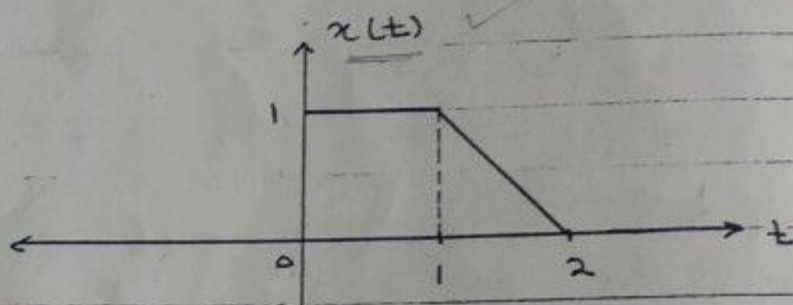


(iv)  $x\left(\frac{3}{2}t + 1\right)$

Solution::

Given that.



(i)  $x(t+1)$

(a) At  $t=0$

$x(t) = 1$

$\Rightarrow$  At  $t+1=0$

$x(t+1) = 1$

$\Rightarrow t = -1$

(b) At  $t=1$

$x(t) = 1$

$\Rightarrow$  At  $t+1=1$

$x(t+1) = 1$

$\Rightarrow t = 0$

(c) At  $t=2$

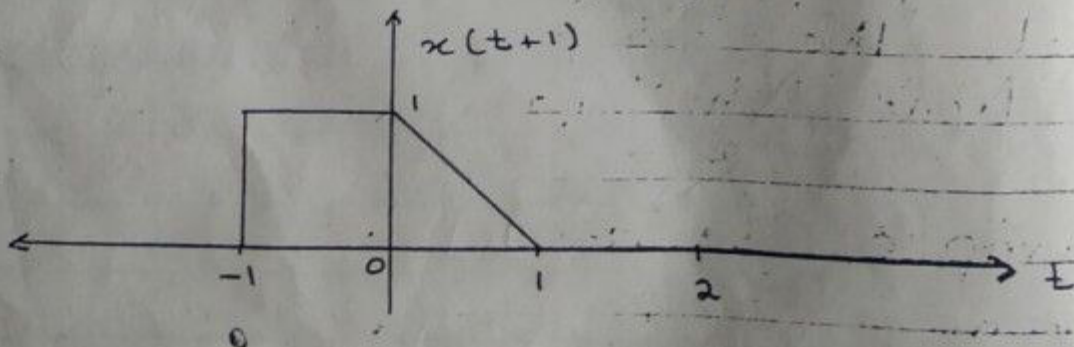
$x(t) = 0$

$\Rightarrow$  At  $t+1=2$

$x(t+1) = 0$

$\Rightarrow t = 1$

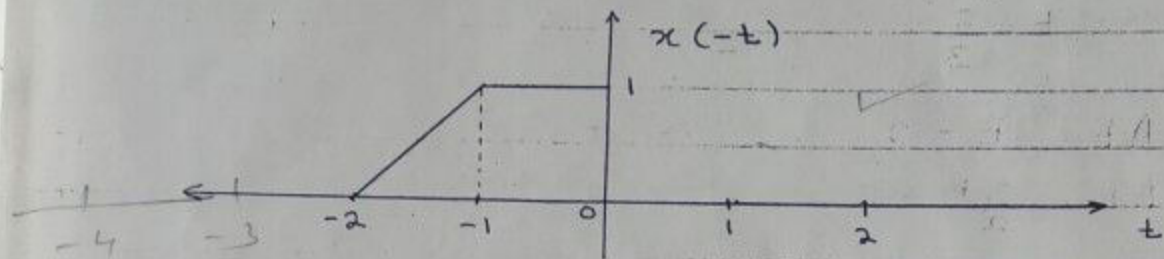
Hence the sketch of  $x(t+1)$  will be:



(iii)  $x(-t+1)$

As there is a -ve sign with the independent variable, hence we must first reflect it & then perform time shift.

