Example 1(a): Design slab and beams of a $90^{\prime} \times 60^{\prime}$ Hall. The height of Hall is $20^{\prime}$.
Concrete compressive strength $\left(\mathrm{f}_{\mathrm{c}}{ }^{\prime}\right)=3 \mathrm{ksi}$.
Steel yield strength $\left(f_{y}\right)=40 \mathrm{ksi}$.


Figure 1: $90^{\prime} \times 60^{\prime}$ Hall.

Solution: Assume structural configuration. Take time to reach to a reasonable arrangement of beams, girders and columns. It depends on experience. Several alternatives are possible.

## First option for structural arrangement of the given Hall, figure 2:

- Beams spaced at $10^{\prime} \mathrm{c} / \mathrm{c}$ running along $60^{\prime}$ side of Hall.
- As height of Hall is $20^{\prime}$, assume $18^{\prime \prime}$ thick brick masonry walls.


Figure 2: Structural Arrangement ( $90^{\prime} \times 60^{\prime}$ Hall).

Discussion: Various structural configurations...
Discussion: Beam as thickened slab portions...

## (1) SLAB DESIGN:

## Step No 1: Sizes.

- Minimum thickness of continuous one way slab as given under ACI 9.5.2, table 9.5 (a) is:

| Table 2.1: ACI formulae for continuous one way slab thickness, ACI 9.5.2 |  |
| :---: | :---: |
| Case | Slab thickness (in) |
| End span (one end continuous) | $l / 24$ |
| Interior span (both ends continuous) | $l / 28$ |
| (i) $l=$ Span length in inches. <br> (ii) For $f_{y}$ other than 60,000 <br> $\left(0.4+f_{\sqrt{ }} / 100000\right)$. |  |

Span length " $l$ " of slab is defined in ACI 8.7

## Span length $(l)$ :

- According to ACI 8.7.1: Span length of members not built integrally with support shall be considered as the clear span plus depth of the member, but need not exceed distance between center of supports.
- According to ACI 8.7.4: Span lengths for slabs built integrally with supports can be taken equal to clear span, if clear span of slab is not more than $10^{\prime}$.
- ACI 8.7.1 applies to end span.
- ACI 8.7.4 applies to other spans.

Assuming the thickness of slab equal to $6^{\prime \prime}$. Span length for end span of slab will be equal to clear span plus depth of member (slab), but need not exceed center to center distance between supports.


Figure 3: c/c \& clear spans of slab.

| Table 2.2: Span length of slab (figure 3) |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Case | $\mathrm{c} / \mathrm{c}$ distance | Clear span $\left(l_{\mathrm{n}}\right)$ | $l_{\mathrm{n}}+$ depth of slab <br> (ACI 8.7.1) | Span <br> length $(l)$ |  |
| End span (one end continuous) | $10.75^{\prime}$ | $9.25^{\prime}$ | $9.25+0.5=9.75^{\prime}$ | $9.75^{\prime}$ |  |
| Interior spans (both ends <br> continuous) | $10^{\prime}$ | $8.5^{\prime}$ | $\mathrm{n} / \mathrm{a}$ | $8.5^{\prime}$ |  |


| Table 2.3: Slab thickness calculation according to ACI 9.5.2. |  |  |
| :---: | :---: | :---: |
| Span | Formula for thickness | Thickness of slab (in) |
| End span (one end continuous) | $l / 24 \times\left(0.4+\mathrm{f}_{\mathrm{y}} / 100000\right)$ | $(9.75 / 24) \times(0.4+40000 / 100000) \times 12=3.9^{\prime \prime}$ |
| Interior span (both ends continuous) | $l / 28 \times\left(0.4+\mathrm{f}_{\mathrm{y}} / 100000\right)$ | $(8.5 / 28) \times(0.4+40000 / 100000) \times 12=2.9^{\prime \prime}$ |
| $l=$ Span length in inches. |  |  |

Therefore,
Slab thickness $\left(\mathrm{h}_{\mathrm{f}}\right)=3.9^{\prime \prime}$ (Minimum requirement by ACI 9.5.2.1).
Though any depth of slab greater than $3.9^{\prime \prime}$ can be taken as per ACI minimum requirement, we will use the same depth as assumed i.e. $6^{\prime \prime}$

Effective depth $(\mathrm{d})=\mathrm{h}_{\mathrm{f}}-0.75-(3 / 8) / 2=5^{\prime \prime}$ (for \#3 main bars)


Figure 4: Effective depth of slab.

