# Logic Gates

#### **CHAPTER OUTLINE**

3-1 The Inverter

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- 3–2 The AND Gate
- 3–3 The OR Gate
- 3-4 The NAND Gate
- 3-5 The NOR Gate
- 3-6 The Exclusive-OR and Exclusive-NOR Gates
- 3-7 Programmable Logic
- 3-8 **Fixed-Function Logic Gates**
- 3-9 Troubleshooting

#### CHAPTER OBJECTIVES

- Describe the operation of the inverter, the AND gate, and the OR gate
- Describe the operation of the NAND gate and the NOR gate
- Express the operation of NOT, AND, OR, NAND, and NOR gates with Boolean algebra
- Describe the operation of the exclusive-OR and exclusive-NOR gates
- Use logic gates in simple applications
- Recognize and use both the distinctive shape logic gate symbols and the rectangular outline logic gate symbols of ANSI/IEEE Standard 91-1984/Std. 91a-1991
- Construct timing diagrams showing the proper time relationships of inputs and outputs for the various logic gates
- Discuss the basic concepts of programmable logic
- Make basic comparisons between the major IC technologies—CMOS and bipolar (TTL)
- Explain how the different series within the CMOS and bipolar (TTL) families differ from each other
- Define propagation delay time, power dissipation, speed-power product, and fan-out in relation to logic gates

List specific fixed-function integrated circuit devices that contain the various logic gates

**CHAPTER** 

Troubleshoot logic gates for opens and shorts by using the oscilloscope

#### **KEY TERMS**

Key terms are in order of appearance in the chapter.

- Inverter
- Truth table
- Boolean algebra
- Complement
- AND gate
- OR gate
- NAND gate
- NOR gate
- Exclusive-OR gate
- Exclusive-NOR gate
- AND array
- Fuse
- Antifuse

#### VISIT THE WEBSITE

Study aids for this chapter are available at http://www.pearsonglobaleditions.com/floyd

#### INTRODUCTION

The emphasis in this chapter is on the operation, application, and troubleshooting of logic gates. The relationship of input and output waveforms of a gate using timing diagrams is thoroughly covered.

Logic symbols used to represent the logic gates are in accordance with ANSI/IEEE Standard 91-1984/ Std. 91a-1991. This standard has been adopted by private industry and the military for use in internal documentation as well as published literature.

- EPROM
  - EEPROM
  - Flash
  - SRAM
  - Target device
  - JTAG
  - VHDL
  - CMOS
  - **Bipolar**
  - Propagation delay time
  - Fan-out
  - Unit load

R1

Both fixed-function logic and programmable logic are discussed in this chapter. Because integrated circuits (ICs) are used in all applications, the logic function of a device is generally of greater importance to the technician or technologist than the details of the component-level circuit operation within the IC package. Therefore, detailed coverage of the devices at the component level can be treated as an optional topic. Digital integrated circuit technologies are discussed in Chapter 15 on the website, all or parts of which may be introduced at appropriate points throughout the text.

Suggestion: Review Section 1–3 before you start this chapter.

#### 3–1 The Inverter

The inverter (NOT circuit) performs the operation called *inversion* or *complementation*. The inverter changes one logic level to the opposite level. In terms of bits, it changes a 1 to a 0 and a 0 to a 1.

After completing this section, you should be able to

- Identify negation and polarity indicators
- Identify an inverter by either its distinctive shape symbol or its rectangular outline symbol
- Produce the truth table for an inverter
- Describe the logical operation of an inverter

Standard logic symbols for the **inverter** are shown in Figure 3–1. Part (a) shows the *distinctive shape* symbols, and part (b) shows the *rectangular outline* symbols. In this textbook, distinctive shape symbols are generally used; however, the rectangular outline symbols are found in many industry publications, and you should become familiar with them as well. (Logic symbols are in accordance with **ANSI/IEEE** Standard 91-1984 and its supplement Standard 91a-1991.)



(a) Distinctive shape symbols with negation indicators

(b) Rectangular outline symbols with polarity indicators



#### The Negation and Polarity Indicators

The negation indicator is a "bubble" ( $\bigcirc$ ) that indicates **inversion** or *complementation* when it appears on the input or output of any logic element, as shown in Figure 3–1(a) for the inverter. Generally, inputs are on the left of a logic symbol and the output is on the right. When appearing on the input, the bubble means that a 0 is the active or *asserted* input state, and the input is called an active-LOW input. When appearing on the output, the bubble means that a 0 is the active or asserted an active-LOW input. When appearing on the output, the bubble means that a 0 is the active or asserted output state, and the output is called an active-LOW output. The absence of a bubble on the input or output means that a 1 is the active or asserted state, and in this case, the input or output is called active-HIGH.

The polarity or level indicator is a "triangle" ( $\searrow$ ) that indicates inversion when it appears on the input or output of a logic element, as shown in Figure 3–1(b). When appearing on the input, it means that a LOW level is the active or asserted input state. When appearing on the output, it means that a LOW level is the active or asserted output state.

Either indicator (bubble or triangle) can be used both on distinctive shape symbols and on rectangular outline symbols. Figure 3-1(a) indicates the principal inverter symbols used in this text. Note that a change in the placement of the negation or polarity indicator does not imply a change in the way an inverter operates.

#### **Inverter Truth Table**

When a HIGH level is applied to an inverter input, a LOW level will appear on its output. When a LOW level is applied to its input, a HIGH will appear on its output. This operation is summarized in Table 3–1, which shows the output for each possible input in terms of levels and corresponding bits. A table such as this is called a **truth table**.

#### **Inverter Operation**

Figure 3–2 shows the output of an inverter for a pulse input, where  $t_1$  and  $t_2$  indicate the corresponding points on the input and output pulse waveforms.

