

Q 1: a) Define 2nd order linear homogenous/non-homogenous differential equation along with examples? (2.5+2.5 Marks)

b) Solve the following 2nd order Linear homogeneous /non-homogenous differential equation? (7.5+7.5 Marks)

- i. 4y''-6y'+7y=0
- ii. y''-4y'-12y=3e^(5x)

Q 2: Solve the following IVP for the 2nd order linear equations. (5+5+5+5 Marks)

- (i) 16y''-40y'+25y=0 y(0)=3 y'(0)=-9/4
- (ii) y''+14y'+49y=0 y(-4)=-1y'(-4)=5
- (iii) y''-4y'+9y=0 y(0)=0y'(0)=-8
- (iv) y''-8y'+17y=0 y(0)=-4y'(0)=-1

Q 3: Define Laplace transform along with two examples? (2+3 Marks)

A. Find the Laplace transforms of the given functions. (5+5+5 Marks)

- 1. $f(t) = 6(e^{5}t) + e^{3}t + 5(t^{3}) 9$
- 2. $g(t) = 4\cos(4t) 9\sin(4t) + 2\cos(10t)$
- 3. $h(t) = e^{3t}+cos(6t)-e^{(3t)}cos(6t)$

Q4: Solve the following IVP using Laplace Transform. (10+10 Marks)

- (i) y''-10y'+9y=5t, y(0)=-1, y'(0)=2
- (ii) y''-6y'+15y=2sin(3t), y(0)=-1 y'(0)=-4