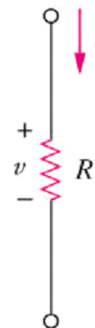
□ Ohm's Law

The voltage across a resistor is directly proportional to the current, i flowing through the resistor.

$$\therefore v \propto i$$

- **Ohm further defined:** The constant of proportionality for a resistor to be the resistance, R .

$$\therefore v = iR$$



2.2 Ohm's Law (2)

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- Thus, the **resistance**, R is the ability of an element to resist the flow of electric current; measured in ohms (Ω).

$$\therefore R = \frac{v}{i}$$

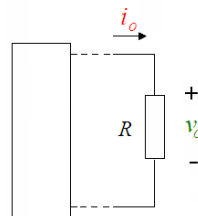
$$\Rightarrow 1\Omega = \frac{1V}{1A}$$

2.2 Ohm's Law (3)

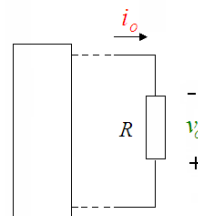
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□ **Passive sign convention;**

a) $v = iR$ >> current from hi pot. to lo pot.



b) $v = -iR$ >> current from lo pot. to hi pot.



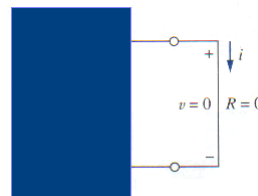
2.2 Ohm's Law (4)

8

- **Extreme cases:** As R can vary from 0 to ∞ it is important that we consider these two extreme possible values of R .

$R=0$ >> short circuit (*ideal circuit*)

However, in practice, a short circuit is usually a connecting wire, assumed to be a perfect conductor.



(a) Short circuit ($R = 0$).

∴ A **short circuit** is a circuit that has circuit element with resistance approaching 0 .

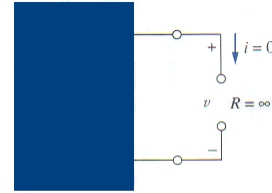
$$v = iR = 0 \quad \therefore R \rightarrow 0 \quad ; \quad v = 0; \quad i = x$$

2.2 Ohm's Law (5)

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$R = \infty \gg$ open circuit

\therefore A **open circuit** is a circuit that has circuit element with resistance approaching ∞ .



(b) Open circuit ($R = \infty$).

$$i = \lim_{R \rightarrow \infty} \frac{v}{R} = 0 \quad \therefore R \rightarrow \infty \quad ; \quad i = 0; \quad v = x$$

2.2 Ohm's Law (6)

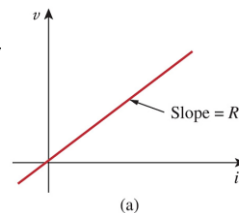
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□ Resistors

Two types — **Fixed** : resistance remains constant.
— **Variable** : have adjustable resistance.

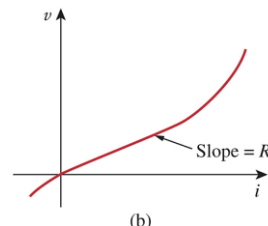
□ Not all resistors obey Ohm's Law.

a) Linear resistors obey
 (e.g. normal resistors)



b) Non-linear resistors do not obey. (e.g. diode)

However, throughout the course, **ALL resistors are assumed LINEAR.**



2.2 Ohm's Law (7)

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□ Conductance

$$\begin{array}{l} \text{if} \\ \text{then} \end{array} \quad \begin{array}{l} R = \frac{v}{i} \\ \frac{1}{R} = \frac{i}{v} \end{array} \quad \begin{array}{l} \rightarrow \\ \rightarrow \end{array} \quad \begin{array}{l} \text{resist current,} \\ \text{conduct current.} \end{array}$$

This special quantity, $\frac{1}{R}$ is known as conductance of an element, G .

2.2 Ohm's Law (8)

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- **Conductance** is a measurement of how well an element will conduct electric current.
- It is measured in mhos (\mathfrak{O}) or siemens (S).

$$1S = 1\mathfrak{O} = 1 \frac{A}{V}$$

- In this course, we will use the SI unit of siemens (S).

2.2 Ohm's Law (9)

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□ Power in Resistor & Conductor

$$\text{Resistor: } p = vi = (iR)i = i^2R = v\left(\frac{v}{R}\right) = \frac{v^2}{R}$$

$$\text{Conductor: } p = vi = v(vG) = v^2G = \left(\frac{i}{G}\right)i = \frac{i^2}{G}$$

Note that R and G are always positive. As is i^2 and v^2 .

- ∴ Power dissipated in or absorbed by the resistor is always positive. Confirms theory - resistor is a passive element, cannot generate energy.

2.2 Ohm's Law (10)

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□ Practice Problem 2.1

The essential component of a toaster is an electrical element (a resistor) that converts electrical energy to heat energy. How much current is drawn by a toaster with resistance 10Ω at 110V ?

Solution

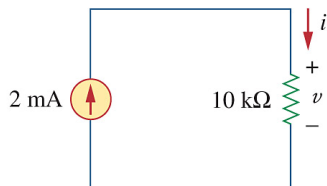
$$i = V/R = 110/10 = \mathbf{11\text{ A}}$$

2.2 Ohm's Law (11)

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□ Practice Problem 2.2

For the circuit shown below, calculate the voltage v , the conductance G , and the power p .



Solution

$$(a) \quad v = iR = 2 \text{ mA} \times 10 \text{ k}\Omega = \mathbf{20 \text{ V}}$$

$$(b) \quad G = 1/R = 1/10 \text{ k}\Omega = \mathbf{100 \mu\text{S}}$$

$$(c) \quad p = vi = 20 \text{ volts} \times 2 \text{ mA} = \mathbf{40 \text{ mW}}$$

2.2 Ohm's Law (12)

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□ Practice Problem 2.3

A resistor absorbs an instantaneous power of $20 \cos^2(t)$ mW when connected to a voltage source $v = 10 \cos(t)$ V. Find i and R .

Solution

$$p = vi \quad \text{thus,} \quad i = p/v = [20 \cos^2(t) \text{ mW}] / [10 \cos(t) \text{ V}] \\ = \mathbf{2 \cos(t) \text{ mA}}$$

$$R = v/i = [10 \cos(t) \text{ V}] / [2 \cos(t) \text{ mA}] \\ = \mathbf{5 \text{ k}\Omega}$$

2.3 Nodes, Branches & Loops (1)

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- A **branch** represents a single element (voltage source, current source or resistor).
- A **node** is the point of connection between 2 or more branches.
- A **loop** is any closed path in a circuit.

