

After simplification we get:

$$\left(\frac{C}{n_0}\right) = P_t \eta_t \eta_r \frac{A_t A_r}{\lambda^2 r^2 l_0 k t_s}$$

⇒ Fixed Antenna Size Link:

Put all fixed values in brackets and we rewrite C/n₀:

$$\left(\frac{C}{n_0}\right) = \left(\frac{\eta_t \eta_r A_t A_r}{l_0 k}\right) \frac{P_t}{\lambda^2 r^2 t_s}$$

⇒ Fixed Antenna Gain Link:

$$\left(\frac{C}{n_0}\right) = \frac{P_t g_t g_r}{\left(\frac{4\pi r}{\lambda}\right)^2 l_0 k t_s} = \underbrace{\left[\frac{g_t g_r}{(4\pi)^2 l_0 k}\right]}_{\text{fixed parameter.}} \frac{P_t \lambda^2}{r^2 t_s}$$

⇒ Fixed Antenna Gain & Antenna Size:

* first quantify satellite coverage requirement.

$$\Omega = \frac{A_s}{d_s^2}$$

Note: $\Omega = 4\pi$ for complete sphere.

*

$$g_t \approx \frac{1}{\Omega} \Rightarrow g_t \approx \frac{K_1}{\Omega} = \frac{K_1 d_s^2}{A_s}$$

* So C/n₀ becomes:

$$\left(\frac{C}{n_0}\right) = \frac{P_t g_t g_r}{l_0 k t_s} = \frac{P_t \left(\frac{K_1 r^2}{A_s}\right) \left(\eta_r \frac{4\pi A_r}{\lambda^2}\right)}{\left(\frac{4\pi r}{\lambda}\right)^2 l_0 k t_s}$$

$$\left(\frac{C}{n_0}\right) = \left[\frac{K_1 \eta_r A_r}{4\pi A_s l_0 k}\right] \frac{P_t}{t_s}$$

Chapter #4 :- PROBLEMS

Q. 1:

① Find gain of parabolic antenna = ? ^{dbi}

$$d = 3\text{m}, \quad f_1 = 6\text{GHz}, \quad f_2 = 14\text{GHz}$$

We know that for parabolic reflector antenna the gain 'g' is given by:

$$g = \eta_A \left(\frac{\pi d}{\lambda} \right)^2$$

$$\text{where } \lambda = \frac{c}{f}$$

$$\text{and } c = 3 \times 10^8 \text{ m/s}$$

So, it implies that,

$$g = 109.66 f^2 d^2 \eta_A$$

To find gain in dbi,

$$G = 10 \log (109.66 f^2 d^2 \eta_A)$$

We also know that $\eta_A = 0.55$, $d = 3\text{m}$

So, for f_1 :

$$G = 10 \log (109.66 \times (6)^2 \times (3)^2 \times 0.55)$$

$$= 10 \log (109.66 \times 36 \times 9 \times 0.55)$$

$$= 10 \log (19541.41)$$

$$\boxed{G_1 = 42.9 \text{ dbi}}$$

For f_2 :

$$G = 10 \log (109.66 \times (14)^2 \times (3)^2 \times 0.55)$$

$$= 10 \log (109.66 \times 196 \times 9 \times 0.55)$$

$$= 10 \log (106392.13)$$

$$\boxed{G_2 = 50.26 \text{ dbi}}$$

⑥ find gain in dBi = ?, effective area = ?

$$d = 30 \text{ m}, \quad f = 4 \text{ GHz}$$

we already know that:

$$G = 10 \log(109.66 \times (4)^2 \times (30)^2 \times 0.55)$$

$$= 10 \log(109.66 \times 16 \times 900 \times 0.55)$$

$$= 10 \log(868507.2)$$

$$G = 59.38 \text{ dBi}$$

To find Effective area we use following formula:

$$A_e = \eta_A A$$

where: $A = \frac{\pi d^2}{4}$ (for parabolic reflector antenna).

$$A = \frac{(\pi)(30)^2}{4} = \frac{3.14 \times 900}{4}$$

$$A = 706.5 \text{ m}^2$$

$$\rightarrow A_e = (0.55)(706.5)$$

$$\boxed{A_e = 388.575 \text{ m}^2}$$

⑦ Find $A_e = ?$, gain = 46 dBi, $f = 12 \text{ GHz}$, $\eta_A = 0.55$

we know, from gain formula:

$$G = 10 \log(109.66 \times f^2 \times d^2 \times \eta_A)$$

$$46 = 10 \log(109.66 \times (12)^2 \times d^2 \times 0.55)$$

$$46 = 10 \log(8685.072 d^2)$$

$$4.6 = \log(8685.072 d^2)$$

Take antilog on both sides:

$$8685.072 d^2 = 10^{4.6} \Rightarrow d^2 = \frac{10^{4.6}}{8685.072}$$

$$d^2 = 4.5838 \Rightarrow d = 2.14 \text{ m}$$

we also know, $A_e = \eta_A A$.