## Step No 2: Loading.

| Table 2.4: Dead Loads. |  |  |  |
| :---: | :---: | :---: | :---: |
| Material | Thickness (in) | $\gamma(\mathrm{kcf})$ | Load $=\gamma \times$ thickness <br> $(\mathrm{ksf})$ |
| Slab | 6 | 0.15 | $(6 / 12) \times 0.15=0.075$ |
| Mud | 3 | 0.12 | $(3 / 12) \times 0.12=0.03$ |
| Tile | 2 | 0.12 | $(2 / 12) \times 0.12=0.02$ |

Service Dead Load (D.L) $=0.075+0.03+0.02=0.125 \mathrm{ksf}$
Service Live Load (L.L) $=40 \mathrm{psf}$ or 0.04 ksf (for Hall)
Class Activity: Calculate live load per square foot on the class room floor when it is fully occupied.
Service Load $\left(\mathrm{w}_{\mathrm{s}}\right)=$ D.L + L. $\mathrm{L}=0.125+0.04=0.165 \mathrm{ksf}$
Factored Load $\left(w_{u}\right)=1.2$ D.L +1.6 L. L

$$
=1.2 \times 0.125+1.6 \times 0.04=0.214 \mathrm{ksf}
$$

## Step No 3: Analysis.

Our Slab system is:

- One-way,
- Clear spans less than $10^{\prime}$, and
- Exterior ends of slab are discontinuous and unrestrained.

Refer to ACI 8.3.3 or page 396, Nilson $13^{\text {th }}$ Ed, following ACI moment coefficients apply:

19.92 in-k/ft


Figure 5: Bending Moment Diagram for slab.
(i) AT INTERIOR SUPPORT (left side of support):

Negative moment $\left(-\mathrm{M}_{\mathrm{Lint}}\right)=$ Coefficient $\times\left(\mathrm{w}_{\mathrm{u}} l_{\mathrm{n}}{ }^{2}\right)$

$$
\begin{aligned}
& =(1 / 12) \times\left\{0.214 \times(9.25)^{2}\right\} \\
& =1.53 \mathrm{ft}-\mathrm{k} / \mathrm{ft}=18.36 \mathrm{in}-\mathrm{k} / \mathrm{ft}
\end{aligned}
$$

(ii) AT INTERIOR SUPPORT (right side of support):

Negative moment $\left(-\mathrm{M}_{\text {Rint }}\right)=$ Coefficient $\times\left(\mathrm{w}_{\mathrm{u}} l_{\mathrm{n}}{ }^{2}\right)$

$$
\begin{aligned}
& =(1 / 12) \times\left\{0.214 \times(8.5)^{2}\right\} \\
& =1.29 \mathrm{ft}-\mathrm{k} / \mathrm{ft}=15.48 \mathrm{in}-\mathrm{k} / \mathrm{ft}
\end{aligned}
$$

(iii)AT EXTERIOR MID SPAN:

Positive moment $\left(+\mathrm{M}_{\text {Mext }}\right)=$ Coefficient $\times\left(\mathrm{w}_{\mathrm{u}} l_{\mathrm{n}}{ }^{2}\right)$

$$
\begin{aligned}
& =(1 / 11) \times\left\{0.214 \times(9.25)^{2}\right\} \\
& =1.66 \mathrm{ft}-\mathrm{k} / \mathrm{ft}=19.92 \mathrm{in}-\mathrm{k} / \mathrm{ft}
\end{aligned}
$$

(iv)AT INTERIOR MID SPAN:

Positive moment $\left(+\mathrm{M}_{\text {Mint }}\right)=$ Coefficient $\times\left(\mathrm{w}_{\mathrm{u}} l_{\mathrm{n}}{ }^{2}\right)$

$$
\begin{aligned}
& =(1 / 16) \times\left\{0.214 \times(8.5)^{2}\right\} \\
& =0.97 \mathrm{ft}-\mathrm{k} / \mathrm{ft}=11.64 \mathrm{in}-\mathrm{k} / \mathrm{ft}
\end{aligned}
$$

Discussion: ACI analysis vs actual conditions for beam support, concepts of hinge, roller supports etc.

## Step No 4: Design.



Figure 6: Reinforcement Placement in slab.

$$
\begin{aligned}
& \mathrm{A}_{\text {smin }}=0.002 \mathrm{bh}_{\mathrm{f}}\left(\text { for }_{\mathrm{y}} 40 \mathrm{ksi}, \mathrm{ACI} 10.5 .4\right) \\
&=0.002 \times 12 \times 6=0.144 \mathrm{in}^{2} / \mathrm{ft} \\
& \mathrm{a}=\mathrm{A}_{\text {smin }} \mathrm{f}_{\mathrm{y}} /\left(0.85 \mathrm{f}_{\mathrm{c}}{ }^{\prime} \mathrm{b}\right)=0.144 \times 40 /(0.85 \times 3 \times 12)=0.188^{\prime \prime}
\end{aligned}
$$

$$
\begin{aligned}
\Phi \mathrm{M}_{\mathrm{n}} & =\Phi \mathrm{A}_{\text {smin }} \mathrm{f}_{\mathrm{y}}(\mathrm{~d}-\mathrm{a} / 2) \\
& =0.9 \times 0.144 \times 40 \times(5-0.188 / 2)=25.4 \mathrm{in}-\mathrm{k} / \mathrm{ft}
\end{aligned}
$$