2.3 Nodes, Branches & Loops (2)

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- A network with 'b' branches, 'n' nodes, and 'l' independent loops will satisfy the **fundamental theorem of network topology**:

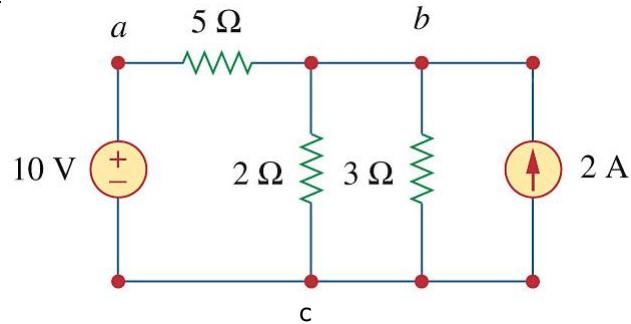
$$b = l + n - 1$$

- ≥ 2 elements are in **series** if they **exclusively share a single node**.
- ≥ 2 elements are in **parallel** if they are **connected to the same 2 nodes**.

2.4 Nodes, Branches & Loops (3)

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Example 1

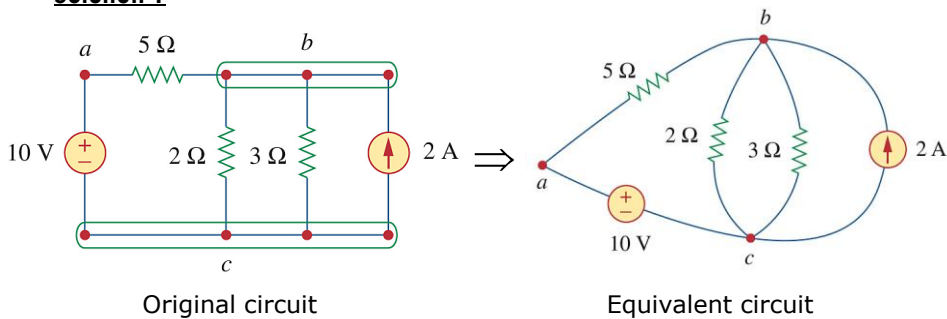


How many branches, nodes and loops are there?

2.4 Nodes, Branches & Loops (4)

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Solution 1



5 branches, 3 nodes and 3 loops

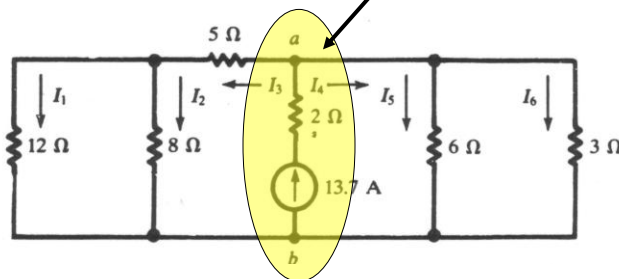
$$b = l + n - 1 \quad \therefore 5 = 3 + 3 - 1$$

2.3 Nodes, Branches & Loops (5)

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Example 2

Should we consider it as one branch or two branches?



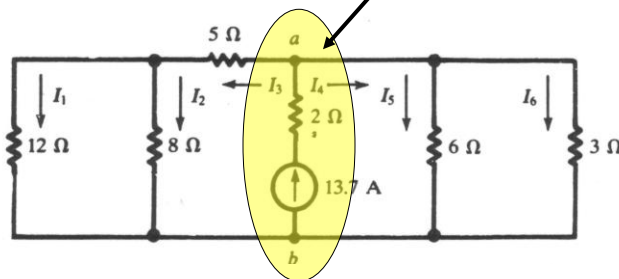
How many branches, nodes and loops are there?

2.3 Nodes, Branches & Loops (6)

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Solution 2

Consider as two branches, as there are 2 elements.

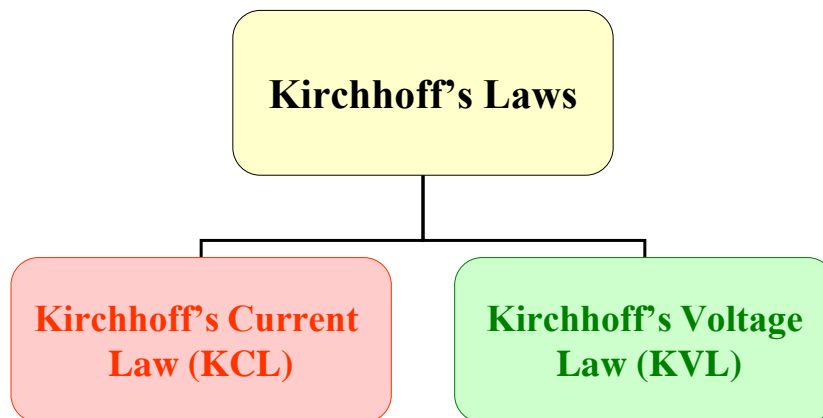


7 branches, 4 nodes and 4 loops

$$b = l + n - 1 \quad \therefore 7 = 4 + 4 - 1$$

2.4 Kirchhoff's Laws (1)

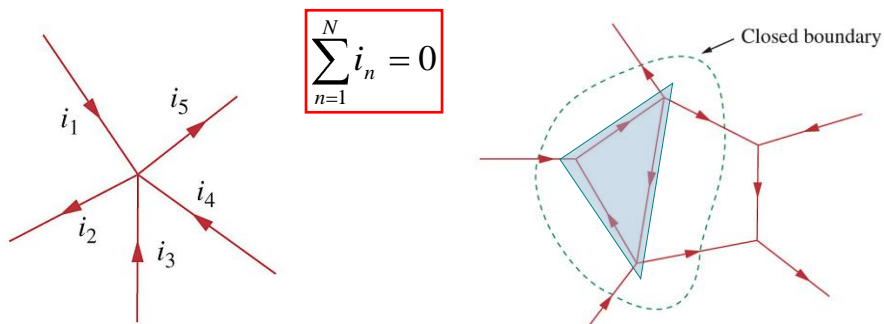
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2.4 Kirchhoff's Laws (2)

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- **KCL** : the algebraic **sum of currents** entering a node (or a closed boundary) is **zero**.



$$\sum_{n=1}^N i_n = 0$$

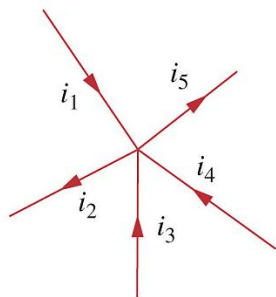
N = no. of branches connected to the node;
 i_n = n th current entering the node.

2.4 Kirchhoff's Laws (3)

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- Alternatively, the **sum of currents entering** a node **equals** the **sum of currents leaving** a node.

$$\sum i_{in} = \sum i_{out}$$



Example:

$$i_1 - i_2 + i_3 + i_4 - i_5 = 0$$

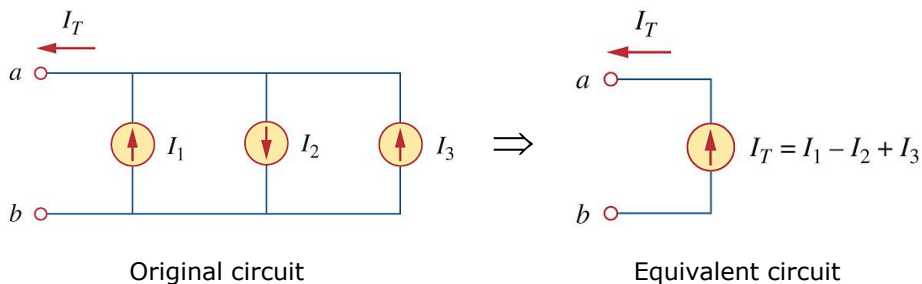
or

$$i_1 + i_3 + i_4 = i_2 + i_5$$

2.4 Kirchhoff's Laws (4)

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- **KCL** can be applied to obtain the combined current, when **current sources are connected in parallel**.