$$\text{where } A = \frac{\pi d^2}{4} = \frac{3.14 \times (2.14)^2}{4} = 3.59 \text{ m}^2$$

$$\therefore, A_e = (0.55)(3.59)$$

$$\boxed{A_e = 1.977 \text{ m}^2}$$

Q. 2: (a) $r = ?$ and $L_{FS} = ?$, $f = 12 \text{ GHz}$, GSO link (2)

As the satellite link is a GSO link orbit, so we can take the GSO orbit range as $r = 35900 \text{ km}$

we have formula for L_{FS} as:

$$L_{FS} = \left(\frac{40\pi}{3} r f \right)^2 \quad \text{where } r \text{ is in meters} \\ \text{and } f \text{ is in GHz}$$

$$L_{FS} = \left(\frac{(40)(3.14)(35900 \times 1000)(12)}{3} \right)^2$$

$$L_{FS} = (1.8036)^2$$

$$L_{FS} = 3.25 \times 10^2$$

we convert it to dB as:

$$L_{FS} = 10 \log(L_{FS})$$

$$\boxed{L_{FS} = 205.12 \text{ dB}}$$

Alternate Method:

$$L_{FS} = 20 \log(f) + 20 \log(r) + 92.44$$

$$= 20 \log(12) + 20 \log(35900) + 92.44$$

$$= 21.58 + 91.10 + 92.44$$

$$\boxed{L_{FS} = 205.12 \text{ dB}}$$

(b)

range, $r = 780 \text{ km}$,

service link freq. = $1600 \text{ MHz} = 1.6 \text{ GHz}$.

Feeder " " , $UL = 29.2 \text{ GHz}$

" " " , $DL = 19.5 \text{ GHz}$

Find $L_{FS} = ?$, $L_{FS(UL)} = ?$, $L_{FS(DL)} = ?$

We know the formula for L_{FS} as:

$$\begin{aligned} L_{FS} &= 20 \log(f) + 20 \log(r) + 92.44 \\ &= 20 \log(1.6) + 20 \log(780) + 92.44 \end{aligned}$$

$$\boxed{L_{FS} = 154.36 \text{ dB}}$$

$$\begin{aligned} L_{FS(UL)} &= L_{FS} + 20 \log\left(\frac{f_u}{f_s}\right) \\ &= 154.36 + 20 \log\left(\frac{29.24 \text{ GHz}}{1.6 \text{ GHz}}\right) \\ &= 154.36 + 20 \log(18.275) \\ &= 154.36 + 25.23 \end{aligned}$$

$$\boxed{L_{FS(UL)} = 179.59 \text{ dB}}$$

$$\begin{aligned} L_{FS(DL)} &= L_{FS} + 20 \log\left(\frac{f_d}{f_s}\right) \\ &= 154.36 + 20 \log\left(\frac{19.5 \text{ GHz}}{1.6 \text{ GHz}}\right) \\ &= 154.36 + 21.718 \end{aligned}$$

$$\boxed{L_{FS(DL)} = 176.07 \text{ dB}}$$

Q.3.

Antenna diameter = $d = 0.66 \text{ m}$,

LNR has noise figure = $NF = 4 \text{ dB}$

Cable line loss = $A = 1.5 \text{ dB}$

Down converter gain = $G_{DC} = 10 \text{ dB}$

" " temp = $t_{DC} = 2800^\circ \text{K}$

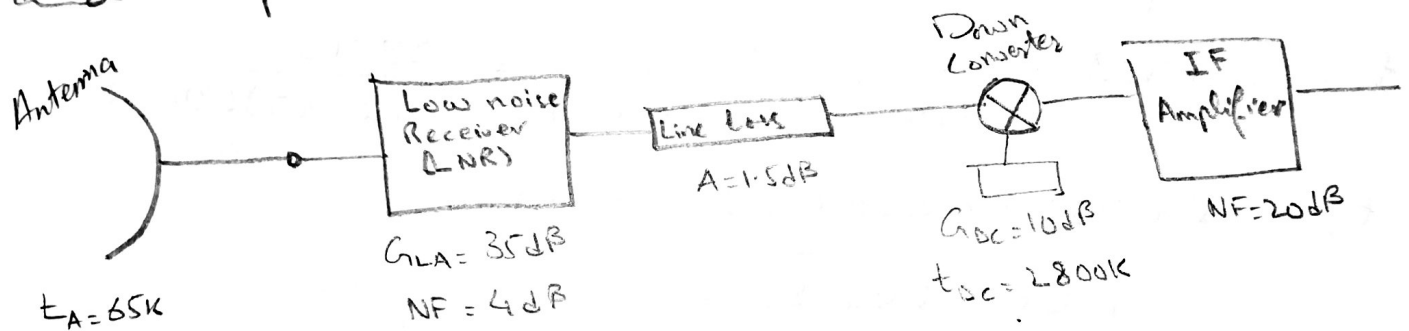
IF amplifier has $NF = NF = 20 \text{ dB}$

LNR has gain of = $G_{LA} = 35 \text{ dB}$

Antenna temp = $t_A = 65^\circ \text{K}$

(9) Find $t_s = ?$ $NFs = ?$

On the basis of the VSAT receiver information and parameters we draw the overall receiver system and respective values as below:



Formula for the calculation of system noise temperature is:

$$t_s = t_A + t_{LA} + \frac{290(l-1)}{g_{LA}} + \frac{t_{DC}}{l g_{LA}} + \frac{t_{IF}}{g_{DC} (1/l) g_{LA}} \quad \text{--- (1)}$$

Now we find the values of each gain and noise temp.