$\Phi \mathrm{M}_{\mathrm{n}}$ calculated from $\mathrm{A}_{\text {smin }}$ is greater than all moments as calculated in Step No 3 .
Therefore $\mathrm{A}_{\mathrm{s}}=\mathrm{A}_{\text {smin }}=0.144 \mathrm{in}^{2} / \mathrm{ft}$
Using $1 / 2^{\prime \prime} \Phi(\# 4)\{\# 13,13 \mathrm{~mm}\}$, with bar area $\mathrm{A}_{\mathrm{b}}=0.20 \mathrm{in}^{2}$
Spacing $=$ Area of one bar $\left(\mathrm{A}_{\mathrm{b}}\right) / \mathrm{A}_{\mathrm{s}}$

$$
=\left(0.20 \mathrm{in}^{2} / 0.144 \mathrm{in}^{2} / \mathrm{ft}\right) \times 12=16.67 \mathrm{in}
$$

Discussion: Bar numbers commonly used in slabs...?
Using $3 / 8^{\prime \prime} \Phi(\# 3)\{\# 10,10 \mathrm{~mm}\}$, with bar area $\mathrm{A}_{\mathrm{b}}=0.11 \mathrm{in}^{2}$
Spacing $=$ Area of one bar $\left(\mathrm{A}_{\mathrm{b}}\right) / \mathrm{A}_{\mathrm{s}}$

$$
=\left(0.11 \mathrm{in}^{2} / 0.144 \mathrm{in}^{2} / \mathrm{ft}\right) \times 12=9.16^{\prime \prime} \approx 9^{\prime \prime}
$$

Finally use \#3@ 9" c/c (\#10@ 225 mm c/c). This will work for both Positive and Negative steel as $\mathrm{A}_{\text {smin }}$ governs.
Shrinkage steel or temperature steel $\left(\mathrm{A}_{\mathrm{st}}\right)$ :
$\mathrm{A}_{\mathrm{st}}=0.002 \mathrm{bh}_{\mathrm{f}}$
$\mathrm{A}_{\mathrm{st}}=0.002 \times 12 \times 6=0.144 \mathrm{in}^{2} / \mathrm{ft}$
Shrinkage reinforcement is same as main reinforcement, because:
$\mathrm{A}_{\mathrm{st}}=\mathrm{A}_{\mathrm{smin}}=0.144 \mathrm{in}^{2}$

- Maximum spacing for main steel reinforcement in one way slab according to ACI 7.6.5 is minimum of:
(i) $3 \mathrm{~h}_{\mathrm{f}}=3 \times 6=18^{\prime \prime}$
(ii) $18^{\prime \prime}$

Therefore $9^{\prime \prime}$ spacing is O.K.

- Maximum spacing for temperature steel reinforcement in one way slab according to ACI 7.12.2.2 is minimum of:
(i) $5 \mathrm{~h}_{\mathrm{f}}=5 \times 6=30^{\prime \prime}$
(ii) $18^{\prime \prime}$

Therefore $9^{\prime \prime}$ spacing is O.K.
(2) BEAM DESIGN (single span, simply supported):

## Data Given:

Exterior supports of beam $=18^{\prime \prime}$ brick masonry wall.
$\mathrm{f}_{\mathrm{c}}{ }^{\prime}=3 \mathrm{ksi} ; \mathrm{f}_{\mathrm{y}}=40 \mathrm{ksi}$
Beams $\mathrm{c} / \mathrm{c}$ spacing $=10^{\prime}$

## Step No 1: Sizes.

According to ACI 9.5.2.1, table 9.5 (a):
Minimum thickness of beam (simply supported) $=\mathrm{h}_{\min }=l / 16$
$l=$ clear span $\left(l_{\mathrm{n}}\right)+$ depth of member $($ beam $) \leq \mathrm{c} / \mathrm{c}$ distance between supports
[ACI 8.7]


Figure 7: Clear span of Beam.


Figure 8: Beam cross-section.

Let depth of beam $=5^{\prime}$
$l_{n}+$ depth of beam $=60^{\prime}+5^{\prime}=65^{\prime}$
$\mathrm{c} / \mathrm{c}$ distance between beam supports $=60+2 \times(9 / 12)=61.5^{\prime}$
Therefore $l=61.5^{\prime}$
Depth $(\mathrm{h})=(61.5 / 16) \times\left(0.4+\mathrm{f}_{\mathrm{y}} / 100000\right) \times 12$
$=36.9^{\prime \prime}$ (Minimum requirement by ACI 9.5.2.1).
Though any depth of beam greater than $36.9^{\prime \prime}$ can be taken as per ACI minimum requirement, we will use the same depth as assumed i.e. $60^{\prime \prime}$

Take $\mathrm{h}=5^{\prime}=60^{\prime \prime}$
$\mathrm{d}=\mathrm{h}-3=57^{\prime \prime}$