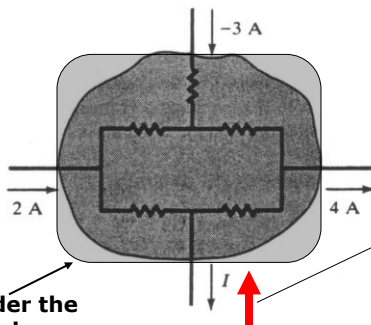


2.4 Kirchhoff's Laws (5)

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Example 3

- Determine the current I for the circuit shown in the figure below.



We can consider the whole enclosed area as one "node".

$$-I - 4 + (-3) + 2 = 0$$

$$I + 4 - (-3) - 2 = 0$$

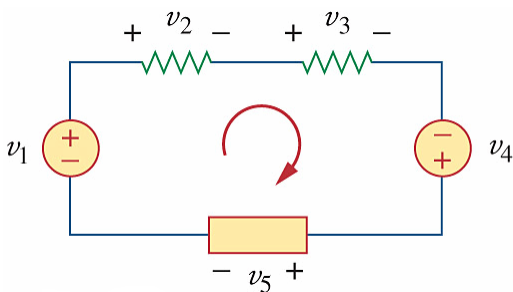
$$\Rightarrow I = -5A$$

This indicates that the actual current for I is flowing in the opposite direction.

2.4 Kirchhoff's Laws (6)

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- **KVL** : the algebraic **sum of all voltages** around a closed path (or loop) is **zero**.



$$\sum_{m=1}^M v_m = 0$$

M = no. of voltages (or no. of branches) in a loop;

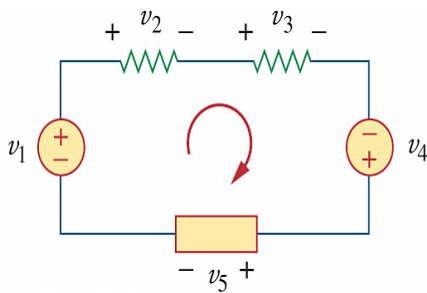
v_m = m th voltage.

2.4 Kirchhoff's Laws (7)

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- **Alternatively**, the sum of voltage drops equals the sum of voltage rise.

$$\sum v_{drop} = \sum v_{rise}$$



Example:

$$-v_1 + v_2 + v_3 - v_4 + v_5 = 0$$

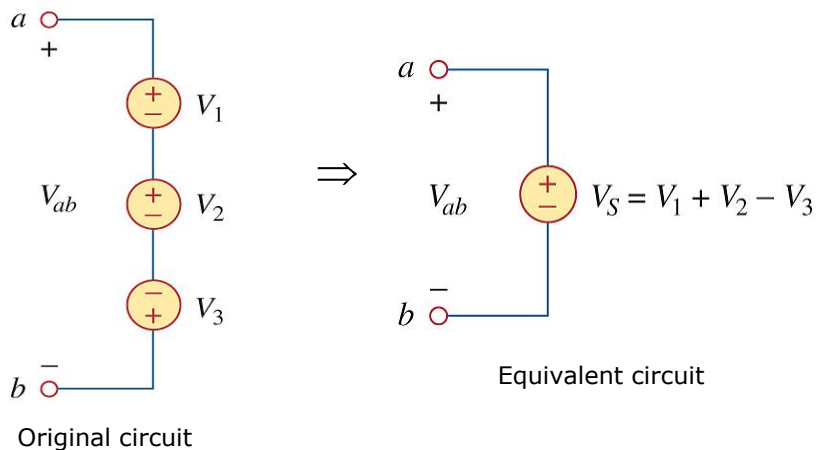
or

$$v_2 + v_3 + v_5 = v_1 + v_4$$

2.4 Kirchhoff's Laws (8)

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- **KVL** can be applied to obtain the combined voltage, when **voltage sources are connected in series**.

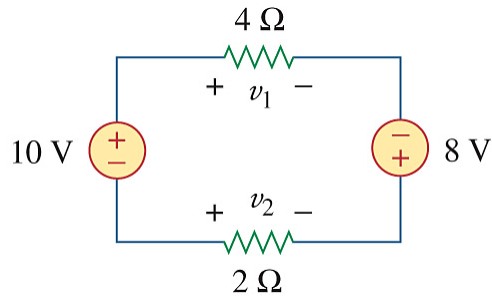


2.4 Kirchhoff's Laws (9)

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Practice Problem 2.5

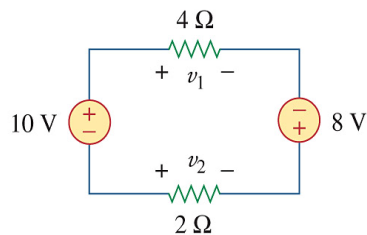
Find v_1 and v_2 in the circuit given below.



2.4 Kirchhoff's Laws (10)

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Solution to Practice Prob. 2.5



Applying KVL to the loop we get:

$$-10 + 4i - 8 + 2i = 0 \text{ which leads to } i = 3\text{A}$$

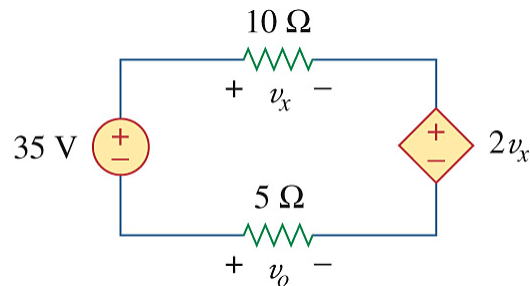
$$v_1 = 4i = \underline{12\text{V}} \quad \text{and} \quad v_2 = -2i = \underline{-6\text{V}}$$

2.4 Kirchhoff's Laws (11)

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Practice Problem 2.6

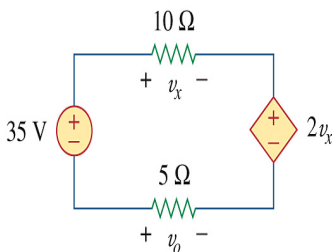
Find v_x and v_o in the circuit given below.



