## Example 8-4

For the circuit shown in Fig. 8-7, design the resistor values to meet these specifications:

$$
\begin{array}{ll}
V_{C C}=10 \mathrm{~V} & V_{C E} @ \text { midpoint } \\
I_{C}=10 \mathrm{~mA} & 2 \mathrm{~N} 3904{ }^{\prime} \mathrm{s} \beta_{\mathrm{dc}}=100-300
\end{array}
$$

SOLIITION First, establish the emitter voltage by:

$$
\begin{aligned}
& V_{E}=0.1 V_{C C} \\
& V_{E}=(0.1)(10 \mathrm{~V})=1 \mathrm{~V}
\end{aligned}
$$

The emitter resistor is found by:

$$
\begin{aligned}
& R_{E}=\frac{V_{E}}{I_{E}} \\
& R_{E}=\frac{1 \mathrm{~V}}{10 \mathrm{~mA}}=100 \Omega
\end{aligned}
$$

The collector resistor is:

$$
\begin{aligned}
& R_{C}=4 R_{E} \\
& R_{C}=(4)(100 \Omega)=400 \Omega(\text { use } 390 \Omega)
\end{aligned}
$$

Next, choose either a stiff or firm voltage divider. A stiff value of $R_{2}$ is found by:

$$
\begin{aligned}
& R_{2} \leq 0.01 \beta_{\mathrm{dc}} R_{E} \\
& R_{2} \leq(0.01)(100)(100 \Omega)=100 \Omega
\end{aligned}
$$

Now, the value of $R_{1}$ is:

$$
\begin{aligned}
& R_{1}=\frac{V_{1}}{V_{2}} R_{2} \\
& V_{2}=V_{E}+0.7 \mathrm{~V}=1 \mathrm{~V}+0.7 \mathrm{~V}=1.7 \mathrm{~V} \\
& V_{1}=V_{C C}-V_{2}=10 \mathrm{~V}-1.7 \mathrm{~V}=8.3 \mathrm{~V} \\
& R_{1}=\left(\frac{8.3 \mathrm{~V}}{1.7 \mathrm{~V}}\right)(100 \Omega)=488 \Omega \text { (use } 490 \Omega \text { ) }
\end{aligned}
$$

PRACTICE PROBLEM 8-4 Using the given VDB design guidelines, design the VDB circuit of Fig. 8-7 to meet these specifications:

$$
\begin{array}{lll}
V_{C C}=10 \mathrm{~V} & V_{C E} @ \text { midpoint } & \text { stiff voltage divider } \\
I_{C}=1 \mathrm{~mA} & \beta_{\mathrm{dc}}=70-200 &
\end{array}
$$

## 8-4 Two-Supply Emitter Bias

Some electronic equipment has a power supply that produces both positive and negative supply voltages. For instance, Fig. $8-8$ shows a transistor circuit with two power supplies: +10 and -2 V . The negative supply forward biases the emitter

## GOOD TO KNOW

When transistors are biased using well-designed voltage-divider or emitter-bias configurations, they are classified as beta-independent circuits because the values of $I_{C}$ and $V_{C E}$ are unaffected by changes in the transistor's beta.

Figure 8-10 Base voltage is idealiy zero.


Figure 8-8 Two-supply emitter bias.


Figure 8-9 Redrawn TSEB circuit.

diode. The positive supply reverse biases the collector diode. This circuit is derived from emitter bias. For this reason, we refer to it as two-supply emitter bias (TSEB).

## Analysis

The first thing to do is to redraw the circuit as it usually appears on schematic diagrams. This means deleting the battery symbols, as shown in Fig. 8-9. This is necessary on schematic diagrams because there usually is no room for battery symbols on complicated diagrams. All the information is still on the diagram, except that it is in condensed form. That is, a negative supply voltage of -2 V is applied to the bottom of the $1 \mathrm{k} \Omega$, and a positive supply voltage of +10 V is applied to the top of the $3.6-\mathrm{k} \Omega$ resistor.

When this type of circuit is correctly designed, the base current will be small enough to ignore. This is equivalent to saying that the base voltage is approximately 0 V , as shown in Fig. 8-10.

The voltage across the emitter diode is 0.7 V , which is why -0.7 V is shown on the emitter node. If this is not clear, stop and think about it. There is a plus-to-minus drop of 0.7 V in going from the base to the emitter. If the base voltage is 0 V , the emitter voltage must be -0.7 V .