## Step No 2: Loads.

Service Dead Load (D.L) $=0.075+0.03+0.02=0.125 \mathrm{ksf}($ Table 2.3 $)$
Service Live Load (L.L) $=40 \mathrm{psf}$ or 0.04 ksf (for Hall)
Beam is supporting 10 ' slab. Therefore load per running foot will be as follows:
Service Dead Load from slab $=0.125 \times 10=1.25 \mathrm{k} / \mathrm{ft}$
Service Dead Load from beam's self weight $=h_{w} b_{w} \gamma_{c}$

$$
=(54 \times 18 / 144) \times 0.15=1.0125 \mathrm{k} / \mathrm{ft}
$$

Total Service Dead Load $=1.25+1.0125=2.2625 \mathrm{k} / \mathrm{ft}$
Service Live Load $=0.04 \times 10=0.4 \mathrm{k} / \mathrm{ft}$
$\mathrm{w}_{\mathrm{s}}=$ D.L $+\mathrm{L} . \mathrm{L}=1.0125+0.4=1.4125 \mathrm{k} / \mathrm{ft}$
$\mathrm{w}_{\mathrm{u}}=1.2 \mathrm{D} \cdot \mathrm{L}+1.6 \mathrm{~L} . \mathrm{L}=1.2 \times 2.2625+1.6 \times 0.4=3.355 \mathrm{k} / \mathrm{ft}$

## Step No 3: Analysis.



Figure 9: Shear Force \& Bending Moment Diagrams.

$$
\begin{aligned}
& \mathrm{M}_{\mathrm{u}}=\mathrm{w}_{\mathrm{u}} \mathrm{l}^{2} / 8 \quad(\mathrm{l}=\text { span length of beam }) \\
& \mathrm{M}_{\mathrm{u}}=3.355 \times 61.5^{2} / 8=1586.18 \mathrm{ft}-\mathrm{k}=1586.18 \times 12=19034 \mathrm{in}-\mathrm{k} \\
& \mathrm{~d}=57^{\prime \prime}=4.75^{\prime} \\
& \mathrm{V}_{\max }=103.16 \mathrm{k} \\
& \mathrm{~V}_{\mathrm{u}}=84.70 \mathrm{k}
\end{aligned}
$$

## Step No 4: Design of beam.

(A)Flexural Design:

Step (a): According to ACI 8.10, $\mathrm{b}_{\text {eff }}$ for T-beam is minimum of:
(i) $16 h_{f}+b_{w}=16 \times 6+18=114^{\prime \prime}$
(ii) $\left(\mathrm{c} / \mathrm{c}\right.$ span of beam) $/ 4=\left(61.5^{\prime} / 4\right) \times 12=184.5^{\prime \prime}$
(iii)c/c spacing between beams $=10^{\prime} \times 12=120^{\prime \prime}$

$$
\text { So } b_{\text {eff }}=114^{\prime \prime}
$$

Step (b): Check if beam is to be designed as rectangular beam or T-beam.
Trial \#1:
(i) Assume $\mathrm{a}=\mathrm{h}_{\mathrm{f}}=6^{\prime \prime}$

$$
\begin{aligned}
& \mathrm{A}_{\mathrm{s}}=\mathrm{M}_{\mathrm{u}} /\left\{\Phi \mathrm{f}_{\mathrm{y}}(\mathrm{~d}-\mathrm{a} / 2)\right\} \\
& \mathrm{A}_{\mathrm{s}}=19034 /\{0.9 \times 40 \times(57-6 / 2)\}=9.79 \mathrm{in}^{2}
\end{aligned}
$$

(ii) Re-calculate " a ":

$$
\begin{aligned}
& \mathrm{a}=\mathrm{A}_{\mathrm{s}} \mathrm{f}_{\mathrm{y}} /\left(0.85 \mathrm{f}_{\mathrm{c}}{ }^{\prime} \mathrm{b}_{\mathrm{eff}}\right) \\
& \mathrm{a}=9.79 \times 40 /(0.85 \times 3 \times 114)=1.34^{\prime \prime}<\mathrm{h}_{\mathrm{f}}
\end{aligned}
$$

Therefore design beam as rectangular beam.
Trial \#2:

$$
\begin{aligned}
& \mathrm{A}_{\mathrm{s}}=19034 /\{0.9 \times 40 \times(57-1.34 / 2)\}=9.38 \mathrm{in}^{2} \\
& \mathrm{a}=9.38 \times 40 /(0.85 \times 3 \times 114)=1.29^{\prime \prime}
\end{aligned}
$$

This value is close enough to the previously calculated value of " $a$ ", therefore, $\mathrm{A}_{\mathrm{s}}=9.38 \mathrm{in}^{2}$, O.K.

