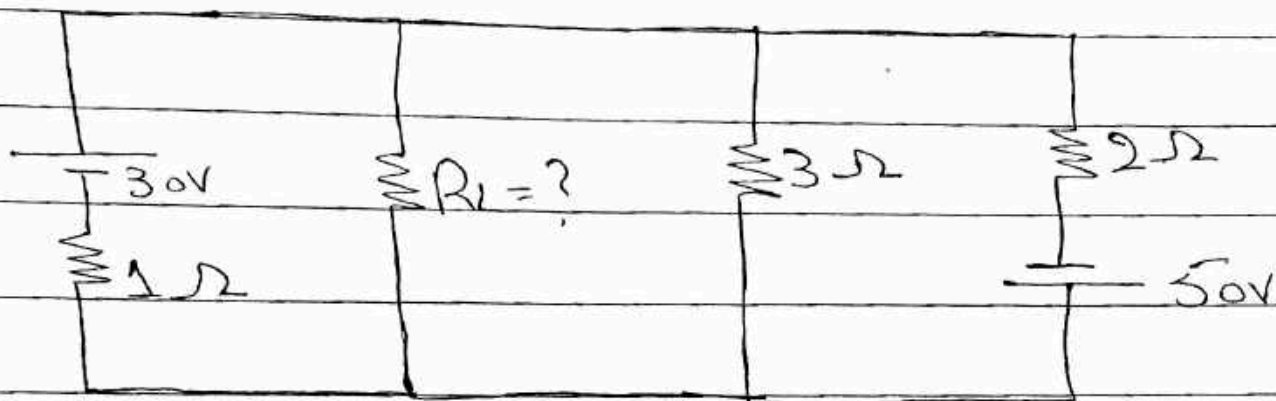
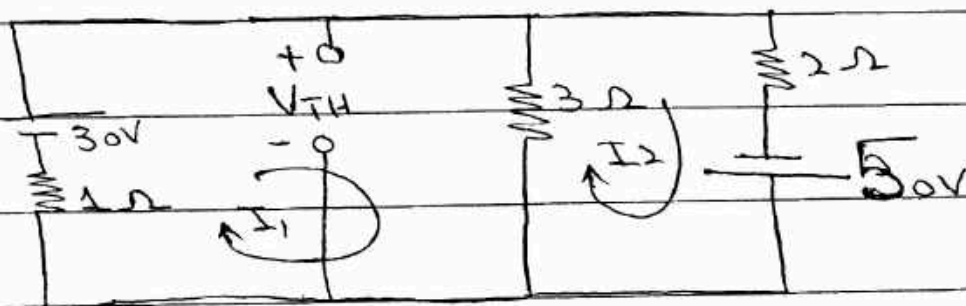


Q:- Find the value of resistance R_L for max power transfer. Also, calculate maximum power.



Step 1:-

remove R_L and replace it by open ckt voltage V_{TH} and find V_{TH} .



$$30 - 3(I_1 - I_2) - 1I_1 = 0 \quad (\text{KVL on loop } \textcircled{1})$$

$$30 - 3I_1 + 3I_2 - I_1 = 0$$

$$-4I_1 + 3I_2 = -30 \quad \text{or} \quad 4I_1 - 3I_2 = 30 \quad \text{--- } \textcircled{1}$$