Antenna: $t_A = 65^\circ \text{K}$

LNR: $t_{LA} = 290(10^{NF/10} - 1)$
 $= 290(10^{4/10} - 1)$
 $= 290(1.51)$

$t_{LA} = 438 \text{ K}$

Downconverter: $t_{DC} = 2800^\circ \text{K}$

IF Amp: $t_{IF} = 290(10^{NF/10} - 1) = 290(10^{20/10} - 1)$
 $= 290(99) \Rightarrow t_{IF} = 28710 \text{ K}$

IF amplifier: $t_{IF} = 28710^{\circ}K$

Line: $t_{e1w} = 290(l-1)$
 $= 290(10^{1.5/10} - 1)$
 $= 290(0.41)$
 $t_{e1w} = 119^{\circ}K$

Now we calculate respective gains:

$$g_{LA} = 10^{35/10} = 3162$$

$$\therefore G(dB) = 10 \log(g)$$

$$g_{DC} = 10^{10/10} = 10$$

$$1/e = \frac{1}{10^{1.5/10}} = \frac{1}{10^{0.15}} = 0.707$$

Now put all above calculated values into eq ①.

$$t_s = 65 + 438 + \frac{119}{3162} + \frac{2800}{(0.707)(3162)} + \frac{28710}{10(0.707)(3162)}$$

$$t_s = 65 + 438 + 0.038 + 1.252 + 1.286$$

$$\boxed{t_s = 505.57 K}$$

We have system noise figure formula as:

$$NF_s = 10 \log \left(1 + \frac{t_s}{290} \right)$$

$$NF_s = 10 \log \left(1 + \frac{505.57}{290} \right) = 10 \log (1 + 1.743)$$

$$NF_s = 10 \log (2.743)$$

$$\boxed{NF_s = 4.382 dB}$$

Q. 3. (b) Find figure of merit = $M = G/T$?

$f = 12.5 \text{ GHz}$, $\eta_A = 0.55$, $d = 0.66 \text{ m}$

We first solve for G in dB:

$$G_r = 10 \log(109.66 \times f^2 \times d^2 \times \eta_A)$$

$$= 10 \log(109.66 \times (12.5)^2 \times (0.66)^2 \times (0.55))$$

$$= 10 \log(4105.05)$$

$G_r = 36.13 \text{ dB}$

Then T_s :

$$T_s = 10 \log(t_s)$$

$$= 10 \log(505.57)$$

$$= 27.03 \text{ dB/K}$$

$$M = \frac{G}{T} = G_r - T_s$$

$$= 36.13 \text{ dB} - 27.03$$

$\frac{G}{T} = 9.1 \text{ dB/K}$

Q. 4. $R_b = \text{bit rate} = 60 \text{ Mbps}$, $E_b/N_0 = 9.5 \text{ dB}$

(a) Find $C/N_0 = ?$

we know that: $\frac{e_b}{n_0} = \frac{1}{R_b} \left(\frac{C}{n_0} \right)$ ——— (1)

Convert it from dB:

$$\frac{E_b}{N_0} = 10 \log \left(\frac{e_b}{n_0} \right)$$

$$9.5 = 10 \log \left(\frac{e_b}{n_0} \right) \Rightarrow \frac{e_b}{n_0} = 10^{0.95}$$

$$\frac{e_b}{n_0} = 8.912$$

Put in eq (1)

$$8.912 = \frac{1}{60 \text{ Mbps}} \left(\frac{e}{n_0} \right)$$

$$\frac{C}{n_0} = 8.912 \times 60 \times 10^6 \text{ bps}$$

$$\frac{C}{n_0} = 534.72 \times 10^6$$

$$\frac{C}{N_0} = 10 \log(534.72 \times 10^6)$$

$$\frac{C}{N_0} = 87.28 \text{ dBHz}$$

(b)

As $\frac{E_b}{N_0} = 9.5 \text{ dB}$ and we have Uplink

noise contribution to downlink is 1.5 dB .

$$\text{Now, } \frac{E_b}{N_0} = 9.5 \text{ dB} - 1.5 \text{ dB} = 8 \text{ dB}$$

$$\frac{e_b}{n_0} = 10^{0.8}$$

$$\frac{e_b}{n_0} = 6.309$$

Now we know that: (Page 366)

$$\begin{aligned} \text{BER} &\approx \frac{e^{-(e_b/n_0)}}{\sqrt{4\pi(e_b/n_0)}} \\ &\approx \frac{e^{-(6.309)}}{\sqrt{(4 \times (3.14) \times (6.309))}} \\ &\approx \frac{1.819 \times 10^{-3}}{\sqrt{79.28}} = \frac{1.819 \times 10^{-3}}{8.904} \end{aligned}$$

$$\text{BER} \approx 2.0429 \times 10^{-4}$$