## **LECTURE # 9**



# In this lecture you will learn about:

Numerical of:

- Lecture 6
- Lecture 7
- Lecture 8

#### **Course Name:**

"Introduction To Earthquake Engineering"

Course Code: CT-634 Credit Hours: 3 Semester: 6<sup>TH</sup>

**Prepared By: Engr. Khurshid Alam** 

#### PROBLEM # 1

Determine lateral stiffness of the frame if a lateral load is applied at beam level. Assume:

1. The flexural stiffness of beam is too high as compared to that of connected columns.

2. Axial deformations in beam is negligible







20 ft



#### SOLUTION



= 3759 k/ft

#### PROBLEM # 2



Determine the stiffness of cantilever beam by assuming that the self weight of beam is negligible Take  $\mathbf{E} = 29,000 \text{ ksi}, \mathbf{k}_{\text{spring}} = 200 \text{ lb/ft}.$ 





#### SOLUTION

$$k_{1} = 200 \, lb/ft$$

$$k_{2} = \frac{3EI}{l^{3}} = \frac{3 \times \left(29000 \, k/_{in^{2}}\right) \times \left(\frac{\pi}{64} \times (2 \, in)^{2}\right)}{(10 \times 12 \, in)^{3}}$$

$$= 0.0396 \, k/in^2 = 474.7 \, lb/ft$$

$$k_{eq} = \frac{k_1 k_2}{k_1 + k_2} = \frac{200 \times 474.7}{200 + 474.7}$$

 $k_{eq} = 140.7 \, lb/ft$ 

PB: GIVEN DATA: Mass, m= 2 kg Halmonic Force, p(t): 15 5in 75t N Amplitude, por 25 N N Foxce Frequency, we 75 lad/sec Voz 0.005 m Modulus Of Elasticity, EAR. e 71 GPg 271. 20 Po Length, L = 0.5 m REQUIRED : Diameter, de?

Foo

SOLUTION:

Uo Rdz 1) Z. 1- Ow2) (Us+)0 . (Ust)or 25 K (Ust)oe Po K 12 Wnz Natural Wh: IK z> Frequency = 75·J2 W Wh Ratio, Dw= 75 Foquency Z J.K. JK put. "dos" (Us+)o value and the of eqO in

Undamped Stoucture

0.005 7 2 25 75-1212 1 -JK k 0.005. 19-19250 25 Z K K 0.005 x 56.25 2 25 r 0.005 z. 56.25 + 25 K K 0.005 z 81.25 K · · · · · · 81.25 KZ 0.005 Kz 36250 M/m K= <u>3 EI</u> 13 > 14 Now 162.50 × (0.5) (3×(7)×109)) J= KxL3 z 38 Jz 9.54 x 20-9 m4 .5 T: T × dy 50 64

3h

d= (7,64) 4 dz ((9.54 + 10-9) × (\$\$)(64)) 3.14 m 160.0 = b dz 0.022 x 1000 de 21 mm



### PROBLEM # 4

A rotating machine with a 600 kg mass operating at a constant speed produces harmonic force in vertical direction. The harmonic force is expressed as p(t)=5000 Sin 150t, where p(t) is in N. If the damping ratio of isolators at the foundation of machine is 7.5%, determine the stiffness of isolators so that the Transmissibility at the operating speed does not exceed 0.15. Also determine the amplitude of force transmitted to the foundation

R: GIVEN DATA Mass, mz 600 Kg Halmonic Foxce, p(E): 5000 × Str. 250+t N Amplitude, Po: 5000 N Force Focquency, We '150 lad /sec

Damping Ratio, Ez 7.5% = 0.075 Transmissibility, TR = 0.15 REQUIRED : Force Toansmitted: Amplitude = (fr) o = ? Stiffness, K = ? SOLUTION:  $\frac{TR = (F_{T})_{0}}{P_{0}} = \frac{1 + (2 \notin \delta \omega)^{2}}{(1 - \delta \omega^{2})^{2} + (2 \times \xi \times \delta \omega)^{2}}$  $\frac{1}{(1-\delta\omega^{2})^{2}+(2\times\xi\times\delta\omega)^{2}}$ (0.15) =  $\frac{1}{(1-\delta\omega^2)^2 + (2\times0.075\times\delta\omega)^2}$ ] + (0.15 × Jw)2 0.0225 z (1-Vw2)2+(0.15 vVw)2 1 + (0.0225 × 8w2) 0.0225 Z (1-Jw2)2 + (0.0225 vow2) put Sw = X 0.0225 2 7 + 0.0225x (1-X)2 + (0.0225x) 1 + 0.0225x 0.0225 1.675.000 z 1+X--1x+0.0225x 0.0225 1+ 0.0205x 2 X2 - 1.9775 + 1

X2- 1.9775x +1 = 1 + 0.0225x 0.0225  $\chi^2 - 1.9775 \chi + 1 = 1 + 0.925 \times \chi$ 0.0225 0.9225 x - 1.9775x + 1 = 44.44 + X x2 - 1.9775x + 1 - 44.44 - X X2- 2.9775x - 43.44 By quadratic formula: X = 8.25 Yen 2 2 8.25 Jow 2 2 18.25 9.87 New 2  $\frac{\omega}{\omega_n}$ Yeu 2 150 2.87 2 NIN 150 1m Z (52.66) \*K 2 600

2731.61 z K 600 K 2 2731.61 × 600 K= 1638966 N/m all the values in . op put 0.15 z (f7)0 5000 (Fi) = 0.15 x 5000 (F7) . = 750 . . • . • .