$$\text{KVL on loop } \textcircled{2} :- -2I_2 + 50 - 3(I_2 - I_1) = 0$$

$$-2I_2 + 50 - 3I_2 + 3I_1 = 0$$

$$3I_1 - 5I_2 = -50$$

$$\text{or} \quad -3I_1 + 5I_2 = 50 \quad \text{--- } \textcircled{2}$$

By solving eq ① & ②

$$\Rightarrow I_1 = 27.27 \text{ A} \quad \& \quad I_2 = 26.36 \text{ A}$$

Now finding V_{TH}

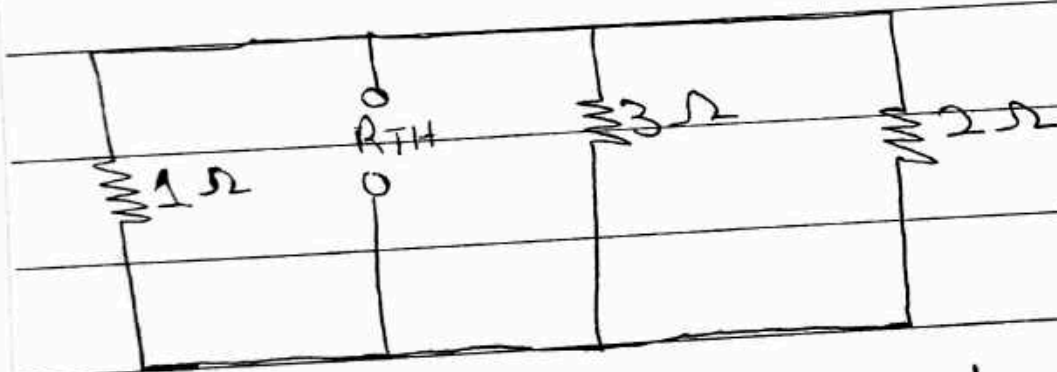
$$30 - V_{TH} - 1 I_1 = 0$$

$$V_{TH} = 30 - 27.27$$

$$V_{TH} = 2.73 \text{ V}$$

Step 2:-

calculating R_{TH} .

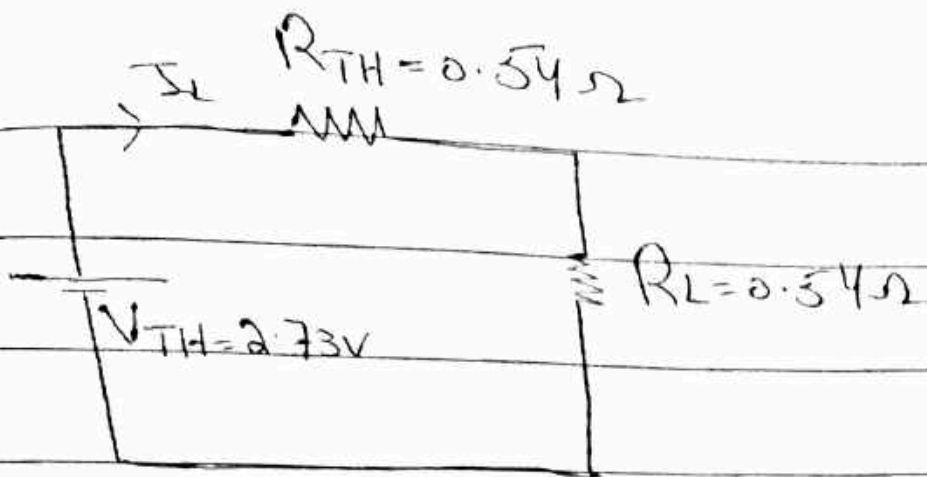


$$\frac{1}{R_{TH}} = \frac{1}{1} + \frac{1}{3} + \frac{1}{2} \Rightarrow \frac{1}{R_{TH}} = \frac{1}{1.833}$$

$$R_{TH} = 0.54 \Omega$$

Step No 3:-

calculating I , E , P_{max} .



$$I_L = \frac{2.73}{2(0.54)}$$

$$I_L = 2.50A$$

$$\begin{aligned} \text{Also } P_{max} &= \frac{V_{TH}^2}{4R_{TH}} \\ &= \frac{(2.73)^2}{4(0.54)} \end{aligned}$$

$$P_{max} = 3.42W \text{ Ans.}$$

Lab No 13

"To analyze a DC Circuit using Millman's Theorem"

Objective:-

The main objective of this lab is to simplify a complex ckt consisting of various voltage sources and find the current through and voltage across a load resistance.

Theory:-

→ Millman's theorem was named after famous electrical engineering professor Jacob Millman.