2.4 Kirchhoff's Laws (12)

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Solution to Practice Prob. 2.6



Applying KVL to the loop we get:

$$-35 + 10i + 2v_x + 5i = 0$$

But, $v_x = 10i$ and $v_o = -5i$. Hence,

$$-35 + 10i + 20i + 5i = 0 \text{ which leads to } i = 1\text{A.}$$

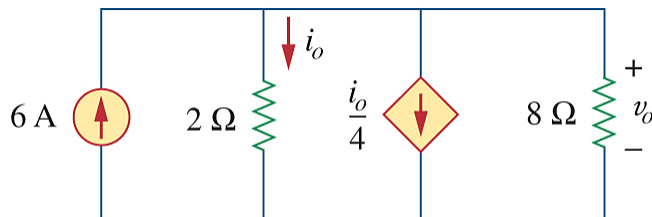
Thus, $v_x = \underline{10\text{V}}$ and $v_o = \underline{-5\text{V}}$

2.4 Kirchhoff's Laws (13)

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Practice Problem 2.7

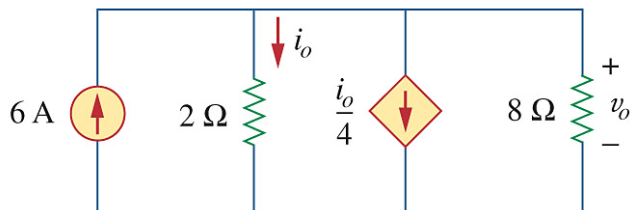
Find v_o and i_o in the circuit given below.



2.4 Kirchhoff's Laws (14)

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Solution to Practice Prob. 2.7



Applying KCL, $6 = i_o + [i_o/4] + [v_o/8]$, but $i_o = v_o/2$

Which leads to: $6 = (v_o/2) + (v_o/8) + (v_o/8)$

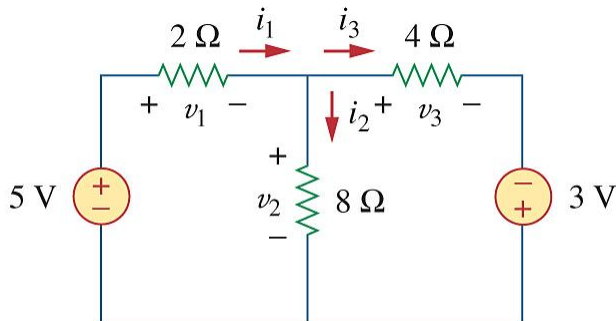
thus, $v_o = \underline{8V}$ and $i_o = \underline{4A}$

2.4 Kirchhoff's Laws (15)

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Practice Problem 2.8

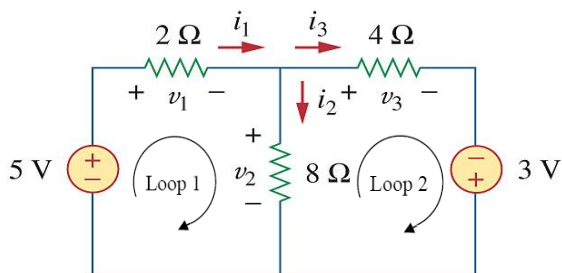
Find the currents and voltages in the circuit shown in the circuit given below.



2.4 Kirchhoff's Laws (16)

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Solution to Practice Prob. 2.8



KCL At the top node, $i_1 = i_2 + i_3$ (1)

KVL For loop 1 $-5 + V_1 + V_2 = 0$
or $V_1 = 5 - V_2$ (2)

KVL For loop 2 $-V_2 + V_3 - 3 = 0$
or $V_3 = V_2 + 3$ (3)

2.4 Kirchhoff's Laws (17)

cont. Solution to Practice Prob. 2.8

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Using (1) and Ohm's law, we get

$$(V_1/2) = (V_2/8) + (V_3/4)$$

and now using (2) and (3) in the above yields

$$[(5 - V_2)/2] = (V_2/8) + (V_2+3)/4$$

or $V_2 = \underline{2V}$

$$V_1 = 5 - V_2 = \underline{3V}, V_3 = 2 + 3 = \underline{5V}, i_1 = (5 - 2)/2 = \underline{1.5A},$$

$$i_2 = \underline{250 mA}, i_3 = \underline{1.25A}$$

2.5 Series Resistors & Voltage Division (1)

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□ What is Series?

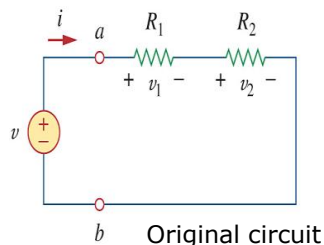
Two or more elements are in series if they **exclusively share a single node** and consequently **carry the same current**.

- The equivalent resistance of any number of resistors connected in a series is the sum of the individual resistances.

$$R_{eq} = R_1 + R_2 + \cdots + R_N = \sum_{n=1}^N R_n$$

2.5 Series Resistors & Voltage Division (2)

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Apply **KVL** (clockwise dir.)

$$-v + v_1 + v_2 = 0$$

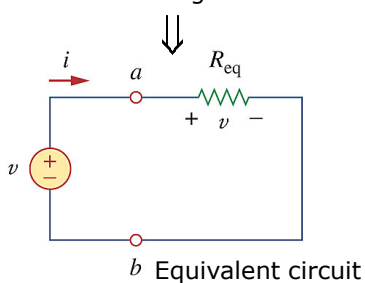
Apply **Ohm's Law**

$$-v + iR_1 + iR_2 = 0$$

$$i(R_1 + R_2) = v$$

$$i = \frac{v}{R_1 + R_2} = \frac{v}{R_{eq}}$$

$$\therefore R_{eq} = R_1 + R_2$$



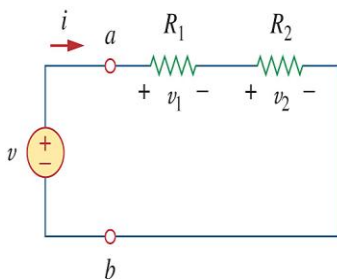
2.5 Series Resistors & Voltage Division (3)

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- To determine the voltage across each resistor;

Ohm's Law

$$v_1 = iR_1, \quad v_2 = iR_2$$



$$\text{Substitute: } i = \frac{v}{R_{eq}} = \frac{v}{R_1 + R_2}$$

$$v_1 = \frac{R_1}{R_1 + R_2} v, \quad v_2 = \frac{R_2}{R_1 + R_2} v$$

2.5 Series Resistors & Voltage Division (4)

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- Note that source voltage v is **divided among the resistors** in **direct proportion** to their resistances.