### When the input is LOW, the output is HIGH; when the input is HIGH, the output is LOW, thereby producing an inverted output pulse.



**FIGURE 3–2** Inverter operation with a pulse input. Open file F03-02 to verify inverter operation. *A Multisim tutorial is available on the website*.

#### **Timing Diagrams**

Recall from Chapter 1 that a *timing diagram* is basically a graph that accurately displays the relationship of two or more waveforms with respect to each other on a time basis. For example, the time relationship of the output pulse to the input pulse in Figure 3–2 can be shown with a simple timing diagram by aligning the two pulses so that the occurrences of the pulse edges appear in the proper time relationship. The rising edge of the input pulse and the falling edge of the output pulse occur at the same time (ideally). Similarly, the falling edge of the input pulse and the rising edge of the output pulse occur at the same time (ideally). This timing relationship is shown in Figure 3–3. In practice, there is a very small delay from the input transition until the corresponding output transition. Timing diagrams are especially useful for illustrating the time relationship of digital waveforms with multiple pulses.

#### EXAMPLE 3-1

A waveform is applied to an inverter in Figure 3–4. Determine the output waveform corresponding to the input and show the timing diagram. According to the placement of the bubble, what is the active output state?



TABLE 3-	1
Inverter truth table.	
Input	Output
LOW (0)	HIGH (1)
HIGH (1)	LOW (0)

MultiSim

### A timing diagram shows how two or more waveforms relate in time.



**FIGURE 3–3** Timing diagram for the case in Figure 3–2.

#### Solution

The output waveform is exactly opposite to the input (inverted), as shown in Figure 3–5, which is the basic timing diagram. The active or asserted output state is 0.



#### FIGURE 3-5

#### **Related Problem\***

If the inverter is shown with the negative indicator (bubble) on the input instead of the output, how is the timing diagram affected?

\*Answers are at the end of the chapter.

#### Logic Expression for an Inverter

In **Boolean algebra**, which is the mathematics of logic circuits and will be covered thoroughly in Chapter 4, a variable is generally designated by one or two letters although there can be more. Letters near the beginning of the alphabet usually designate inputs, while letters near the end of the alphabet usually designate outputs. The **complement** of a variable is designated by a bar over the letter. A variable can take on a value of either 1 or 0. If a given variable is 1, its complement is 0 and vice versa.

The operation of an inverter (NOT circuit) can be expressed as follows: If the input variable is called *A* and the output variable is called *X*, then

 $X = \overline{A}$ 

 $A \longrightarrow X = \overline{A}$ 

Boolean algebra uses variables and operators to describe a logic circuit.

**FIGURE 3–6** The inverter complements an input variable.

This expression states that the output is the complement of the input, so if A = 0, then X = 1, and if A = 1, then X = 0. Figure 3–6 illustrates this. The complemented variable  $\overline{A}$  can be read as "A bar" or "not A."

#### An Application

Figure 3–7 shows a circuit for producing the 1's complement of an 8-bit binary number. The bits of the binary number are applied to the inverter inputs and the 1's complement of the number appears on the outputs.



FIGURE 3-7 Example of a 1's complement circuit using inverters.

#### SECTION 3-1 CHECKUP

Answers are at the end of the chapter.

- 1. When a 1 is on the input of an inverter, what is the output?
- 2. An active-HIGH pulse (HIGH level when asserted, LOW level when not) is required on an inverter input.
  - (a) Draw the appropriate logic symbol, using the distinctive shape and the negation indicator, for the inverter in this application.
  - (b) Describe the output when a positive-going pulse is applied to the input of an inverter.

### 3-2 The AND Gate

The AND gate is one of the basic gates that can be combined to form any logic function. An AND gate can have two or more inputs and performs what is known as logical multiplication.

After completing this section, you should be able to

- Identify an AND gate by its distinctive shape symbol or by its rectangular outline symbol
- Describe the operation of an AND gate
- · Generate the truth table for an AND gate with any number of inputs
- Produce a timing diagram for an AND gate with any specified input waveforms
- Write the logic expression for an AND gate with any number of inputs
- Discuss examples of AND gate applications

The term *gate* was introduced in Chapter 1 and is used to describe a circuit that performs a basic logic operation. The AND gate is composed of two or more inputs and a single output, as indicated by the standard logic symbols shown in Figure 3–8. Inputs are on the left, and the output is on the right in each symbol. Gates with two inputs are shown; however, an AND gate can have any number of inputs greater than one. Although examples of both distinctive shape symbols and rectangular outline symbols are shown, the distinctive shape symbol, shown in part (a), is used predominantly in this book.



### InfoNote

Logic gates are one of the fundamental building blocks of digital systems. Most of the functions in a computer, with the exception of certain types of memory, are implemented with logic gates used on a very large scale. For example, a microprocessor, which is the main part of a computer, is made up of hundreds of thousands or even millions of logic gates.

FIGURE 3–8 Standard logic symbols for the AND gate showing two inputs (ANSI/IEEE Std. 91-1984/Std. 91a-1991).

#### Operation of an AND Gate

An **AND** gate produces a HIGH output *only* when *all* of the inputs are HIGH. When any of the inputs is LOW, the output is LOW. Therefore, the basic purpose of an AND gate is to determine when certain conditions are simultaneously true, as indicated by HIGH levels on all of its inputs, and to produce a HIGH on its output to indicate that all these conditions are

An AND gate can have more than two inputs.

true. The inputs of the 2-input AND gate in Figure 3–8 are labeled *A* and *B*, and the output is labeled *X*. The gate operation can be stated as follows:

### For a 2-input AND gate, output *X* is HIGH only when inputs *A* and *B* are HIGH; *X* is LOW when either *A* or *B* is LOW, or when both *A* and *B* are LOW.