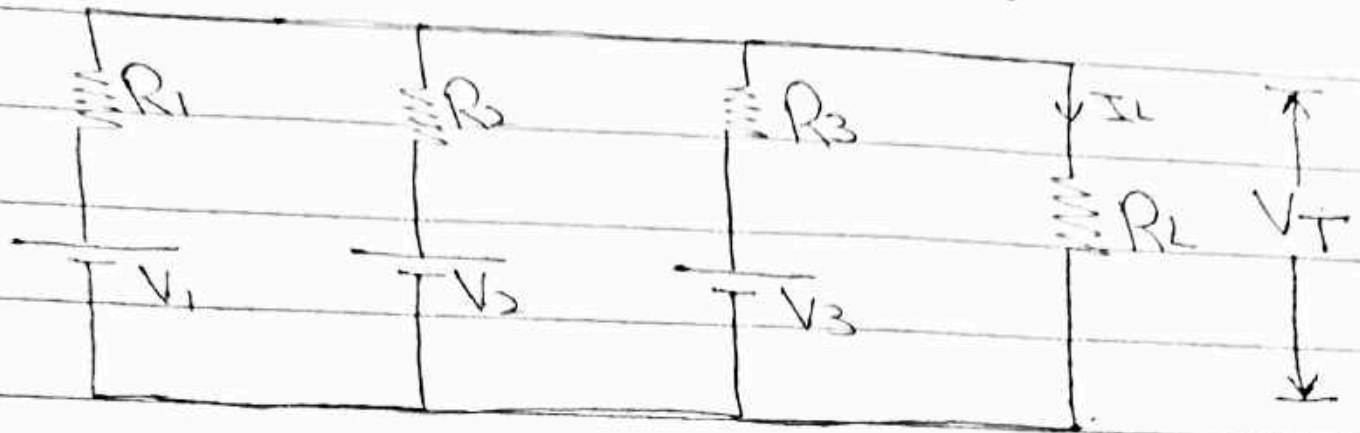
→ This theorem acts as a very strong tool in case of simplifying the special type of complex electrical circuit.

→ This theorem is very useful to find voltage across the load and current through the load resistor.

→ This theorem is also called parallel generator theorem.

→ Millman's theorem is applicable to a ckt which may contain only voltage sources in parallel or a combination of voltage and current sources connected in parallel.

→ In this lab, we will consider a ckt which consists of voltage sources only.



→ Here V_1 , V_2 and V_3 are voltages of respective 1st, 2nd and 3rd branch.

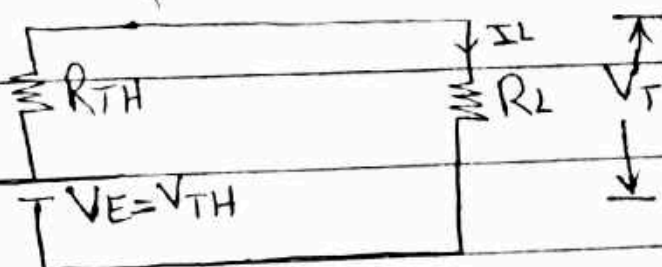
→ R_1 , R_2 and R_3 are the respective resistances of the voltage sources.

→ I_L is the current passing through load resistor (R_L)

→ V_T is the voltage across R_L .

$$E, V_T = I_L \times R_L$$

→ Now this complex ckt can be reduced easily to a single equivalent voltage source with a series resistance with the help of millman's theorem as shown below:-



where V_E is the equivalent voltage

To calculate V_E :