First sketching  $x(-t)$  by reflecting  $x(t)$  around  $t=0$



Note:

$$x(-t+1) = x(-(t-1))$$

Hence  $x(-t+1)$  is reflected & time delayed version of  $x(t)$ , (by 1 time unit).

Now, Alternately:

(a) At  $t=0$   $x(t) = 1$

$\Rightarrow$  At  $-t+1=0$   $x(-t+1) = 1$

$\Rightarrow$   $t = 1$

(b) At  $t=+1$   $x(t) = 1$

$\Rightarrow$  At  $-t+1=+1$   $x(-t+1) = 1$

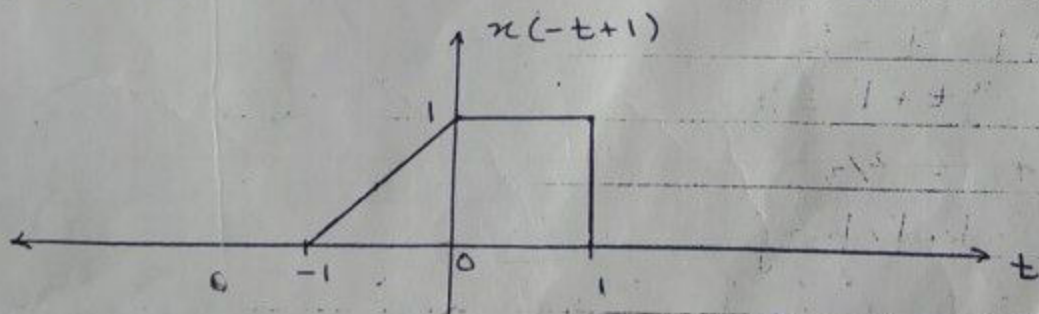
$\Rightarrow$   $t = 0$

(c) At  $t=2$   $x(t) = 0$

$\Rightarrow$  At  $-t+1=2$   $x(-t+1) = 0$

$\Rightarrow$   $t = -1$

Hence sketching according to above calculation.



i)  $x(\frac{3}{2}t)$

Now:

At  $t=0$   $x(t) = 1$

At  $\frac{3}{2}t = 0$   $x(\frac{3}{2}t) = 1$

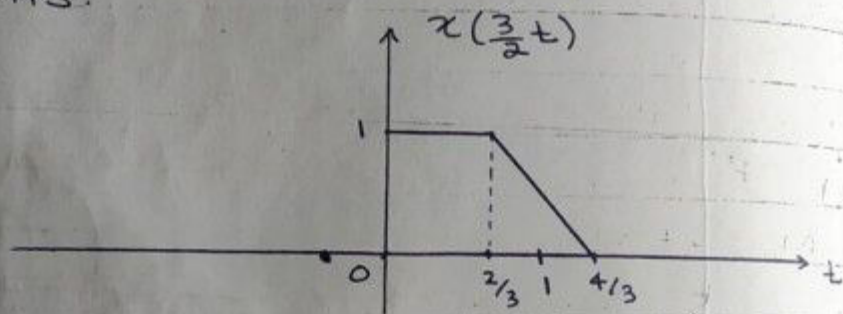
$\Rightarrow$   $t = 0$



(b) At  $t = 1$   $x(t) = 1$   
 $\Rightarrow$  At  $\frac{3}{2}t = 1$   $x(\frac{3}{2}t) = 1$   
 $\Rightarrow t = \frac{2}{3}$

(c) At  $t = 2$   $x(t) = 0$   
 $\Rightarrow$  At  $\frac{3}{2}t = 2$   $x(\frac{3}{2}t) = 0$   
 $\Rightarrow t = \frac{4}{3}$

Hence, sketching according to above calculations:



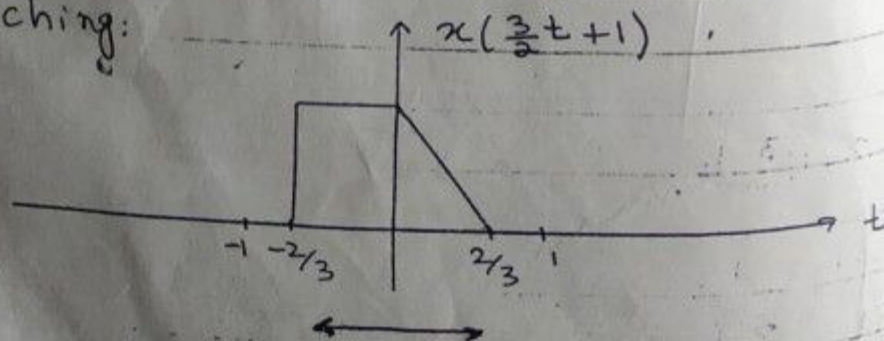
(iv)  $x(\frac{3}{2}t + 1)$

(a) At  $t = 0$   $x(t) = 1$   
 At  $\frac{3}{2}t + 1 = 0$   $x(\frac{3}{2}t + 1) = 1$   
 $\Rightarrow t = -\frac{2}{3}$

(b) At  $t = 1$   $x(t) = 1$   
 At  $\frac{3}{2}t + 1 = 1$   $x(\frac{3}{2}t + 1) = 1$   
 $\Rightarrow t = 0$

(c) At  $t = 2$   $x(t) = 0$   
 At  $\frac{3}{2}t + 1 = 2$   $x(\frac{3}{2}t + 1) = 0$   
 $\Rightarrow t = \frac{2}{3}$

$\therefore$  Sketching:

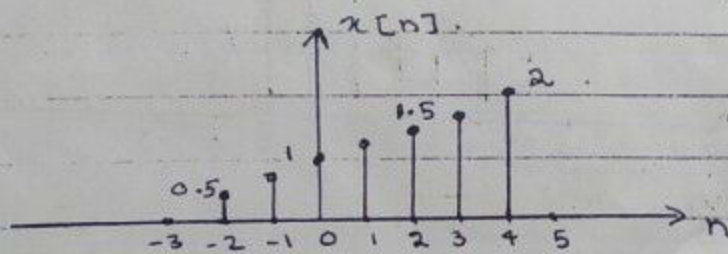


# "Basic Problems"

1.4) Let  $x[n]$  be a signal with  $x[n] = 0$  for  $n < -2$  &  $n > 4$ . For each signal given below, determine the values of "n" for which it is guaranteed to be zero.

Solution:

According to the conditions given, let the signal,  $x[n]$  be given as:



a)  $x[n-3]$  ✓

This signal can be drawn as - ۲۳۱

At,  $n = -2$  ;  $x[n] = 0.5$

At,  $n-3 = -2$  ;  $x[n-3] = 0.5$  (must)

$\Rightarrow n = 0 + 1$

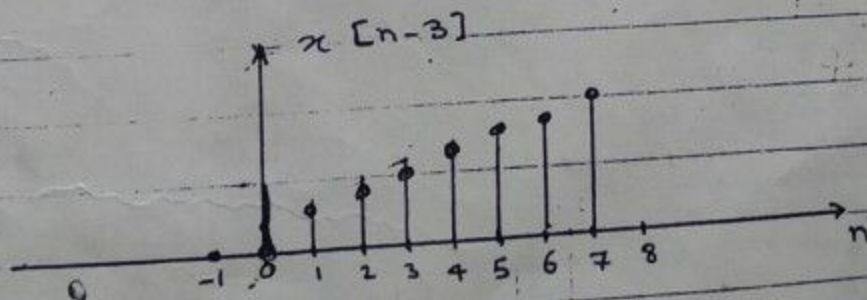
Similarly;

At,  $n = 4$  ;  $x[n] = 2$ .

At,  $n-3 = 4$  ;  $x[n-3] = 2$ .

$\Rightarrow n = 7$ .

$\therefore$



Hence, the value of n is zero for  $n < 1$  &  $n > 7$