Figure 3–9 illustrates a 2-input AND gate with all four possibilities of input combinations and the resulting output for each.





**FIGURE 3–9** All possible logic levels for a 2-input AND gate. Open file F03-09 to verify AND gate operation.

#### AND Gate Truth Table

For an AND gate, all HIGH inputs produce a HIGH output.

#### TABLE 3-2

Truth table for a 2-input AND gate.

Inp	outs	Output
A	B	X
0	0	0
0	1	0
1	0	0
1	1	1

1 = HIGH, 0 = LOW

#### The logical operation of a gate can be expressed with a truth table that lists all input combinations with the corresponding outputs, as illustrated in Table 3–2 for a 2-input AND gate. The truth table can be expanded to any number of inputs. Although the terms HIGH and LOW tend

tions with the corresponding outputs, as illustrated in Table 3–2 for a 2-input AND gate. The truth table can be expanded to any number of inputs. Although the terms HIGH and LOW tend to give a "physical" sense to the input and output states, the truth table is shown with 1s and 0s; a HIGH is equivalent to a 1 and a LOW is equivalent to a 0 in positive logic. For any AND gate, regardless of the number of inputs, the output is HIGH *only* when *all* inputs are HIGH.

The total number of possible combinations of binary inputs to a gate is determined by the following formula:

$$N = 2^n$$
 Equation 3–1

where N is the number of possible input combinations and n is the number of input variables. To illustrate,

For two input variables:	$N = 2^2 = 4$ combinations
For three input variables:	$N = 2^3 = 8$ combinations
For four input variables:	$N = 2^4 = 16$ combinations

You can determine the number of input bit combinations for gates with any number of inputs by using Equation 3–1.

EXA	MP	LE	3-2

	Inputs		Output
A	B	С	X
0	0	0	0
0	0	1	0
0	1	0	0
0	1	1	0
1	0	0	0
1	0	1	0
1	1	0	0
1	1	1	1

- (a) Develop the truth table for a 3-input AND gate.
- (b) Determine the total number of possible input combinations for a 4-input AND gate.

#### Solution

- (a) There are eight possible input combinations (2<sup>3</sup> = 8) for a 3-input AND gate. The input side of the truth table (Table 3–3) shows all eight combinations of three bits. The output side is all 0s except when all three input bits are 1s.
- (b)  $N = 2^4 = 16$ . There are 16 possible combinations of input bits for a 4-input AND gate.

#### **Related Problem**

Develop the truth table for a 4-input AND gate.

#### AND Gate Operation with Waveform Inputs

In most applications, the inputs to a gate are not stationary levels but are voltage waveforms that change frequently between HIGH and LOW logic levels. Now let's look at the operation of AND gates with pulse waveform inputs, keeping in mind that an AND gate obeys the truth table operation regardless of whether its inputs are constant levels or levels that change back and forth.

Let's examine the waveform operation of an AND gate by looking at the inputs with respect to each other in order to determine the output level at any given time. In Figure 3–10, inputs *A* and *B* are both HIGH (1) during the time interval,  $t_1$ , making output *X* HIGH (1) during this interval. During time interval  $t_2$ , input *A* is LOW (0) and input *B* is HIGH (1), so the output is LOW (0). During time interval  $t_3$ , both inputs are HIGH (1) again, and therefore the output is HIGH (1). During time interval  $t_4$ , input *A* is HIGH (1) and input *B* is LOW (0), resulting in a LOW (0) output. Finally, during time interval  $t_5$ , input *A* is LOW (0), input *B* is LOW (0), and the output is therefore LOW (0). As you know, a diagram of input and output waveforms showing time relationships is called a *timing diagram*.



**FIGURE 3–10** Example of AND gate operation with a timing diagram showing input and output relationships.

#### **EXAMPLE 3-3**

If two waveforms, *A* and *B*, are applied to the AND gate inputs as in Figure 3–11, what is the resulting output waveform?



#### FIGURE 3-11

#### **Solution**

The output waveform X is HIGH only when both A and B waveforms are HIGH as shown in the timing diagram in Figure 3-11.

#### **Related Problem**

Determine the output waveform and show a timing diagram if the second and fourth pulses in waveform *A* of Figure 3–11 are replaced by LOW levels.

Remember, when analyzing the waveform operation of logic gates, it is important to pay careful attention to the time relationships of all the inputs with respect to each other and to the output.

#### **EXAMPLE 3-4**

For the two input waveforms, *A* and *B*, in Figure 3–12, show the output waveform with its proper relation to the inputs.



#### FIGURE 3–12

#### **Solution**

The output waveform is HIGH only when both of the input waveforms are HIGH as shown in the timing diagram.

#### **Related Problem**

Show the output waveform if the B input to the AND gate in Figure 3–12 is always HIGH.

#### EXAMPLE 3-5

For the 3-input AND gate in Figure 3–13, determine the output waveform in relation to the inputs.



#### FIGURE 3-13

#### **Solution**

The output waveform X of the 3-input AND gate is HIGH only when all three input waveforms A, B, and C are HIGH.

#### **Related Problem**

What is the output waveform of the AND gate in Figure 3–13 if the *C* input is always HIGH?

#### EXAMPLE 3-6

Use Multisim to simulate a 3-input AND gate with input waveforms that cycle through binary numbers 0 through 9.

#### Solution

Use the Multisim word generator in the up counter mode to provide the combination of waveforms representing the binary sequence, as shown in Figure 3–14. The first three waveforms on the oscilloscope display are the inputs, and the bottom waveform is the output.