$$V_L = \frac{V_1/R_1 + V_2/R_2 + V_3/R_3}{1/R_1 + 1/R_2 + 1/R_3}$$

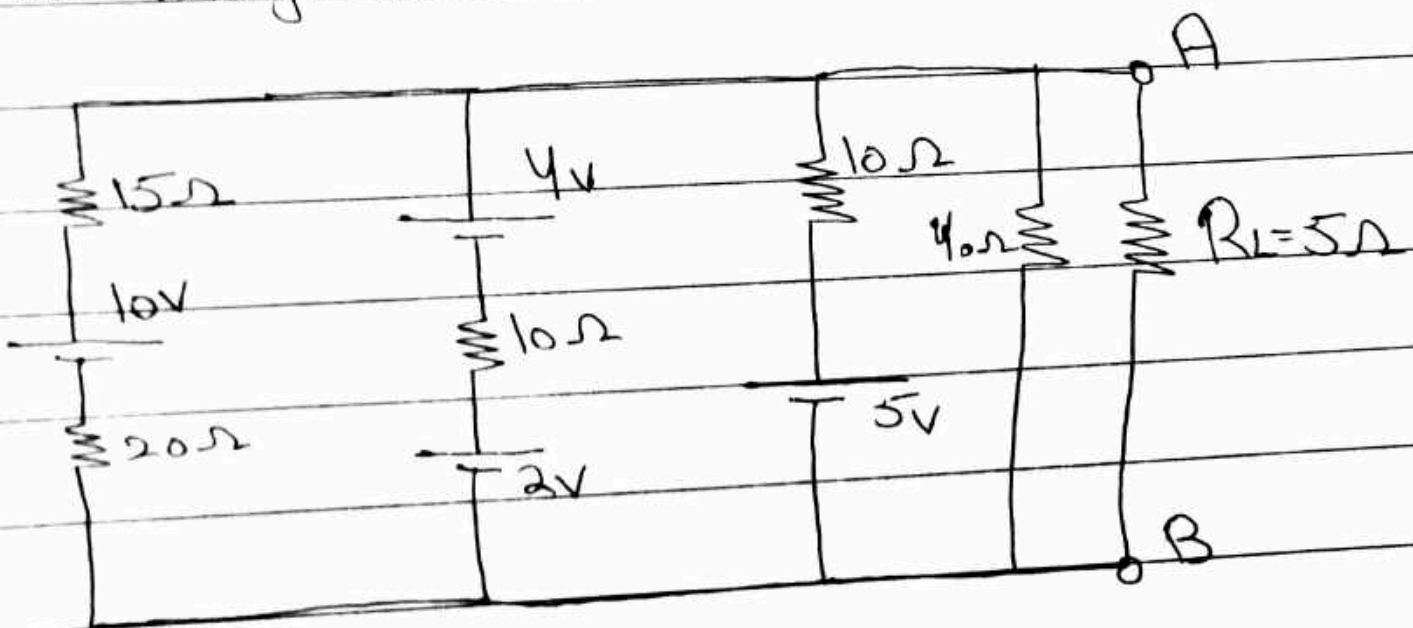
To calculate load current (I_L) and terminal voltage (V_T):

$$I_L = \frac{V_{TH}}{R_L + R_{TH}}$$

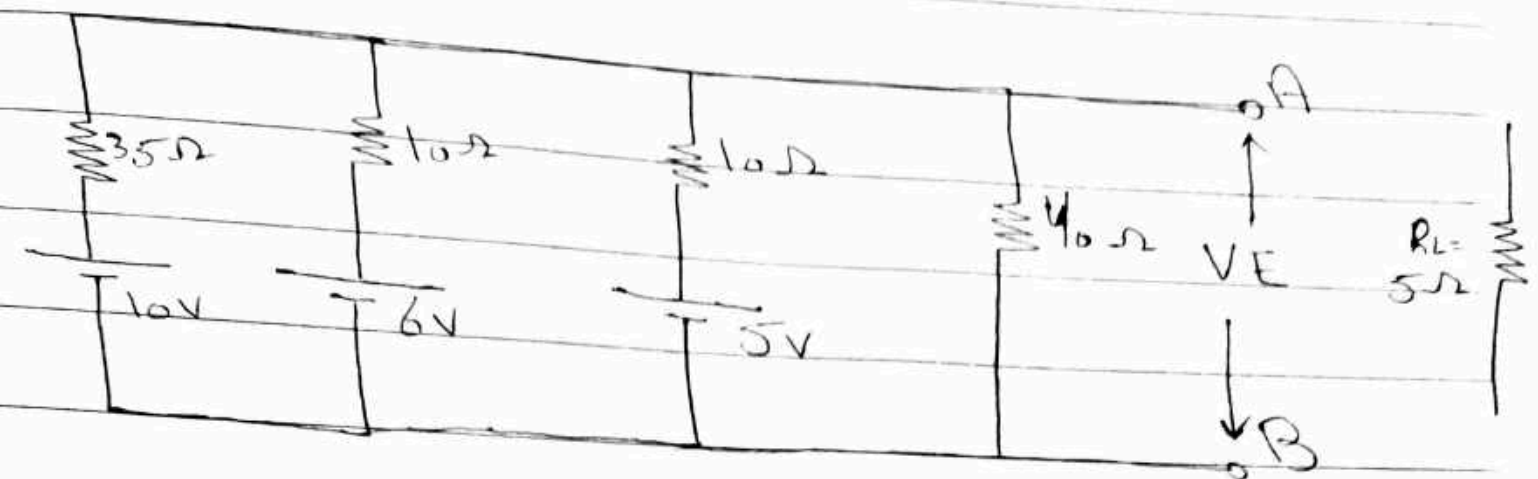
$$E, V_T = I_L \times R_L$$

Circuit Diagram:-

using millman's Theorem, calculate the current through and voltage across 5Ω resistor in the ckt shown below:-



