

## Lab # 2

### Find Impulse Response, Step Response and Ramp Response Of A Transfer Function

#### Objective:

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#### Step Signal:

A step signal is a signal whose value changes from one level to another level in zero time. Mathematically, the step signal is represented as given below:

$$r(t) = u(t), \text{ where}$$

$$u(t) = 1; t > 0$$

$$= 0; t < 0$$

In the Laplace transform form,

$$R(s) = \frac{1}{s}$$

#### Command Used In Matlab:

- step(num,den)

#### Procedure:

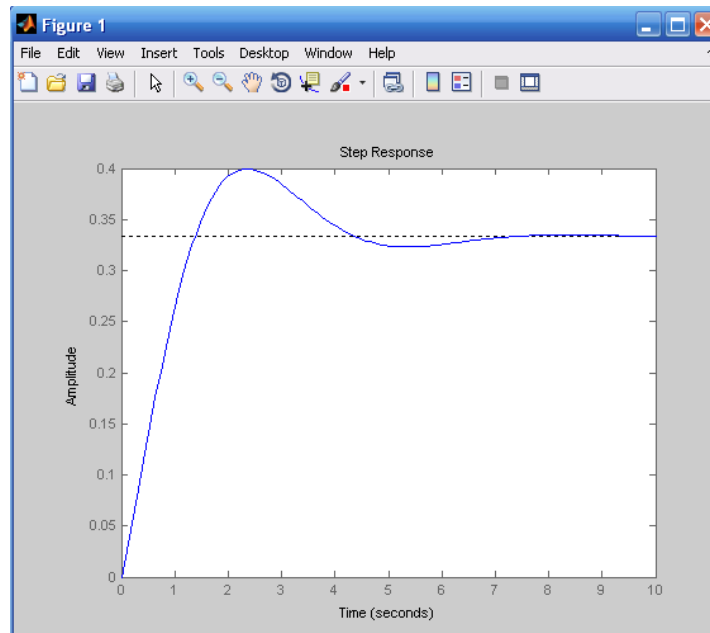
- Type the program in MATLAB editor that is in M-file.
- Give the required inputs in the command window of MATLAB in matrix format.
- 'step' function calculates the unit step response of a linear system.
- Zero initial state is assumed in state-space case.
- This model can be continuous or discrete, and SISO or MIMO.
- The step response of multi-input systems is the collection of step responses for each input channel.
- The duration of simulation is determined automatically based on the system poles and zeroes.

#### Example:

$$\frac{s + 2}{4s^2 + 5s + 6}$$

### Code in Matlab :

```
num=[1 2]
den=[ 4 5 6]
tf(num,den)
step(num,den)
```



### Impulse Response:

An impulse signal is a signal whose value changes from zero to infinity in zero time. Mathematically, the unit impulse signal is represented as given below:

$$r(t) = \delta(t),$$

where:

$$\delta(t) = 1; t = 0$$

$$= 0; t \neq 0$$

In the Laplace transform form,

$$R(s) = 1$$

### Command Used In Matlab:

```
impulse(num,den)
```

### Procedure:

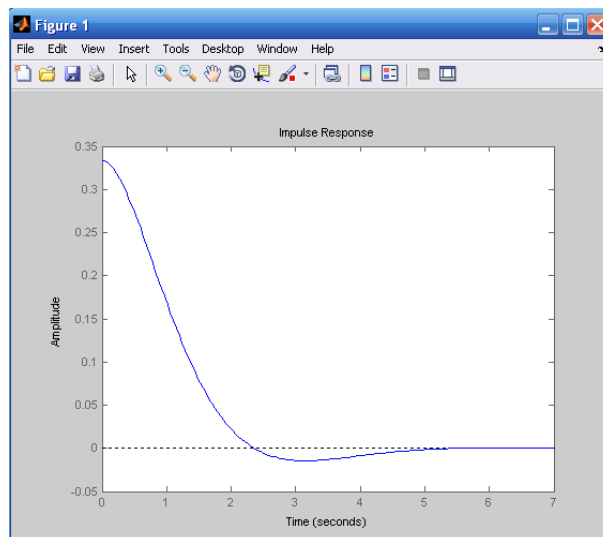
- Type the program in the MATLAB editor that is in M-file.
- Save and run the program.
- Give the required inputs in the command window of MATLAB in matrix format.
- 'impulse' calculates the impulse response of a linear system.
- The impulse response is the response to the Dirac input,  $\delta(t)$  for continuous time systems and to a unit pulse at for discrete time systems.
- Zero initial state is assumed in the state space case.
- This model can be continuous or discrete, SISO or MIMO.
- The impulse response of multi-input systems is the collection of impulse responses for each input channel.
- The duration of simulation is determined automatically to display the transient behavior of the response.
- Note down the response of the given transfer function obtained in MATLAB.
- The response of the transfer function

### Example 2:

$$\frac{s + 2}{3s^2 + 6s + 6}$$

### Code in Matlab :

```
num=[1 2]
den=[3 6 6]
tf(num,den)
impulse(num,den)
```



### Ramp Response:

A ramp signal is a signal which changes with time gradually in a linear fashion. Mathematically, the unit ramp signal is represented as given below:

$$r(t) = t; t > 0$$
$$= 0; t < 0$$

In the Laplace transform form,

$$R(s) = \frac{1}{s^2}$$

### **Command Used In Matlab:**

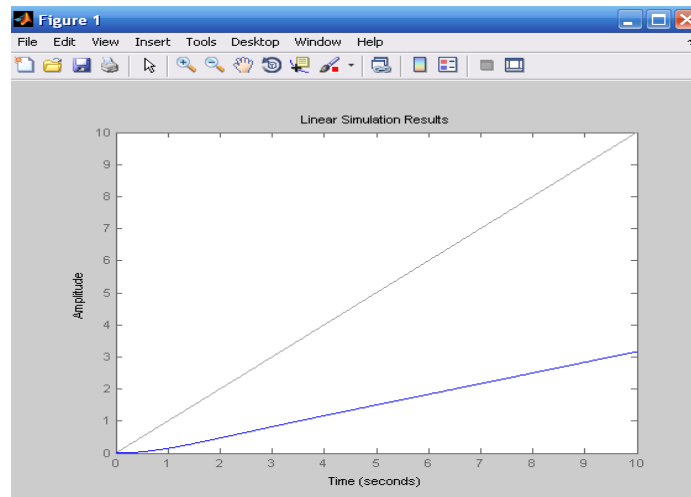
```
t=0:0.01:10;
```

```
u=t;
```

```
num = input('enter the numerator of the transfer function')
```

```
den = input('enter the denominator of the transfer function')
```

```
lsim(num,den,u,t)
```



## Post Lab Questions

a) Fill the following table:

<u>S.No</u>	<u>Name</u>	<u>Definition</u>	<u>Command Used</u>
<u>1</u>	Step Signal		
<u>2</u>	RampSignal		
<u>3</u>	Impulse Signal		
<u>4</u>	Transfer Function		

## Lab Tasks

### Task 1

a) Find the step response and impulse response of the following transfer function:

1.

$$H(s) = \frac{y(s)}{u(s)} = \frac{2}{4s + 1}$$

2.

$$H(s) = \frac{y(s)}{u(s)} = \frac{2s + 3}{s^2 + 4s + 3}$$

### Task 2

Given the following :

Numerator=[2 3]

Denominator=[1 4 3 7]

- i) Find the transfer function
- ii) Find the zeros, poles and gain.
- iii) Find the step response of the signal
- iv) Find the impulse response.

### Task 3

Find the Ramp response of the following:

$$\frac{C(s)}{R(s)} = \frac{s^2 + 4s + 3}{s^3 + 3s^2 + 7s + 5}$$