\Rightarrow *principle of voltage division*

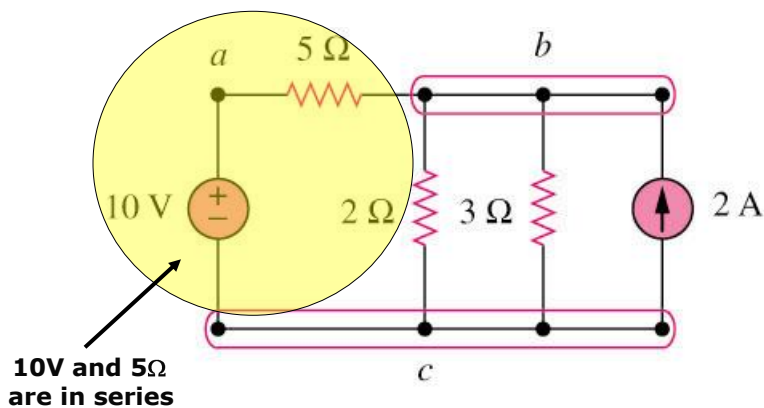
- In general, if a voltage supply has N resistors in series with the source voltage v , the n th resistor (R_n) can be expressed as:

$$v_n = \frac{R_n}{R_1 + R_2 + \cdots + R_N} v$$

2.5 Series Resistors & Voltage Division (5)

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Example 4



2.6 Parallel Resistors & Current Division (1)

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□ What is Parallel?

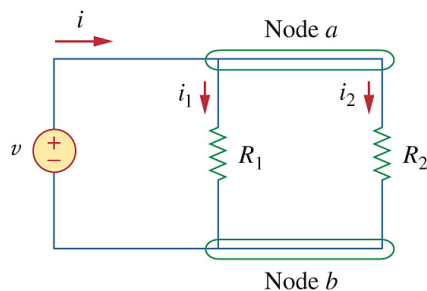
Two or more elements are in parallel if they are **connected to the same two nodes** and consequently have the **same voltage across them**.

- The equivalent resistance of **2 parallel resistors** is equal to the **product of their resistances divided by their sum**.

$$R_{eq} = \frac{R_1 R_2}{R_1 + R_2}$$

2.6 Parallel Resistors & Current Division (2)

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Apply **KCL** at node a

$$i = i_1 + i_2$$

Apply **Ohm's Law**

$$i = \frac{v}{R_1} + \frac{v}{R_2} = v \left(\frac{1}{R_1} + \frac{1}{R_2} \right) = \frac{v}{R_{eq}}$$

$$\therefore \frac{1}{R_{eq}} = \frac{1}{R_1} + \frac{1}{R_2}$$

$$R_{eq} = \frac{R_1 R_2}{R_1 + R_2}$$

2.6 Parallel Resistors & Current Division (3)

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- The equivalent **resistance** of a circuit with N resistors in parallel is:

$$\frac{1}{R_{eq}} = \frac{1}{R_1} + \frac{1}{R_2} + \cdots + \frac{1}{R_N}$$

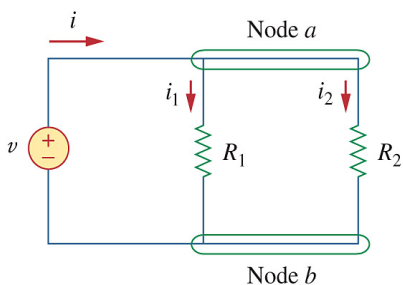
- The equivalent **conductance** of a circuit with N resistors in parallel is the sum of their individual conductance:

$$G_{eq} = G_1 + G_2 + \cdots + G_N$$

2.6 Parallel Resistors & Current Division (4)

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- To determine the current through each resistor;



Ohm's Law

$$i_1 = \frac{v}{R_1}, \quad i_2 = \frac{v}{R_2}$$

$$\text{Substitute: } v = iR_{eq} = \frac{iR_1R_2}{R_1 + R_2}$$

$$i_1 = \frac{iR_2}{R_1 + R_2}, \quad i_2 = \frac{iR_1}{R_1 + R_2}$$

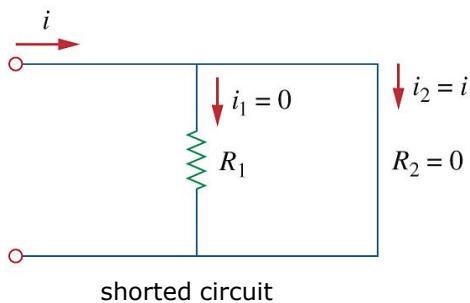
2.6 Parallel Resistors & Current Division (5)

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- Note that the total current i is shared by the resistors in **inverse proportion** to their resistances.

⇒ *principle of current division*

- Extreme cases:**

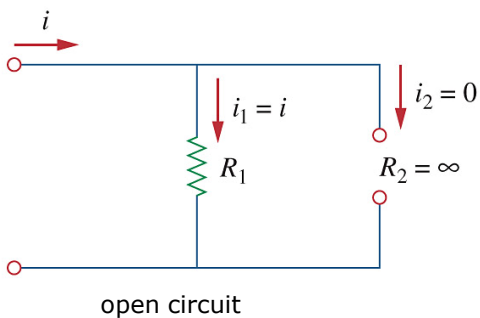


When $R_2=0$, the entire current i bypasses R_1 and flows through the short circuit $R_2=0$, the **path of least resistance**.

2.6 Parallel Resistors & Current Division (6)

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- cont. Extreme cases:**

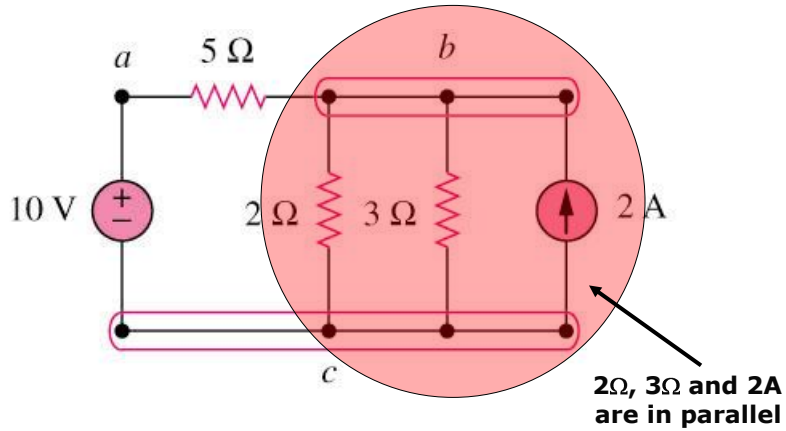


When $R_2= \infty$, the entire current i bypasses open circuited R_2 and flows through R_1 , the **path of least resistance**.