Simplifying the circuit:-



$$V_E = \frac{V_1/R_1 + V_2/R_2 + V_3/R_3 + V_4/R_4}{1/R_1 + 1/R_2 + 1/R_3 + 1/R_4}$$

$$= \frac{10/35 + 6/10 + 5/10 + 0/40}{1/35 + 1/10 + 1/10 + 1/40}$$

$$= \frac{10/35 + 6/10 + 5/10 + 0/40}{1/35 + 1/10 + 1/10 + 1/40}$$

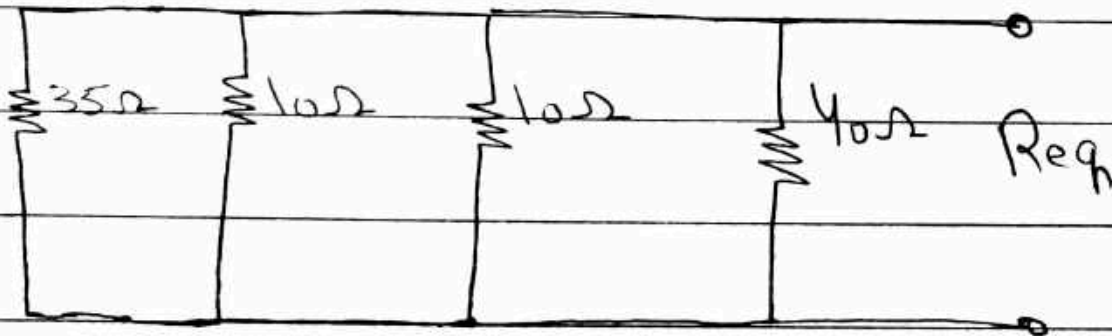
$$= 1.3857$$

$$0.253$$

$$5.48V$$

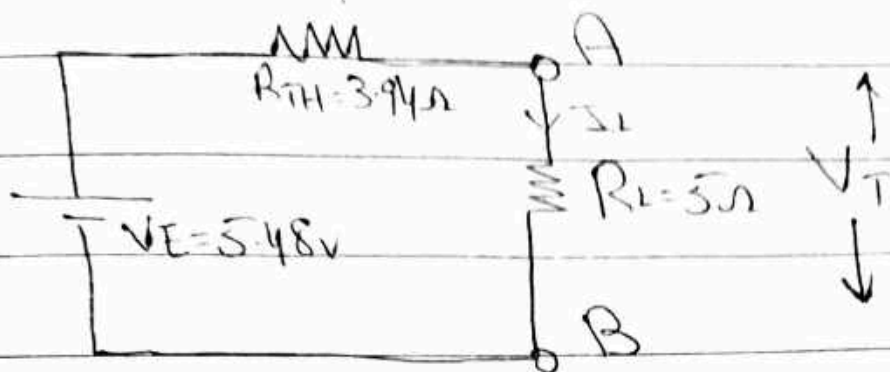
$$\boxed{V_E^{oc} / V_{TH} = 5.48V}$$

Now calculating R_{TH} .



$$\frac{1}{R_{eq}} = \frac{1}{35} + \frac{1}{10} + \frac{1}{10} + \frac{1}{40} \Rightarrow \boxed{R_{eq} = 3.94\Omega}$$

The simplified ckt will be:



$$I_L = \frac{V_E}{R_{TH} + R_L} = \frac{5.48}{3.94 + 5} = \boxed{0.61A}$$

$$\text{also } V_T = I_L \times R_L$$
$$= 0.61 \times 5$$

$$\boxed{V_T = 3.05V}$$