Step (c): Check for maximum and minimum reinforcement.

$$
\begin{aligned}
& \mathrm{A}_{\mathrm{smax}}=\rho_{\max } \mathrm{b}_{\mathrm{w}} \mathrm{~d} \\
& \rho_{\max }=0.85 \beta_{1}\left(\mathrm{f}_{\mathrm{c}}^{\prime} / \mathrm{f}_{\mathrm{y}}\right)\left\{\varepsilon_{\mathrm{u}} /\left(\varepsilon_{\mathrm{u}}+\varepsilon_{\mathrm{y}}\right)\right\} \\
& \rho_{\max }=0.85 \times 0.85 \times(3 / 40) \times\{0.003 /(0.003+0.005)\}=0.0203
\end{aligned}
$$

$\mathrm{A}_{\text {smax }}=0.0203 \times 18 \times 57=20.83 \mathrm{in}^{2}$
$\mathrm{A}_{\text {smin }}=\rho_{\text {min }} \mathrm{b}_{\mathrm{w}} \mathrm{d}=(200 / 40000) \times 18 \times 57=5.13 \mathrm{in}^{2}$
$\mathrm{A}_{\text {smin }}<\mathrm{A}_{\mathrm{s}}<\mathrm{A}_{\text {smax }}$, O.K.
Note that $\rho_{\min } \& \rho_{\max }$ can also be found using table A.4, Nelson $13^{\text {th }}$ Ed.

Beam (main reinforcement):
$\mathrm{A}_{\mathrm{s}}=9.38 \mathrm{in}^{2}$
Using \#8, $1^{\prime \prime} \Phi\{\# 25,25 \mathrm{~mm}\}$, with bar area $\mathrm{A}_{\mathrm{b}}=0.79 \mathrm{in}^{2}$
No. of bars $=\mathrm{A}_{\mathrm{s}} / \mathrm{A}_{\mathrm{b}}=9.38 / 0.79=11.87 \approx 12$ bars
Use 12 \#8 bars ( $12 \# 25$ bars, 25 mm ).
4 Check the capacity of designed beam:
Area of $12 \# 8$ Bars $=12 \times 0.79=9.48$ in $^{2}$
$\mathrm{a}=\mathrm{A}_{\mathrm{s}} \mathrm{f}_{\mathrm{y}} /\left(0.85 \mathrm{f}_{\mathrm{c}}{ }^{\prime} \mathrm{b}_{\text {eff }}\right)=9.48 \times 40 /(0.85 \times 3 \times 114)=1.30^{\prime \prime}$
$\mathrm{d}^{\prime}=1.5+(3 / 8)+1+(1 / 2)=3.375^{\prime \prime}$
$\mathrm{d}=\mathrm{h}-\mathrm{d}^{\prime}=60-3.375=56.625^{\prime \prime}$


Figure 10: Beam section dimensions.
$\mathrm{M}_{\mathrm{d}}=\Phi \mathrm{A}_{\mathrm{s}} \mathrm{f}_{\mathrm{y}}(\mathrm{d}-\mathrm{a} / 2)=0.9 \times 9.48 \times 40 \times(56.625-1.30 / 2)=19103.2 \mathrm{in}-\mathrm{k}$ $M_{d}>\left(M_{u}=19034\right.$ in-k), O.K.

## Skin Reinforcement:

According to ACI 10.6.7 "If the effective depth $\boldsymbol{d}$ of a beam or joist exceeds 36 in., longitudinal skin reinforcement shall be uniformly distributed along both side faces of the member for a distance $\boldsymbol{d} / \mathbf{2}$ nearest the flexural tension reinforcement. The spacing $\boldsymbol{s}_{\boldsymbol{s} \boldsymbol{k}}$ between longitudinal
bars or wires of the skin reinforcement shall not exceed the least of $\boldsymbol{d} / 6,12$ in., and $1000 A_{b} /(d-30)$. It shall be permitted to include such reinforcement in strength computations if a strain compatibility analysis is made to determine stress in the individual bars or wires. The total area of longitudinal skin reinforcement in both faces need not exceed one-half of the required flexural tensile reinforcement".

Reinforcement in tension, negative bending


Figure 11: Skin reinforcement for beams and joists with $\mathrm{d}>36$ inches.

Maximum area of skin reinforcement allowed by ACI:
$\mathrm{A}_{\text {skin, } \max }=$ Main flexural reinforcement $/ 2=9.38 / 2=4.69 \mathrm{in}^{2}$
Range up to which skin reinforcement is provided:
$\mathrm{d} / 2=56.625 / 2=28.3125^{\prime \prime}$
For \#6 bar used in skin reinforcement,
$\mathrm{s}_{\text {sk }}$ is least of:

- $\mathrm{d} / 6=56.625 / 6=9.44^{\prime \prime}$
- $12^{\prime \prime}$
- $1000 A_{b} /(d-30)=1000 \times 0.44 /(56.625-30)=16.53^{\prime \prime}$