#### FIGURE 3-14

#### **Related Problem**

#### **MultiSim**

Use Multisim software to create the setup and simulate the 3-input AND gate as illustrated in this example.

#### Logic Expressions for an AND Gate

The logical AND function of two variables is represented mathematically either by placing a dot between the two variables, as  $A \cdot B$ , or by simply writing the adjacent letters without the dot, as *AB*. We will normally use the latter notation.

#### InfoNote

Processors can utilize all of the basic logic operations when it is necessary to selectively manipulate certain bits in one or more bytes of data. Selective bit manipulations are done with a *mask*. For example, to clear (make all 0s) the right four bits in a data byte but keep the left four bits, ANDing the data byte with 11110000 will do the job. Notice that any bit ANDed with zero will be 0 and any bit ANDed with 1 will remain the same. If 10101010 is ANDed with the mask 11110000, the result is 10100000.

When variables are shown together like *ABC*, they are ANDed.

**Boolean multiplication** follows the same basic rules governing binary multiplication, which were discussed in Chapter 2 and are as follows:

$0 \cdot 0$	=	0
$0 \cdot 1$	=	0
$1 \cdot 0$	=	0
1 • 1	=	1

#### Boolean multiplication is the same as the AND function.

The operation of a 2-input AND gate can be expressed in equation form as follows: If one input variable is A, if the other input variable is B, and if the output variable is X, then the Boolean expression is

$$X = AB$$

Figure 3–15(a) shows the AND gate logic symbol with two input variables and the output variable indicated.



FIGURE 3-15 Boolean expressions for AND gates with two, three, and four inputs.

To extend the AND expression to more than two input variables, simply use a new letter for each input variable. The function of a 3-input AND gate, for example, can be expressed as X = ABC, where A, B, and C are the input variables. The expression for a 4-input AND gate can be X = ABCD, and so on. Parts (b) and (c) of Figure 3–15 show AND gates with three and four input variables, respectively.

You can evaluate an AND gate operation by using the Boolean expressions for the output. For example, each variable on the inputs can be either a 1 or a 0; so for the 2-input AND gate, make substitutions in the equation for the output, X = AB, as shown in Table 3–4. This evaluation shows that the output X of an AND gate is a 1 (HIGH) only when both inputs are 1s (HIGHs). A similar analysis can be made for any number of input variables.

#### Applications

#### The AND Gate as an Enable/Inhibit Device

A common application of the AND gate is to **enable** (that is, to allow) the passage of a signal (pulse waveform) from one point to another at certain times and to **inhibit** (prevent) the passage at other times.

A simple example of this particular use of an AND gate is shown in Figure 3–16, where the AND gate controls the passage of a signal (waveform A) to a digital counter. The purpose of this circuit is to measure the frequency of waveform A. The enable pulse has a width of precisely 1 ms. When the enable pulse is HIGH, waveform A passes through the gate to the counter; and when the enable pulse is LOW, the signal is prevented from passing through the gate (inhibited).

During the 1 millisecond (1 ms) interval of the enable pulse, pulses in waveform *A* pass through the AND gate to the counter. The number of pulses passing through during the 1 ms interval is equal to the frequency of waveform *A*. For example, Figure 3–16 shows six pulses in one millisecond, which is a frequency of 6 kHz. If 1000 pulses pass through the gate in the 1 ms interval of the enable pulse, there are 1000 pulses/ms, or a frequency of 1 MHz.

TABLE 3-4			
A	В	AB = X	
0	0	$0 \cdot 0 = 0$	
0	1	$0 \cdot 1 = 0$	
1	0	$1 \cdot 0 = 0$	
1	1	$1 \cdot 1 = 1$	



**FIGURE 3–16** An AND gate performing an enable/inhibit function for a frequency counter.

The counter counts the number of pulses per second and produces a binary output that goes to a decoding and display circuit to produce a readout of the frequency. The enable pulse repeats at certain intervals and a new updated count is made so that if the frequency changes, the new value will be displayed. Between enable pulses, the counter is reset so that it starts at zero each time an enable pulse occurs. The current frequency count is stored in a register so that the display is unaffected by the resetting of the counter.

#### A Seat Belt Alarm System

In Figure 3–17, an AND gate is used in a simple automobile seat belt alarm system to detect when the ignition switch is on *and* the seat belt is unbuckled. If the ignition switch is on, a HIGH is produced on input A of the AND gate. If the seat belt is not properly buckled, a HIGH is produced on input B of the AND gate. Also, when the ignition switch is turned on, a timer is started that produces a HIGH on input C for 30 s. If all three conditions exist—that is, if the ignition is on *and* the seat belt is unbuckled *and* the timer is running—the output of the AND gate is HIGH, and an audible alarm is energized to remind the driver.



FIGURE 3-17 A simple seat belt alarm circuit using an AND gate.

#### SECTION 3-2 CHECKUP

- 1. When is the output of an AND gate HIGH?
- 2. When is the output of an AND gate LOW?
- 3. Describe the truth table for a 5-input AND gate.

#### **3–3** The OR Gate

The OR gate is another of the basic gates from which all logic functions are constructed. An OR gate can have two or more inputs and performs what is known as logical addition.

After completing this section, you should be able to

- Identify an OR gate by its distinctive shape symbol or by its rectangular outline symbol
- Describe the operation of an OR gate
- Generate the truth table for an OR gate with any number of inputs
- Produce a timing diagram for an OR gate with any specified input waveforms
- Write the logic expression for an OR gate with any number of inputs
- Discuss an OR gate application

An OR gate can have more than two inputs.