In Fig. 8-10, the emitter resistor again plays the key role in setting up the emitter current. To find this current, apply. Ohm's law to the emitter resistor as follows: The top of the emitter resistor has a voltage of -0.7 V , and the bottom has a voltage of -2 V . Therefore, the voltage across the emitter resistor equals the difference between the two voltages. To get the right answer, subtract the more negative value from the more positive value. In this case, the more negative value is -2 V , so:

$$
V_{R E}=-0.7 \mathrm{~V}-(-2 \mathrm{~V})=1.3 \mathrm{~V}
$$

Once you have found the voltage across the emitter resistor, calculate the emitter current with Ohm's law:

$$
I_{E}=\frac{1.3 \mathrm{~V}}{1 \mathrm{k} \Omega}=1.3 \mathrm{~mA}
$$

This current flows through the $3.6 \mathrm{k} \Omega$ and produces a voltage drop that we subtract from +10 V as follows:

$$
V_{C}=10 \mathrm{~V}-(1.3 \mathrm{~mA})(3.6 \mathrm{k} \Omega)=5.32 \mathrm{~V}
$$

The collector-emitter voltage is the difference between the collector voltage and the emitter voltage:

$$
V_{C E}=5.32 \mathrm{~V}-(-0.7 \mathrm{~V})=6.02 \mathrm{~V}
$$

When two-supply emitter bias is well designed, it is similar to voltagedivider bias and satisfies this $100: 1$ rule:

$$
\begin{equation*}
R_{\mathcal{B}}<0.01 \beta_{\mathrm{dc}} R_{E} \tag{8-12}
\end{equation*}
$$

In this case, the simplified equations for analysis are:

$$
\begin{align*}
V_{B} & \approx 0  \tag{8-13}\\
I_{E} & =\frac{V_{E E}-0.7 \mathrm{~V}}{R_{E}}  \tag{8-14}\\
V_{C} & =V_{C C}-I_{C} R_{C}  \tag{8-15}\\
V_{C E} & =V_{C}+0.7 \mathrm{~V} \tag{8-16}
\end{align*}
$$

## Base Voltage

One source of error in the simplified method is the small voltage across the base resistor of Fig. 8-10. Since a small base current flows through this resistance, a negative voltage exists between the base and ground. In a well-designed circuit, this base voltage is less than -0.1 V . If a designer has to compromise by using a larger base resistance, the voltage may be more negative than -0.1 V . If you are troubleshooting a circuit like this, the voltage between the base and ground should produce a low reading; otherwise, something is wrong with the circuit.

## Example 8-5


What is the collector voltage in Fig. 8 -10 if the emitter resistor is increased to $1.8 \mathrm{k} \Omega$ ?
SOLUTION The voltage across the emitter resistor is still 1.3 V . The emitter current is:

$$
I_{E}=\frac{1.3 \mathrm{~V}}{1.8 \mathrm{k} \Omega}=0.722 \mathrm{~mA}
$$

The collector voltage is:

$$
V_{C}=10 \mathrm{~V}-(0.722 \mathrm{~mA})(3.6 \mathrm{k} \Omega)=7.4 \mathrm{~V}
$$

PRACTICE PROBLEM 8-5 Change the emitter resistor of Fig. $8-10$ to $2 \mathrm{k} \Omega$ and solve for $V_{C E}$.

## Example 8-6

A stage is a transistor and the passive components connected to it. Figure 8-11 shows a three-stage circuit using twosupply emitter bias. What are the collector-to-ground voltages for each stage in Fig. 8-11?

SOLUTION To begin with, ignore the capacitors because they appear as open circuits to do voltage and currents. Then, we are left with three isolated transistors, each using two-supply emitter bias.

The first stage has an emitter current of:

$$
I_{E}=\frac{15 \mathrm{~V}-0.7 \mathrm{~V}}{20 \mathrm{k} \Omega}=\frac{143 \mathrm{~V}}{20 \mathrm{k} \Omega}=0.715 \mathrm{~mA}
$$

and a collector voltage of:

$$
V_{C}=15 \mathrm{~V}-(0.715 \mathrm{~mA})(10 \mathrm{k} \Omega)=7.85 \mathrm{~V}
$$

Since the other stages have the same circuit values, each has a collector-to-ground voltage of approximately 7.85 V . Summary Table 8-1 illustrates the four main types of bias circuits.

PRACIICE PROBLEM 8-6 Change the supply voltages of Fig. 8-11 to +12 V and -12 V . Then, calculate $V_{C E}$ for each transistor.

Figure 8-11 Three-stage circuit.


## Summary Table 8-1 Wam Bias Cicuits

Type

Base bias


Emitter bias


Voltage divider bias


Calculations
$I_{B}=\frac{V_{B B}-0.7 \mathrm{~V}}{R_{B}}$
$I_{C}=\beta I_{B}$.
$V_{C E}=V_{C C}-I_{C} R_{C}$
$V_{E}=V_{B B}-0.7 \mathrm{~V}$
$I_{E}=\frac{V_{E}}{R_{E}}$
$V_{C}=V_{C}-I_{C} R_{C}$
$V_{C E}=V_{C}-V_{E}$

Characteristics
Few parts; $\beta$ dependent: fixed base
current

Fixed emitter
current; $\beta$ independent

Needs more resistors; $\beta$ independent; needs only one power supply

Where used

Switch; digital
$I_{C}$ driver: amplifier
. 1
$V_{B}=\frac{R_{2}}{R_{1}+R_{2}} V_{C C}$
$V_{E}=V_{B}-0.7 \mathrm{~V}$
$I_{E}=\frac{V_{E}}{R_{E}}$
$V_{C}=V_{C C}-I_{C} R_{C}$
$V_{C E}=V_{C}-V_{E}$