Therefore $\mathrm{s}_{\text {sk }}=9.44^{\prime \prime} \approx 9^{\prime \prime}$
With this spacing, 3 bars on each face are required. And for \#6 bar, the total area of skin reinforcement is:
$\mathrm{A}_{\text {skin }}=6 \times 0.44=2.64 \mathrm{in}^{2}<\mathrm{A}_{\text {skin, } \max }=4.69 \mathrm{in}^{2}$, O.K
(B) Shear Design:
$\mathrm{V}_{\mathrm{u}}=84.71 \mathrm{k}$
$\Phi V_{c}=\Phi 2 \sqrt{ }\left(\mathrm{f}_{\mathrm{c}}{ }^{\prime}\right) \mathrm{b}_{\mathrm{w}} \mathrm{d}=(0.75 \times 2 \times \sqrt{ }(3000) \times 18 \times 57) / 1000=84.29 \mathrm{k}$
$\Phi \mathrm{V}_{\mathrm{c}}<\mathrm{V}_{\mathrm{u}}$ \{Shear reinforcement is required\}
$\mathrm{s}_{\mathrm{d}}=\Phi \mathrm{A}_{\mathrm{v}} \mathrm{f}_{\mathrm{y}} \mathrm{d} /\left(\mathrm{V}_{\mathrm{u}}-\Phi \mathrm{V}_{\mathrm{c}}\right)$
Using \#3, 2 legged stirrups with $\left.\mathrm{A}_{\mathrm{v}}=0.11 \times 2=0.22 \mathrm{in}^{2}\right\}$
$\mathrm{s}_{\mathrm{d}}=0.75 \times 0.22 \times 40 \times 57 /(84.71-84.29)=895^{\prime \prime}$
Maximum spacing and minimum reinforcement requirement as permitted by ACI 11.5.4 and 11.5.5.3 shall be minimum of:
(i) $\mathrm{A}_{\mathrm{v}} \mathrm{f}_{\mathrm{y}} /\left(50 \mathrm{~b}_{\mathrm{w}}\right)=0.22 \times 40000 /(50 \times 18) \approx 9.5^{\prime \prime}$
(ii) $\mathrm{d} / 2=57 / 2=28.5^{\prime \prime}$
(iii) $24^{\prime \prime}$
(iv) $\mathrm{A}_{\mathrm{v}} \mathrm{f}_{\mathrm{y}} / 0.75 \sqrt{ }\left(\mathrm{f}_{\mathrm{c}}{ }^{\prime}\right) \mathrm{b}_{\mathrm{w}}=0.22 \times 40000 /\left\{(0.75 \times \sqrt{ }(3000) \times 18\}=11.90^{\prime \prime}\right.$

Other checks:
(a) Check for depth of beam:

$$
\begin{aligned}
& \Phi \mathrm{V}_{\mathrm{s}} \leq \Phi 8 \sqrt{ }\left(\mathrm{f}_{\mathrm{c}}{ }^{\prime}\right) \mathrm{b}_{\mathrm{w}} \mathrm{~d}(\text { ACI 11.5.6.9) } \\
& \Phi 8 \sqrt{ }\left(\mathrm{f}_{\mathrm{c}}{ }^{\prime}\right) \mathrm{b}_{\mathrm{w}} \mathrm{~d}=0.75 \times 8 \times \sqrt{ }(3000) \times 18 \times 57 / 1000=337.18 \mathrm{k} \\
& \Phi \mathrm{~V}_{\mathrm{s}}=\left(\Phi \mathrm{A}_{\mathrm{v}} \mathrm{f}_{\mathrm{y}} \mathrm{~d}\right) / \mathrm{s}_{\mathrm{d}} \\
& =(0.75 \times 0.22 \times 40 \times 57) / 9.5=39.6 \mathrm{k}<337.18 \mathrm{k}, \text { O.K. }
\end{aligned}
$$

So depth is O.K. If not, increase depth of beam.
(b) Check if " $\Phi V_{s} \leq \Phi 4 \sqrt{ }\left(f_{c}{ }_{c}\right) b_{w} d$ " $\{$ ACI 11.5.4.3 $\}$ :

If " $\Phi V_{s} \leq \Phi 4 \sqrt{ }\left(\mathrm{f}_{\mathrm{c}}\right) \mathrm{b}_{\mathrm{w}} \mathrm{d}$ ", the maximum spacing ( $\mathrm{s}_{\max }$ ) is O.K.
Otherwise reduce spacing by one half.

$$
\begin{aligned}
& \Phi 4 \sqrt{ }\left(\mathrm{f}_{\mathrm{c}}{ }^{\prime}\right) \mathrm{b}_{\mathrm{w}} \mathrm{~d}=0.75 \times 4 \times \sqrt{ }(3000) \times 18 \times 57 / 1000=168.58 \mathrm{k} \\
& \Phi \mathrm{~V}_{\mathrm{s}}=\left(\Phi \mathrm{A}_{\mathrm{v}} \mathrm{f}_{\mathrm{y}} \mathrm{~d}\right) / \mathrm{s}_{\mathrm{d}} \\
& \quad=(0.75 \times 0.22 \times 40 \times 57) / 9.5=39.6 \mathrm{k}<168.58 \mathrm{k}, O . \mathrm{K} .
\end{aligned}
$$