2.6 Parallel Resistors & Current Division (7)

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Example 5

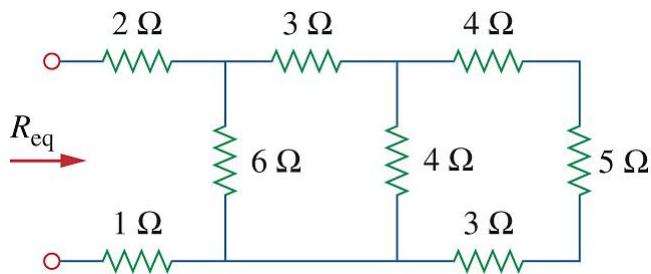


2.6 Parallel Resistors & Current Division (8)

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Practice Problem 2.9

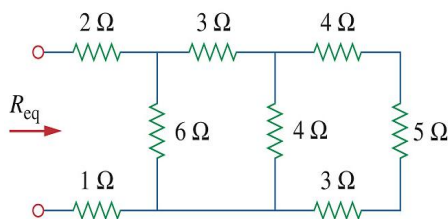
By combining the resistors in the circuit below, find R_{eq}



2.6 Parallel Resistors & Current Division (9)

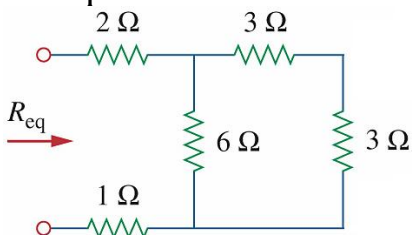
Soln to Practice Prob 2.9

53



Combining the 4Ω , 5Ω and 3Ω resistors in series gives $4+5+3 = 12\Omega$
 Then, $4\Omega // 12\Omega$ gives $[4 \times 12] / [4 + 12] = 3\Omega$

\therefore Equivalent circuit:



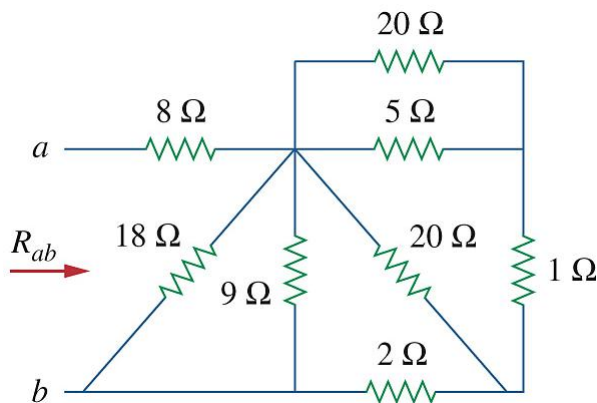
Thus, $R_{eq} = 1 + 2 + 6//6 = 6\Omega$

2.6 Parallel Resistors & Current Division (10)

54

Practice Problem 2.10

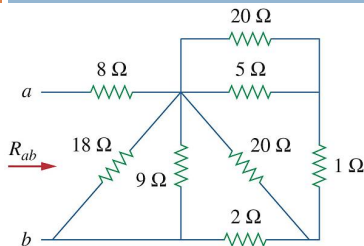
Find R_{ab} for the circuit shown below.



2.6 Parallel Resistors & Current Division (11)

Soln to Practice Prob 2.10

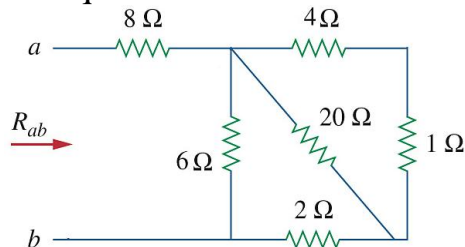
55



Combining $18\Omega // 9\Omega$ gives
 $[9 \times 18] / [9 + 18] = 6\Omega$

Then, $5\Omega // 20\Omega$ gives
 $[5 \times 20] / [5 + 20] = 4\Omega$

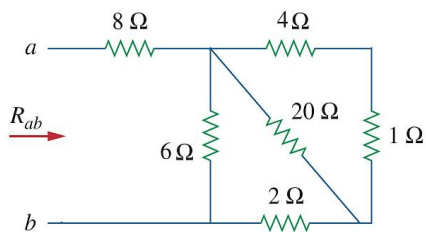
\therefore Equivalent circuit:



2.6 Parallel Resistors & Current Division (12)

cont. Soln to Practice Prob 2.10

56



Combine 4Ω and 1Ω , get 5Ω .

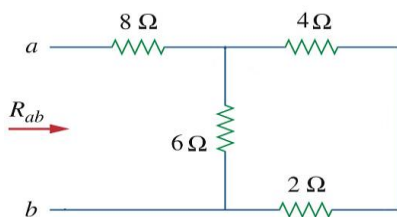
Then $5 // 20$ gives 4Ω .

\therefore Equivalent circuit:

Combine 4Ω and 2Ω , get 6Ω .

Then $6 // 6$ gives 3Ω .

Thus, $R_{eq} = 8 + 3$
 $= 11\Omega$

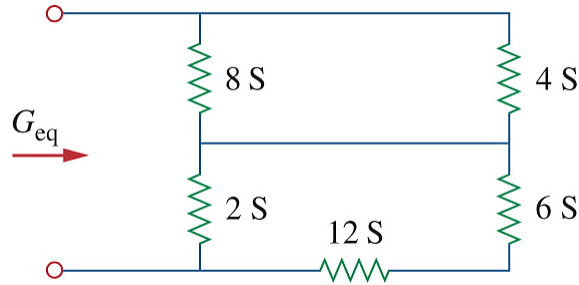


2.6 Parallel Resistors & Current Division (13)

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Practice Problem 2.11

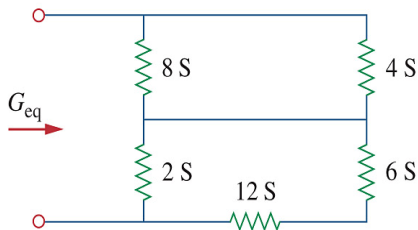
Calculate G_{eq} for the circuit shown below.



2.6 Parallel Resistors & Current Division (14)

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Soln to Practice Prob 2.11

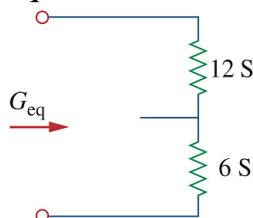


$$8//4 = 8+4 = 12 \text{ S}$$

$$6 \text{ in series with } 12 = [6 \times 12] / [6+12] = 4 \text{ S}$$

$$4//2 = 4+2 = 6 \text{ S}$$

\therefore Equivalent circuit:



$$12 \text{ in series with } 6 = [12 \times 6] / [12+6] = 4 \text{ S}$$

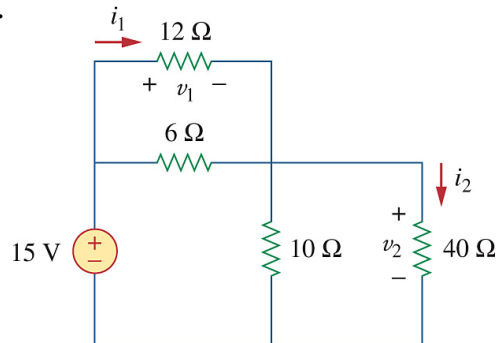
$$\text{Thus, } G_{eq} = 4 \text{ S}$$

2.6 Parallel Resistors & Current Division (15)

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Practice Problem 2.12

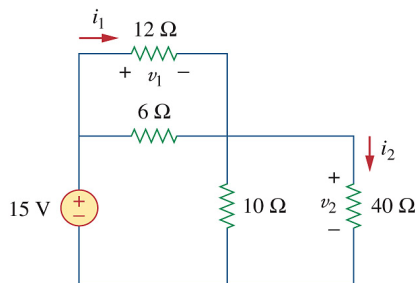
Find v_1 and v_2 for the circuit shown below. Also calculate i_1 and i_2 and the power dissipated in the 12Ω and 40Ω resistors.