An **OR gate** has two or more inputs and one output, as indicated by the standard logic symbols in Figure 3–18, where OR gates with two inputs are illustrated. An OR gate can have any number of inputs greater than one. Although both distinctive shape and rectangular outline symbols are shown, the distinctive shape OR gate symbol is used in this textbook.



**FIGURE 3–18** Standard logic symbols for the OR gate showing two inputs (ANSI/IEEE Std. 91-1984/Std. 91a-1991).

#### Operation of an OR Gate

An OR gate produces a HIGH on the output when *any* of the inputs is HIGH. The output is LOW only when all of the inputs are LOW. Therefore, an OR gate determines when one or more of its inputs are HIGH and produces a HIGH on its output to indicate this condition. The inputs of the 2-input OR gate in Figure 3–18 are labeled *A* and *B*, and the output is labeled *X*. The operation of the gate can be stated as follows:

### For a 2-input OR gate, output X is HIGH when either input A or input B is HIGH, or when both A and B are HIGH; X is LOW only when both A and B are LOW.

The HIGH level is the active or asserted output level for the OR gate. Figure 3–19 illustrates the operation for a 2-input OR gate for all four possible input combinations.





**FIGURE 3–19** All possible logic levels for a 2-input OR gate. Open file F03-19 to verify OR gate operation.

For an OR gate, at least one HIGH input produces a HIGH output.

#### **OR Gate Truth Table**

The operation of a 2-input OR gate is described in Table 3–5. This truth table can be expanded for any number of inputs; but regardless of the number of inputs, the output is HIGH when one or more of the inputs are HIGH.

#### OR Gate Operation with Waveform Inputs

Now let's look at the operation of an OR gate with pulse waveform inputs, keeping in mind its logical operation. Again, the important thing in the analysis of gate operation with pulse waveforms is the time relationship of all the waveforms involved. For example, in Figure 3–20, inputs *A* and *B* are both HIGH (1) during time interval  $t_1$ , making output *X* HIGH (1). During time interval  $t_2$ , input *A* is LOW (0), but because input *B* is HIGH (1), the output is HIGH (1). Both inputs are LOW (0) during time interval  $t_3$ , so there is a LOW (0) output during this time. During time interval  $t_4$ , the output is HIGH (1) because input *A* is HIGH (1).



TAB	LE 3–5	
Truth OR g	table fo ate.	or a 2-input
In	puts	Output
Δ	R	Y

A	В	X
0	0	0
0	1	1
1	0	1
1	1	1

1 = HIGH, 0 = LOW

**FIGURE 3–20** Example of OR gate operation with a timing diagram showing input and output time relationships.

In this illustration, we have applied the truth table operation of the OR gate to each of the time intervals during which the levels are nonchanging. Examples 3–7 through 3–9 further illustrate OR gate operation with waveforms on the inputs.



#### Solution

The output waveform *X* of a 2-input OR gate is HIGH when either or both input waveforms are HIGH as shown in the timing diagram. In this case, both input waveforms are never HIGH at the same time.

#### **Related Problem**

Determine the output waveform and show the timing diagram if input *A* is changed such that it is HIGH from the beginning of the existing first pulse to the end of the existing second pulse.

#### EXAMPLE 3-8

For the two input waveforms, A and B, in Figure 3–22, show the output waveform with its proper relation to the inputs.



#### FIGURE 3-22

#### Solution

When either or both input waveforms are HIGH, the output is HIGH as shown by the output waveform *X* in the timing diagram.

#### **Related Problem**

Determine the output waveform and show the timing diagram if the middle pulse of input *A* is replaced by a LOW level.

#### **EXAMPLE 3-9**

For the 3-input OR gate in Figure 3–23, determine the output waveform in proper time relation to the inputs.



#### FIGURE 3-23

#### Solution

The output is HIGH when one or more of the input waveforms are HIGH as indicated by the output waveform *X* in the timing diagram.

#### **Related Problem**

Determine the output waveform and show the timing diagram if input *C* is always LOW.

#### Logic Expressions for an OR Gate

The logical OR function of two variables is represented mathematically by a + between the two variables, for example, A + B. The plus sign is read as "OR."

Addition in Boolean algebra involves variables whose values are either binary 1 or binary 0. The basic rules for **Boolean addition** are as follows:

$$0 + 0 = 0$$
  
 $0 + 1 = 1$   
 $1 + 0 = 1$   
 $1 + 1 = 1$ 

#### Boolean addition is the same as the OR function.

Notice that Boolean addition differs from binary addition in the case where two 1s are added. There is no carry in Boolean addition.

The operation of a 2-input OR gate can be expressed as follows: If one input variable is A, if the other input variable is B, and if the output variable is X, then the Boolean expression is

$$X = A + B$$

Figure 3–24(a) shows the OR gate logic symbol with two input variables and the output variable labeled.



FIGURE 3-24 Boolean expressions for OR gates with two, three, and four inputs.

To extend the OR expression to more than two input variables, a new letter is used for each additional variable. For instance, the function of a 3-input OR gate can be expressed as X = A + B + C. The expression for a 4-input OR gate can be written as X = A + B + C + D, and so on. Parts (b) and (c) of Figure 3–24 show OR gates with three and four input variables, respectively.

OR gate operation can be evaluated by using the Boolean expressions for the output X by substituting all possible combinations of 1 and 0 values for the input variables, as shown in Table 3–6 for a 2-input OR gate. This evaluation shows that the output X of an OR gate is a 1 (HIGH) when any one or more of the inputs are 1 (HIGH). A similar analysis can be extended to OR gates with any number of input variables.