Arrangement of stirrups in the beam: With \#3, 2 legged vertical stirrups @ 9.5" c/c (maximum spacing and minimum reinforcement requirement as permitted by ACI), the shear capacity $\left(\Phi \mathrm{V}_{\mathrm{n}}\right)$ of the beam will be equal to:
$\Phi \mathrm{V}_{\mathrm{n}}=\Phi \mathrm{V}_{\mathrm{c}}+\Phi \mathrm{V}_{\mathrm{s}}$
$\Phi \mathrm{V}_{\mathrm{s}}=\left(\Phi \mathrm{A}_{\mathrm{v}} \mathrm{f}_{\mathrm{y}} \mathrm{d}\right) / \mathrm{s}_{\text {max }}$
$\Phi \mathrm{V}_{\mathrm{s}}=(0.75 \times 0.22 \times 40 \times 57 / 9.5)=39.6 \mathrm{k}$
Therefore $\Phi \mathrm{V}_{\mathrm{n}}=84.29+39.6=123.89 \mathrm{k}>\left(\mathrm{V}_{\mathrm{u}}=87.22 \mathrm{k}\right)$
It means that theoretically, from a section at a distance equal to $\mathrm{s} / 2 \mathrm{up}$ to a section where shear is equal to $\Phi \mathrm{V}_{\mathrm{c}} / 2, \# 3,2$ legged vertical stirrups @ $9.5^{\prime \prime} \mathrm{c} / \mathrm{c}$ shall be provided. Beyond the value of $\Phi \mathrm{V}_{\mathrm{c}} / 2$, no shear reinforcement is theoretically required. However \# 3, 2 legged vertical stirrups @ $12^{\prime \prime} \mathrm{c} / \mathrm{c}$ are recommended to hold the flexural reinforcement bars.


Figure 12: Stirrups arrangement.

## (3) DRAFTING:

(I) Slab (S1 and S2):


| Panel | Depth (in) | Mark | Bottom <br> Reinforcement | Mark | Top reinforcement |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| S1 | $6 \prime$ | M1 | $3 / 8^{\prime \prime} \phi @ 9 " \mathrm{c} / \mathrm{c}$ | MT1 | $3 / 8^{\prime \prime} \phi @ 9 " \mathrm{c} / \mathrm{c}$ | Non continuous End |
| S2 | $6^{\prime \prime}$ | M1 | $3 / 8^{\prime \prime} \phi @ 9 " \mathrm{c} / \mathrm{c}$ | MT1 | $3 / 8^{\prime \prime} \phi @ 9 " \mathrm{c} / \mathrm{c}$ | Continuous End |



Section A-A. Refer to figure 5.15, chapter 5, Nelson $13^{\text {th }}$ Ed for bar cutoff.

(a) Use graph A2 to find location of points where bars can be bent up or cutoff for simply supported beams uniformly loaded.
(b) Approximate locations of points where bars can be bent up or cotoff for continuous beams uniformly loaded and built integrally with their supports according to the coefficients in ACI code.


## Appendix A

## Comparison of ACI coefficients analysis with analysis of SAP2000 (finite element

 method based software): Assumptions made in SAP model are,a. Brick masonry walls are modeled as hinged support.
b. Slab is modeled as shell element.
c. Beams are modeled as frame elements.


Figure 13: Plan view of hall showing variation in slab moment (kip-in/in). Marked points show the locations picked for comparison purpose.

| Table 2.5: Slab moments |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: |
|  | ACI 318-02 <br> (kip-in/in) | See figure <br> 9 | SAP Results <br> $(\mathrm{k}-\mathrm{in} / \mathrm{in})$ | Percentage Difference |
| $\mathrm{M}_{\text {(at wall) }}$ | 0 | $\mathrm{M}_{\mathrm{I}}$ | 0.02 | - |
| $\mathrm{M}_{\text {(at ext. mid span) }}$ |  | $\mathrm{M}_{\mathrm{F}}$ | 4.59 | 64 |
|  |  |  | $\mathrm{M}_{\mathrm{G}}$ | 3.40 |
|  |  | $\mathrm{M}_{\mathrm{H}}$ | 1.55 | 51 |
|  |  | $\mathrm{M}_{\mathrm{B}}$ | 1.47 | -7 |
|  |  | $\mathrm{M}_{\mathrm{C}}$ | 1.48 | -4 |
|  |  | $\mathrm{M}_{\mathrm{E}}$ | 0.617 | -4 |
|  | 0.97 | $\mathrm{M}_{\mathrm{A}}$ | 1.04 | -60 |
|  |  | $\mathrm{M}_{\mathrm{D}}$ | 1.2 | 7 |


| Table 2.6: Simply supported beam moment. |  |  |  |
| :--- | :---: | :---: | :---: |
|  | ACI 318-02 | SAP Results | Percentage Difference |
| $\mathrm{M}_{\text {,mid span }}(\mathrm{k}-\mathrm{in})$ | 19034 | 18987.253 | 0.25 |

## Conclusions:

- There is more variation between SAP and ACI in slab moments.
- Less variation in beam moment.