2.6 Parallel Resistors & Current Division (16)

Soln to Practice Prob 2.12

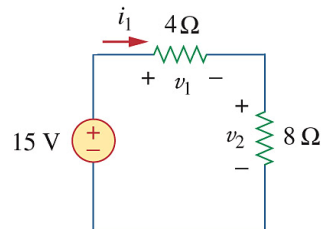
60



$$12//6 = [6 \times 12] / [6 + 12] = 4$$

$$10//40 = [10 \times 40] / [10 + 40] = 8$$

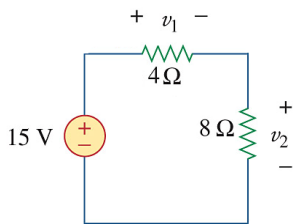
∴ Equivalent circuit:



2.6 Parallel Resistors & Current Division (17)

cont. Soln to Practice Prob 2.12

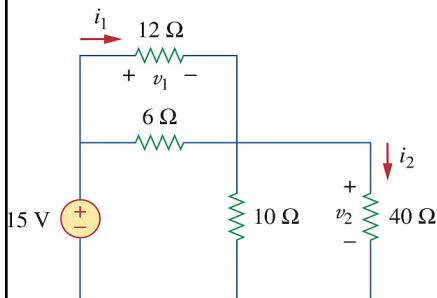
61



Use **voltage division**,

$$v_1 = [4/(4+8)](15) = 5\text{V}$$

$$v_2 = [8/(4+8)](15) = 10\text{V}$$



$$i_1 = v_1/12 = 5/12 = 416.7\text{mA}$$

$$i_2 = v_2/40 = 10/40 = 250\text{mA}$$

$$p_1 = v_1 i_1 = 5 \times (5/12) = 2.083\text{W}$$

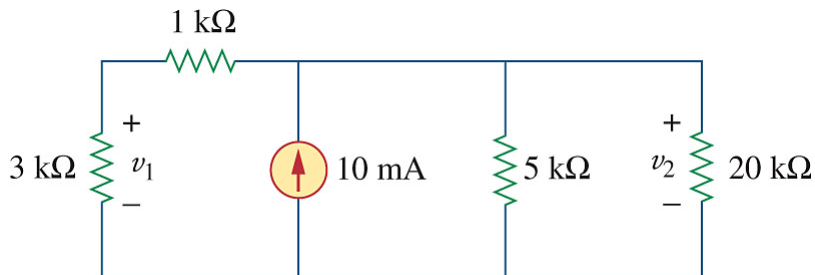
$$p_2 = v_2 i_2 = 10 \times (0.25) = 2.5\text{W}$$

2.6 Parallel Resistors & Current Division (18)

62

Practice Problem 2.12

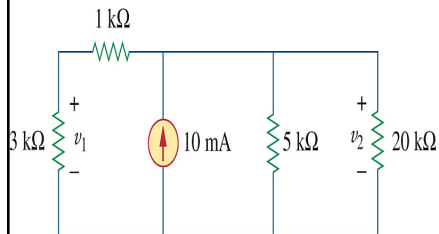
For the circuit given below, find: (a) v_1 and v_2 , (b) the power dissipated in the $3\text{k}\Omega$ and $20\text{k}\Omega$ resistors, and (c) the power supplied by the current source.



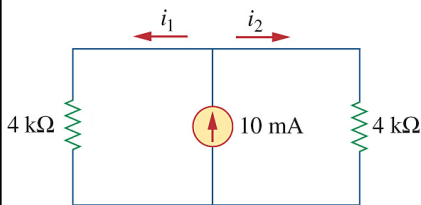
2.6 Parallel Resistors & Current Division (19)

Soln to Practice Prob 2.13

63



Simplify circuit, to get:



Use **current division**,

$$i_1 = i_2 = 10\text{mA} \left[\frac{4}{4+4} \right] = 5\text{mA}$$

Ohms' Law

$$v_1 = 5\text{mA} \times 3\text{k} = 15\text{V}$$

$$v_2 = 5\text{mA} \times 4\text{k} = 20\text{V}$$

$$p_{3k} = v_1 i_1 = 15 \times 5\text{mA} = 75\text{mW}$$

$$p_{20k} = v_2^2 / 20\text{k} = 400 / 20\text{k} = 20\text{mW}$$

Power supplied, $p_o = v_o i_o$

$$v_o = 4\text{k} \times i_1 = 4\text{k} \times 5\text{mA} = 20\text{V}$$

$$p_o = 20\text{V} \times 10\text{mA} = 200\text{mW}$$

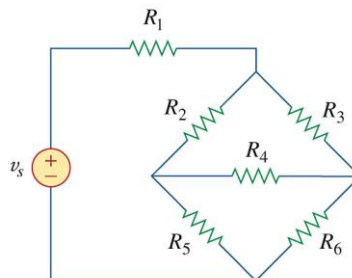
2.7 Wye-Delta Transformations (1)

64

□ Why Transform?

Often, in circuit analysis, the resistors are NOT in parallel nor series.

Example:



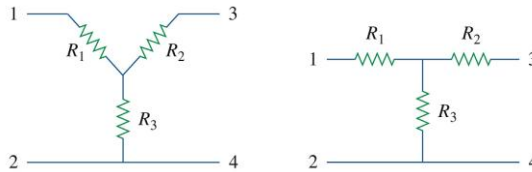
- The equivalent resistance is found by **simplifying** circuits **using three-terminal equivalent networks**.

2.7 Wye-Delta Transformations (2)

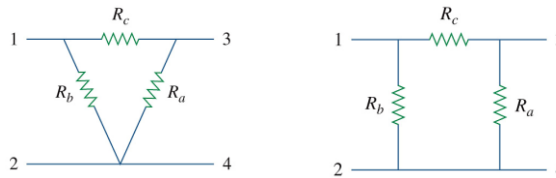
65

□ Three-terminal network equivalents

(i) wye (Y) or tee (T)



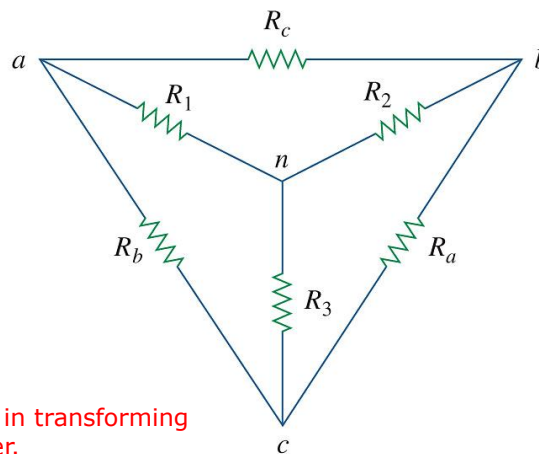
(ii) delta (Δ) or pi (Π)



2.7 Wye-Delta Transformations (3)

66

□ Superposition of Y and Δ networks



Used as an aid in transforming one to the other.