#### An Application

A simplified portion of an intrusion detection and alarm system is shown in Figure 3–25. This system could be used for one room in a home—a room with two windows and a door. The sensors are magnetic switches that produce a HIGH output when open and a LOW output when closed. As long as the windows and the door are secured, the switches are closed and all three of the OR gate inputs are LOW. When one of the windows or the door is opened, a HIGH is produced on that input to the OR gate and the gate output goes HIGH. It then activates and latches an alarm circuit to warn of the intrusion.

#### InfoNote

A mask operation that is used in computer programming to selectively make certain bits in a data byte equal to 1 (called setting) while not affecting any other bit is done with the OR operation. A mask is used that contains a 1 in any position where a data bit is to be set. For example, if you want to force the sign bit in an 8-bit signed number to equal 1, but leave all other bits unchanged, you can OR the data byte with the mask 10000000.

TAE	BLE 3-	6
A	B	A + B = X
0	0	0 + 0 = 0
0	1	0 + 1 = 1
1	0	1 + 0 = 1
1	1	1 + 1 = 1

When variables are separated by +, they are ORed.





#### SECTION 3-3 CHECKUP

- **1.** When is the output of an OR gate HIGH?
- 2. When is the output of an OR gate LOW?
- **3.** Describe the truth table for a 3-input OR gate.

### 3-4 The NAND Gate

The NAND gate is a popular logic element because it can be used as a universal gate; that is, NAND gates can be used in combination to perform the AND, OR, and inverter operations. The universal property of the NAND gate will be examined thoroughly in Chapter 5.

After completing this section, you should be able to

- Identify a NAND gate by its distinctive shape symbol or by its rectangular outline symbol
- Describe the operation of a NAND gate
- Develop the truth table for a NAND gate with any number of inputs
- Produce a timing diagram for a NAND gate with any specified input waveforms
- Write the logic expression for a NAND gate with any number of inputs
- Describe NAND gate operation in terms of its negative-OR equivalent
- Discuss examples of NAND gate applications

The NAND gate is the same as the AND gate except the output is inverted.

The term *NAND* is a contraction of NOT-AND and implies an AND function with a complemented (inverted) output. The standard logic symbol for a 2-input NAND gate and its equivalency to an AND gate followed by an inverter are shown in Figure 3-26(a), where the symbol  $\equiv$  means equivalent to. A rectangular outline symbol is shown in part (b).



(a) Distinctive shape, 2-input NAND gate and its NOT/AND equivalent



FIGURE 3-26 Standard NAND gate logic symbols (ANSI/IEEE Std. 91-1984/Std. 91a-1991).

#### Operation of a NAND Gate

A **NAND gate** produces a LOW output only when all the inputs are HIGH. When any of the inputs is LOW, the output will be HIGH. For the specific case of a 2-input NAND gate, as shown in Figure 3-26 with the inputs labeled *A* and *B* and the output labeled *X*, the operation can be stated as follows:

### For a 2-input NAND gate, output X is LOW only when inputs A and B are HIGH; X is HIGH when either A or B is LOW, or when both A and B are LOW.

This operation is opposite that of the AND in terms of the output level. In a NAND gate, the LOW level (0) is the active or asserted output level, as indicated by the bubble on the output. Figure 3–27 illustrates the operation of a 2-input NAND gate for all four input combinations, and Table 3–7 is the truth table summarizing the logical operation of the 2-input NAND gate.



**FIGURE 3–27** Operation of a 2-input NAND gate. Open file F03-27 to verify NAND gate operation.

#### NAND Gate Operation with Waveform Inputs

Now let's look at the pulse waveform operation of a NAND gate. Remember from the truth table that the only time a LOW output occurs is when all of the inputs are HIGH.



#### Solution

Output waveform *X* is LOW only during the four time intervals when both input waveforms *A* and *B* are HIGH as shown in the timing diagram.

#### **Related Problem**

Determine the output waveform and show the timing diagram if input waveform B is inverted.

#### TABLE 3-7

Truth table for a 2-input NAND gate.

Inp	outs	Output
A	В	X
0	0	1
0	1	1
1	0	1
1	1	0

1 = HIGH, 0 = LOW.



#### EXAMPLE 3-11

Show the output waveform for the 3-input NAND gate in Figure 3–29 with its proper time relationship to the inputs.



FIGURE 3-29

#### Solution

The output waveform *X* is LOW only when all three input waveforms are HIGH as shown in the timing diagram.

#### **Related Problem**

Determine the output waveform and show the timing diagram if input waveform A is inverted.

#### Negative-OR Equivalent Operation of a NAND Gate

Inherent in a NAND gate's operation is the fact that one or more LOW inputs produce a HIGH output. Table 3–7 shows that output X is HIGH (1) when any of the inputs, A and B, is LOW (0). From this viewpoint, a NAND gate can be used for an OR operation that requires one or more LOW inputs to produce a HIGH output. This aspect of NAND operation is referred to as **negative-OR**. The term *negative* in this context means that the inputs are defined to be in the active or asserted state when LOW.



FIGURE 3–30 ANSI/IEEE standard symbols representing the two equivalent operations of a NAND gate.

### For a 2-input NAND gate performing a negative-OR operation, output *X* is HIGH when either input *A* or input *B* is LOW, or when both *A* and *B* are LOW.

When a NAND gate is used to detect one or more LOWs on its inputs rather than all HIGHs, it is performing the negative-OR operation and is represented by the standard logic symbol shown in Figure 3–30. Although the two symbols in Figure 3–30 represent the same physical gate, they serve to define its role or mode of operation in a particular application, as illustrated by Examples 3–12 and 3–13.

#### EXAMPLE 3-12

Two tanks store certain liquid chemicals that are required in a manufacturing process. Each tank has a sensor that detects when the chemical level drops to 25% of full. The sensors produce a HIGH level of 5 V when the tanks are more than one-quarter full. When the volume of chemical in a tank drops to one-quarter full, the sensor puts out a LOW level of 0 V.

