

end of the compression stroke if the law for the compression is  $pV^{1.35} = \text{constant}$ .

- (4) Three cubic feet of a gas are expanded in a cylinder which causes the pressure to fall from  $100 \text{ lbf/in}^2$  to  $35 \text{ lbf/in}^2$ . If the expansion follows the law  $pV^{1.1} = \text{constant}$ , Find the final volume of the gas.
- (5) The specific heat of a gas at constant pressure and constant volume are  $0.235$  and  $0.174$  respectively; Find the value of  $\gamma$  for this gas. If  $4 \text{ lbf}$  of this gas are heated from  $60^\circ$  to  $312^\circ \text{F}$ , Find the heat absorb if the heating takes place at (1) constant pressure (2) constant volume.
- (6) The value of  $\gamma$  for a certain gas is  $1.38$  and its specific heat at constant pressure is  $0.25$ . Find the heat given out when  $0.16 \text{ lbf}$  of this gas is cooled at constant volume from  $360^\circ$  to  $20^\circ \text{C}$ .
- (7) Steam occupying a volume of  $1.3 \text{ ft}^3$  is expanded in an engine cylinder from an absolute pressure of  $160 \text{ lbf/in}^2$  to an absolute pressure of  $3 \text{ lbf/in}^2$ . Find the final volume of the steam and the work done on the piston if the

Expansion follows a law  $pV^{1.13} = \text{constant}$ .

⑧ A volume of  $3.5 \text{ ft}^3$  of steam at a pressure of  $85 \text{ lbf/in}^2$  (abs) is expanded hyperbolically to a pressure of  $14.5 \text{ lbf/in}^2$  (abs). Find the work done by steam.

⑨ A Diesel engine has a cylinder diameter of  $12 \text{ in}$  and a stroke of  $18 \text{ in}$ . The compression ratio is  $13.5$ . Pure air at a pressure of  $14.7 \text{ lbf/in}^2$  (~~abs~~) is sucked into the cylinder during the suction stroke and is compressed into the clearance volume during the compression stroke. Find the work done during the compression stroke. If the compression is assumed to be reversible adiabatic.

⑩ Ten cubic feet of air at a pressure of ~~of~~  $40 \text{ lbf/in}^2$  is expanded to a volume of  $25 \text{ ft}^3$ . Find the work done during the expansion of each of the following methods of expansion. (a) constant pressure (b) isothermal (c) Free (d) reversible adiabatic (e) Follows the law  $pV^{1.2} = \text{constant}$  (f) hyperbolic.

P-1.4)

Data:-

$$V_1 = 3 \text{ ft}^3$$

$$P_1 = 100 \text{ lb}_f/\text{in}^2$$

$$P_2 = 35 \text{ lb}_f/\text{in}^2$$

$$V_2 = ?$$

$$P V^{1.1} = \text{const.}$$

Solution:-

As the expansion follows the law:

$$P_1 V_1^{1.1} = P_2 V_2^{1.1}$$

$$V_2 = \left( \frac{P_1}{P_2} \right)^{1/1.1} V_1$$

$$= \left( \frac{100}{35} \right)^{1/1.1} 3$$

$$V_2 = 7.79 \text{ ft}^3$$

P-1.5)

Data:-

$$C_p = 0.235$$

$$C_v = 0.174$$

$$\gamma = ?$$

$$W = 4 \text{ lb}_f$$

$$T_1 = 60^\circ \text{F}$$

$$T_2 = 312^\circ \text{F}$$

$$Q_p = ?$$

$$Q_v = ?$$

Solution:-

$$\text{As } \gamma = \frac{C_p}{C_v}$$

(35)

$$\gamma = \frac{0.235}{0.174}$$

$$\gamma = 1.35$$

As

$$Q_p = W C_p (T_2 - T_1) \\ = 4 * 0.235 (312 - 60)$$

$$Q_p = 236.88 \text{ B.T.U}$$

Similarly;

$$Q_v = W C_v (T_2 - T_1) \\ = 4 * 0.174 (312 - 60)$$

$$Q_v = 175.39 \text{ B.T.U}$$

P-1.6)

Data:-

$$\gamma = 1.38$$

$$C_p = 0.25$$

$$W = 0.16 \text{ lb}$$

$$T_2 = 20^\circ\text{C}$$

$$T_1 = 360^\circ\text{C}$$

$$Q_v = ?$$

Solution:-

$$\text{As } \frac{C_p}{C_v} = \gamma$$

$$C_v = \frac{C_p}{\gamma} = \frac{0.25}{1.38}$$

$$C_v = 0.181$$

(36)

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$$Q_v = W C_v (T_2 - T_1)$$

\* IRFAN MARWAT

$$= 0.16 * 0.181 (20 - 360)$$

SECTION 'B'

$$Q_v = -9.855 \text{ Chu}$$

where:

-ve sign shows that gas is cooled or heat is rejected.

=&gt;

$$Q_v = 9.855 \text{ Chu}$$

P-1.7)

Data:-

$$V_1 = 1.3 \text{ ft}^3$$

$$P_1 = 160 \text{ lb}_f/\text{in}^2$$

$$P_2 = 3 \text{ lb}_f/\text{in}^2$$

$$V_2 = ?$$

Work done = ?

$$P V^{1.13} = \text{Const.}$$

Solution:-

As the expansion follows the law:

$$P_1 V_1^{1.13} = P_2 V_2^{1.13}$$

$$V_2 = V_1 \left( \frac{P_1}{P_2} \right)^{1.13}$$

$$= 1.3 \left( \frac{160}{3} \right)^{1.13}$$

$$V_2 = 43.87 \text{ ft}^3$$

Now work done in this expansion will be:

$$\begin{aligned} \text{Work done} &= \frac{P_1 V_1 - P_2 V_2}{n-1} \\ &= \frac{(160 \times 1.3 - 3 \times 43.8) 144}{1.13 - 1} \end{aligned}$$

$$\text{Work done} = 84585.33 \text{ ft-lbf}$$

P-1.8)

Data:-

$$V_1 = 3.5 \text{ ft}^3$$

$$P_1 = 85 \text{ lbf/in}^2$$

$$P_2 = 14.5 \text{ lbf/in}^2$$

Work done = ?