2.7 Wye-Delta Transformations (4)

67

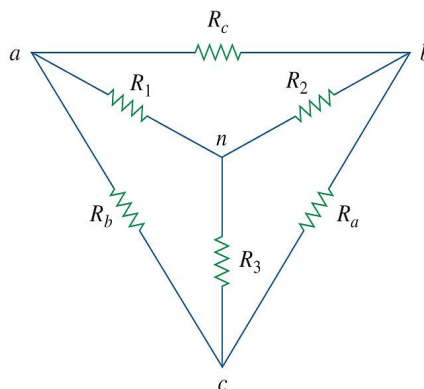
□ Delta to Wye Conversion

Each resistor in the Y network is a **product of the resistors in adjacent Δ branches**, **divided by the sum of the three Δ resistors**.

$$R_1 = \frac{R_b R_c}{(R_a + R_b + R_c)}$$

$$R_2 = \frac{R_c R_a}{(R_a + R_b + R_c)}$$

$$R_3 = \frac{R_a R_b}{(R_a + R_b + R_c)}$$



2.7 Wye-Delta Transformations (5)

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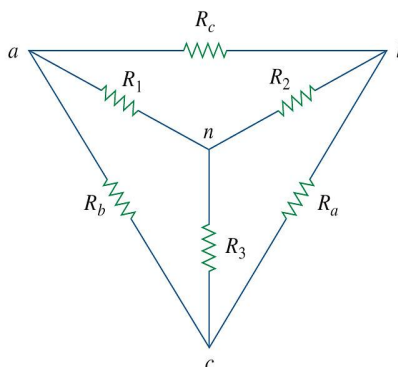
□ Wye to Delta Conversion

Each resistor in the Δ network is the **sum of all possible products of Y resistors taken two at a time**, **divided by the opposite Y resistor**.

$$R_a = \frac{R_1 R_2 + R_2 R_3 + R_3 R_1}{R_1}$$

$$R_b = \frac{R_1 R_2 + R_2 R_3 + R_3 R_1}{R_2}$$

$$R_c = \frac{R_1 R_2 + R_2 R_3 + R_3 R_1}{R_3}$$

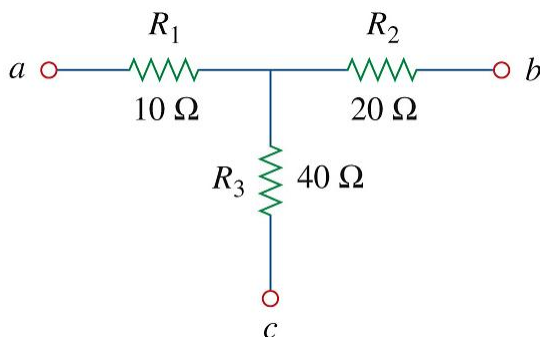


2.7 Wye-Delta Transformations (6)

69

Practice Problem 2.14

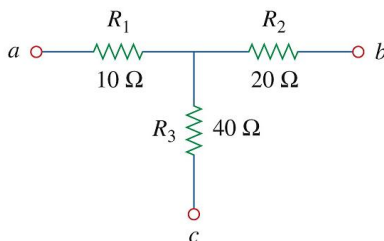
Transform the wye network, in the figure shown below, to a delta network.



2.7 Wye-Delta Transformations (7)

70

Solution for P.P. 2.14



$$R_a = [R_1 R_2 + R_2 R_3 + R_3 R_1] / R_1 = [10 \times 20 + 20 \times 40 + 40 \times 10] / 10 = \underline{\underline{140 \text{ ohms}}}$$

$$R_b = [R_1 R_2 + R_2 R_3 + R_3 R_1] / R_2 = 1400 / 20 = \underline{\underline{70 \text{ ohms}}}$$

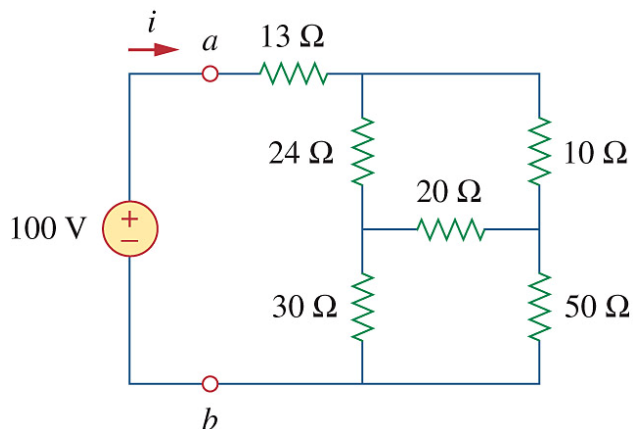
$$R_c = [R_1 R_2 + R_2 R_3 + R_3 R_1] / R_3 = 1400 / 40 = \underline{\underline{35 \text{ ohms}}}$$

2.7 Wye-Delta Transformations (8)

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Practice Problem 2.15

For the bridge network in the figure below, find R_{ab} and i .

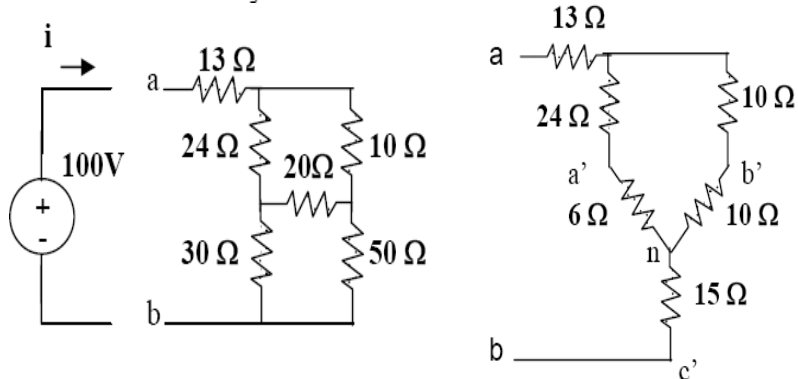


2.7 Wye-Delta Transformations (9)

72

Solution for P.P. 2.15

We first find the equivalent resistance, R . We convert the delta sub-network to a wye connected form as shown below:



2.7 Wye-Delta Transformations (10)

73

cont. Solution for P.P. 2.15

$$R_{a'n} = 20 \times 30 / [20 + 30 + 50] = 6 \text{ ohms}$$

$$R_{b'n} = 20 \times 50 / 100 = 10 \text{ ohms}$$

$$R_{c'n} = 30 \times 50 / 100 = 15 \text{ ohms}$$

$$\text{Thus, } R_{ab} = 13 + (24 + 6) \parallel ((10 + 10) + 15) = 28 + 30 \times 20 / (30 + 20) = \underline{\underline{40 \text{ ohms.}}}$$

$$i = 100 / R_{ab} = 100 / 40 = \underline{\underline{2.5 \text{ amps}}}$$