It is required that a single green light-emitting diode (LED) on an indicator panel show when both tanks are more than one-quarter full. Show how a NAND gate can be used to implement this function.

#### Solution

Figure 3–31 shows a NAND gate with its two inputs connected to the tank level sensors and its output connected to the indicator panel. The operation can be stated as follows: If tank *A* and tank *B* are above one-quarter full, the LED is on.



#### FIGURE 3-31

As long as both sensor outputs are HIGH (5 V), indicating that both tanks are more than one-quarter full, the NAND gate output is LOW (0 V). The green LED circuit is connected so that a LOW voltage turns it on. The resistor limits the LED current.

#### **Related Problem**

How can the circuit of Figure 3–31 be modified to monitor the levels in three tanks rather than two?

#### EXAMPLE 3-13

For the process described in Example 3–12 it has been decided to have a red LED display come on when at least one of the tanks falls to the quarter-full level rather than have the green LED display indicate when both are above one quarter. Show how this requirement can be implemented.

#### **Solution**

Figure 3–32 shows a NAND gate operating as a negative-OR gate to detect the occurrence of at least one LOW on its inputs. A sensor puts out a LOW voltage if the volume in its tank goes to one-quarter full or less. When this happens, the gate output goes HIGH. The red LED circuit in the panel is connected so that a HIGH voltage turns it on. The operation can be stated as follows: If tank *A or* tank *B or* both are below one-quarter full, the LED is on.



Notice that, in this example and in Example 3–12, the same 2-input NAND gate is used, but in this example it is operating as a negative-OR gate and a different gate symbol is used in the schematic. This illustrates the different way in which the NAND and equivalent negative-OR operations are used.

#### **Related Problem**

How can the circuit in Figure 3–32 be modified to monitor four tanks rather than two?

#### EXAMPLE 3-14

For the 4-input NAND gate in Figure 3–33, operating as a negative-OR gate, determine the output with respect to the inputs.



#### FIGURE 3-33

#### Solution

The output waveform *X* is HIGH any time an input waveform is LOW as shown in the timing diagram.

#### **Related Problem**

Determine the output waveform if input waveform A is inverted before it is applied to the gate.

#### Logic Expressions for a NAND Gate

The Boolean expression for the output of a 2-input NAND gate is

 $X = \overline{AB}$ 

This expression says that the two input variables, A and B, are first ANDed and then complemented, as indicated by the bar over the AND expression. This is a description in equation form of the operation of a NAND gate with two inputs. Evaluating this expression for all possible values of the two input variables, you get the results shown in Table 3–8.

Once an expression is determined for a given logic function, that function can be evaluated for all possible values of the variables. The evaluation tells you exactly what the output of the logic circuit is for each of the input conditions, and it therefore gives you a complete description of the circuit's logic operation. The NAND expression can be extended to more than two input variables by including additional letters to represent the other variables.

A bar over a variable or variables indicates an inversion.

TAB	LE 3-8	
A	B	$\overline{AB} = X$
0	0	$\overline{0 \cdot 0} = \overline{0} = 1$
0	1	$\overline{0 \cdot 1} = \overline{0} = 1$
1	0	$\overline{1 \cdot 0} = \overline{0} = 1$
1	1	$\overline{1\cdot 1} = \overline{1} = 0$

#### SECTION 3-4 CHECKUP

- **1.** When is the output of a NAND gate LOW?
- **2.** When is the output of a NAND gate HIGH?
- **3.** Describe the functional differences between a NAND gate and a negative-OR gate. Do they both have the same truth table?
- **4.** Write the output expression for a NAND gate with inputs *A*, *B*, and *C*.

#### 3–5 The NOR Gate

The NOR gate, like the NAND gate, is a useful logic element because it can also be used as a universal gate; that is, NOR gates can be used in combination to perform the AND, OR, and inverter operations. The universal property of the NOR gate will be examined thoroughly in Chapter 5.

After completing this section, you should be able to

- Identify a NOR gate by its distinctive shape symbol or by its rectangular outline symbol
- Describe the operation of a NOR gate
- Develop the truth table for a NOR gate with any number of inputs
- · Produce a timing diagram for a NOR gate with any specified input waveforms
- Write the logic expression for a NOR gate with any number of inputs
- Describe NOR gate operation in terms of its negative-AND equivalent
- Discuss examples of NOR gate applications

The term *NOR* is a contraction of NOT-OR and implies an OR function with an inverted (complemented) output. The standard logic symbol for a 2-input NOR gate and its equivalent OR gate followed by an inverter are shown in Figure 3–34(a). A rectangular outline symbol is shown in part (b).

The NOR is the same as the OR except the output is inverted.



(a) Distinctive shape, 2-input NOR gate and its NOT/OR equivalent

 $A \longrightarrow X$ 

(b) Rectangular outline, 2-input NOR gate with polarity indicator

FIGURE 3-34 Standard NOR gate logic symbols (ANSI/IEEE Std. 91-1984/Std. 91a-1991).

#### Operation of a NOR Gate

A **NOR gate** produces a LOW output when *any* of its inputs is HIGH. Only when all of its inputs are LOW is the output HIGH. For the specific case of a 2-input NOR gate, as shown in Figure 3–34 with the inputs labeled *A* and *B* and the output labeled *X*, the operation can be stated as follows:

For a 2-input NOR gate, output X is LOW when either input A or input B is HIGH, or when both A and B are HIGH; X is HIGH only when both A and B are LOW.



#### MultiSim

**FIGURE 3–35** Operation of a 2-input NOR gate. Open file F03-35 to verify NOR gate operation.

#### TABLE 3-9

Truth table for a 2-input NOR gate.