Solution:-

As the gas is expanded hyperbolically;

So

$$P_1 V_1 = P_2 V_2$$

$$V_2 = \frac{P_1 V_1}{P_2}$$

$$\begin{aligned} &= \frac{85 \times 3.5}{14.5} \\ &= 20.51 \end{aligned}$$

$$V_2 = 20.51 \text{ ft}^3$$

Now

$$\text{Work done} = P_1 V_1 \ln \left( \frac{V_2}{V_1} \right)$$

$$= 85 \times 144 \times 3.5 \ln \left( \frac{20.51}{3.5} \right)$$

$$\text{Work done} = 75762.65 \text{ ft-lbf}$$

Q3

P-1.9)

Data:-

$d = 12 \text{ inch} = 1 \text{ ft}$

Stroke = 18 inch = 1.5 ft

$P_1 = 14.7 \text{ lbf/in}^2$

$\frac{V_1}{V_2} = 13.5$

Work done = ?

Solution:-

As

Clearance Volume =  $V_1 - V_2 = \pi \frac{d^2}{4} \times \text{stroke}$

$V_1 - V_2 = \pi \frac{1}{4} \cdot 1.5$

$V_1 - V_2 = 1.178 \text{ --- (1)}$

Also

$\frac{V_1}{V_2} = 13.5$

$V_1 = 13.5 V_2 \text{ --- (2)}$

putting in eq (1)

$13.5 V_2 - V_2 = 1.178$

$V_2 = 0.0942 \text{ ft}^3$

→ eq (2)

$V_1 = 1.272 \text{ ft}^3$

Now:

$P_1 V_1^\gamma = P_2 V_2^\gamma$

$P_2 = \frac{P_1 V_1^\gamma}{V_2^\gamma}$

$= \frac{14.7 \times 144 \times (1.272)^{1.40}}{(0.0942)^{1.40}}$

~~$P_2 = 2856.38 \text{ lbf/in}^2$~~

$P_2 = 562.24 \text{ lbf/in}^2$

As  
~~Work done =  $\frac{P_1 V_1 - P_2 V_2}{\gamma - 1}$~~

As the process is reversible adiabatic.

$$\text{Work done} = \frac{P_1 V_1 - P_2 V_2}{\gamma - 1}$$

$$= \frac{14.7 \times 1.272 - 569.84 \times 0.0942}{1.4 - 1}$$

$$\text{Work done} = -12335 \text{ ft-lbf}$$

As work is done on the system, hence -ve sign comes:  
 So,

$$\text{Work done} = 12335 \text{ ft-lbf}$$

P-1.10)

Data:-

$$V_1 = 10 \text{ ft}^3$$

$$P_1 = 40 \text{ lb}_f/\text{in}^2 = 40 \times 144 \text{ lb}_f/\text{ft}^2$$

$$V_2 = 2.5 \text{ ft}^3$$

Work done = ?

- (a) Iso baric
- (b) Iso thermal
- (c) Free expansion
- (d) Reversible adiabatic
- (e) Follows the law  $PV^{1.2} = \text{const}$ .
- (f) Hyperbolic



Solutions:

(a) At const. pressure.

$$\begin{aligned} \text{Work done} &= P(V_2 - V_1) \\ &= 40(25 - 10) 144 \end{aligned}$$

$$\text{Work done} = 86400 \text{ ft-lbf}$$

(b) In Iso thermal process:

$$\begin{aligned} \text{Work done} &= P_1 V_1 \ln\left(\frac{V_2}{V_1}\right) \\ &= 40 \times 144 \times 10 \ln\left(\frac{25}{10}\right) \end{aligned}$$

$$\text{Work done} = 52778 \text{ ft-lbf}$$

(c) As in free expansion.

$$\text{Work done} = 0$$

(d) In reversible adiabatic process:

$$P_1 V_1^\gamma = P_2 V_2^\gamma$$

$$P_2 = \left(\frac{V_1}{V_2}\right)^\gamma P_1$$

$$= \left(\frac{10}{25}\right)^{1.4} 40$$

$$P_2 = 11.09 \text{ lbf/in}^2$$

Now

(41)

$$\begin{aligned} \text{Work done} &= \frac{P_1 V_1 - P_2 V_2}{\gamma - 1} \\ &= \frac{(40 \times 10 - 11.09 \times 25) 144}{1.4 - 1} \end{aligned}$$

$$\text{Work done} = 44187 \text{ ft-lbf}$$

(e) As the process follows the law:

$$P_1 V_1^{1.2} = P_2 V_2^{1.2}$$

$$P_2 = \left( \frac{V_1}{V_2} \right)^{1.2} P_1$$

$$= \left( \frac{10}{25} \right)^{1.2} \times 40$$

$$P_2 = 13.32 \text{ lbf/in}^2$$

Now

$$\begin{aligned} \text{Work done} &= \frac{P_1 V_1 - P_2 V_2}{n - 1} \\ &= \frac{(40 \times 10 - 13.32 \times 25) 144}{1.2 - 1} \end{aligned}$$

$$\text{Work done} = 48240 \text{ ft-lbf}$$

(f) As hyperbolic & Isothermal processes are the same.

So

$$\text{Work done} = 52778 \text{ ft-lbf}$$