## Appendix B

## Relevant Pictures



Figure 14: Supporting chairs for slab reinforcement.


Figure 15: Reinforcement in slab.


Figure 16: Flexure and shear reinforcement in a beam.


Figure 16: Local arrangement for bar bending.

## Appendix C

## Minimum uniformly distributed live load:

Representative values of minimum live loads to be used in a wide variety of buildings are found in Minimum Design Loads for Buildings and Other Structures, SEI/ASCE 7-02, American Society of Civil Engineers, a portion of which is reproduced in table C1. The table gives uniformly distributed live loads for various types of occupancies; these include impact provisions where necessary. These loads are expected maxima and considerably exceed average values.

| Table C1: Minimum uniformly distributed live loads. |  |  |  |
| :---: | :---: | :---: | :---: |
| Occupancy or Use | Live Load, psf |  | Live Load, psf |
| Apartments (see residential) |  | Dining rooms and restaurants | 100 |
| Access floor systems |  | Dwellings (see residential) |  |
| Office use | 50 | Fire escapes | 100 |
| Computer use | 100 | On single-family dwellings only | 40 |
| Armories and drill rooms | 150 | Garages (passenger cars only) <br> Trucks and buses (see foot note) |  |
| Assembly areas and theaters |  | Trucks and buses (see foot note) |  |
| Fixed seats (fastened to floors) | 60 | Grandstands (see stadium and arena bleachers) |  |
| Lobbies | 100 | Gymnasiums, main floors, and balconies | 100 |
| Movable seats | 100 | Hospitals |  |
| Platforms (assembly) | 100 | Operating rooms, laboratories | 60 |
| Stage floors | 150 | Private rooms | 40 |
| Balconies (exterior) | 100 | Wards | 40 |
| On one and two family residences only, and not exceeding 100 ft 2 | 60 | Corridors above first floor | 80 |
| Bowling alleys, poolrooms, and similar recreational areas | 75 | Hotels (see residential) |  |
| Catwalks for maintenance access | 40 | Libraries |  |
| Corridors |  | Reading rooms | 60 |
| First floor | 100 | Stack rooms | 150 |
| Other floors, same as occupancy served except as indicated |  | Corridors above first floor | 80 |
| Dance halls and ballrooms | 100 | Manufacturing |  |
| Decks (patio and roof) |  | Light | 125 |
| Same as area served, or for the type of occupancy accommodated |  | Heavy | 250 |


| Table C1: (Continued) |  |  |  |
| :---: | :---: | :---: | :---: |
| Occupancy or Use | Live <br> Load, psf | Occupancy or Use | Live <br> Load, psf |
| Marquees and Canopies | 75 | Sidewaks, vehicular driveways, and yards subject to trucking | 250 |
| Office Buildings |  | Stadium and arenas |  |
| File and computer rooms shall be designed for heavier loads based on anticipated occupancy |  | Pleachers | 100 |
| Lobbies and first-floor corridors | 100 | Fixed seats (fastened to floors) | 60 |
| Offices | 50 | Stairs and exitways | 100 |
| Corridors above first floor | 80 | One and two-family residences only | 40 |
| Penal institutions |  | Storage areas above ceilings | 20 |
| Cell blocks | 40 | Storage warehouses (shall be designed for heavier loads if required for anticipated storage) |  |
| Corridors | 100 | Light | 125 |
| Residential |  | Heavy | 250 |
| Dwellings (one and two-family) |  | Stores |  |
| Uninhabitable attics without storage | 10 | Retail |  |
| Uninhabitable attics with storage | 20 | First floor | 100 |
| Habitable attics and sleeping areas | 30 | Upper floors | 73 |
| All other areas except stairs and balconies | 40 | Wholesale, all floors | 125 |
| Hotels and multifamily houses |  | Walkways and elevated platforms (other than exitways) | 60 |
| Private rooms and corridors serving them | 40 | Yards and terraces, pedestrians | 100 |
| Public rooms and corridors serving them | 100 |  |  |
| Reviewing stands, grandstands and bleachers | 100 |  |  |
| Schools |  |  |  |
| Classrooms | 40 |  |  |
| Corridors above first floor | 80 |  |  |
| First-floor corridors | 100 |  |  |
| ${ }^{a}$ Garages accommodating trucks and buses shall be designed in accordance with an approved method that contains provisions for truck and bus loadings. |  |  |  |

## Appendix D

## Various Structural Configurations














## Appendix E

Cutoff or bend points for bars in approximately equal spans with uniformly distributed loads:


## References

> Design of Concrete Structures by Nilson, Darwin and Dolan (13 ${ }^{\text {th }}$ ed.)
> ACI 318-02/05