Inputs		Output
A	B	X
0	0	1
0	1	0
1	0	0
1	1	0

1 = HIGH, 0 = LOW.

operation.

This operation results in an output level opposite that of the OR gate. In a NOR gate, the LOW output is the active or asserted output level as indicated by the bubble on the output. Figure 3–35 illustrates the operation of a 2-input NOR gate for all four possible input combinations, and Table 3–9 is the truth table for a 2-input NOR gate.

#### NOR Gate Operation with Waveform Inputs

The next two examples illustrate the operation of a NOR gate with pulse waveform inputs. Again, as with the other types of gates, we will simply follow the truth table operation to determine the output waveforms in the proper time relationship to the inputs.

#### EXAMPLE 3-15

If the two waveforms shown in Figure 3–36 are applied to a NOR gate, what is the resulting output waveform?



#### FIGURE 3-36

#### Solution

Whenever any input of the NOR gate is HIGH, the output is LOW as shown by the output waveform *X* in the timing diagram.

#### **Related Problem**

Invert input *B* and determine the output waveform in relation to the inputs.

#### EXAMPLE 3-16

Show the output waveform for the 3-input NOR gate in Figure 3–37 with the proper time relation to the inputs.



FIGURE 3-37

#### Solution

The output *X* is LOW when any input is HIGH as shown by the output waveform *X* in the timing diagram.

#### **Related Problem**

With the *B* and *C* inputs inverted, determine the output and show the timing diagram.

#### Negative-AND Equivalent Operation of the NOR Gate

A NOR gate, like the NAND, has another aspect of its operation that is inherent in the way it logically functions. Table 3–9 shows that a HIGH is produced on the gate output only when all of the inputs are LOW. From this viewpoint, a NOR gate can be used for an AND operation that requires all LOW inputs to produce a HIGH output. This aspect of NOR operation is called **negative-AND**. The term *negative* in this context means that the inputs are defined to be in the active or asserted state when LOW.

### For a 2-input NOR gate performing a negative-AND operation, output *X* is HIGH only when both inputs *A* and *B* are LOW.

When a NOR gate is used to detect all LOWs on its inputs rather than one or more HIGHs, it is performing the negative-AND operation and is represented by the standard symbol in Figure 3–38. Remember that the two symbols in Figure 3–38 represent the same physical gate and serve only to distinguish between the two modes of its operation. The following three examples illustrate this.



FIGURE 3–38 Standard symbols representing the two equivalent operations of a NOR gate.

#### EXAMPLE 3-17

A device is needed to indicate when two LOW levels occur simultaneously on its inputs and to produce a HIGH output as an indication. Specify the device.

#### Solution

A 2-input NOR gate operating as a negative-AND gate is required to produce a HIGH output when both inputs are LOW, as shown in Figure 3–39.



#### **Related Problem**

A device is needed to indicate when one or two HIGH levels occur on its inputs and to produce a LOW output as an indication. Specify the device.

#### EXAMPLE 3-18

As part of an aircraft's functional monitoring system, a circuit is required to indicate the status of the landing gears prior to landing. A green LED display turns on if all three gears are properly extended when the "gear down" switch has been activated in preparation for landing. A red LED display turns on if any of the gears fail to extend properly prior to landing. When a landing gear is extended, its sensor produces a LOW voltage. When a landing gear is retracted, its sensor produces a HIGH voltage. Implement a circuit to meet this requirement.

#### Solution

Power is applied to the circuit only when the "gear down" switch is activated. Use a NOR gate for each of the two requirements as shown in Figure 3–40. One NOR gate operates as a negative-AND to detect a LOW from each of the three landing gear sensors. When all three of the gate inputs are LOW, the three landing gears are properly extended and the

resulting HIGH output from the negative-AND gate turns on the green LED display. The other NOR gate operates as a NOR to detect if one or more of the landing gears remain retracted when the "gear down" switch is activated. When one or more of the landing gears remain retracted, the resulting HIGH from the sensor is detected by the NOR gate, which produces a LOW output to turn on the red LED warning display.



## What type of gate should be used to detect if all three landing gears are retracted after takeoff, assuming a LOW output is required to activate an LED display?



When driving a load such as an LED with a logic gate, consult the manufacturer's data sheet for maximum drive capabilities (output current). A regular IC logic gate may not be capable of handling the current required by certain loads such as some LEDs. Logic gates with a buffered output, such as an open-collector (OC) or open-drain (OD) output, are available in many types of IC logic gate configurations. The output current capability of typical IC logic gates is limited to the  $\mu$ A or relatively low mA range. For example, standard TTL can handle output currents up to 16 mA but only when the output is LOW. Most LEDs require currents in the range of about 10 mA to 50 mA.

#### EXAMPLE 3-19





#### Solution

Any time all of the input waveforms are LOW, the output is HIGH as shown by output waveform *X* in the timing diagram.

#### **Related Problem**

Determine the output with input *D* inverted and show the timing diagram.

#### Logic Expressions for a NOR Gate

The Boolean expression for the output of a 2-input NOR gate can be written as

 $X = \overline{A + B}$ 

This equation says that the two input variables are first ORed and then complemented, as indicated by the bar over the OR expression. Evaluating this expression, you get the results shown in Table 3–10. The NOR expression can be extended to more than two input variables by including additional letters to represent the other variables.

#### SECTION 3-5 CHECKUP

- 1. When is the output of a NOR gate HIGH?
- **2.** When is the output of a NOR gate LOW?
- **3.** Describe the functional difference between a NOR gate and a negative-AND gate. Do they both have the same truth table?
- 4. Write the output expression for a 3-input NOR with input variables *A*, *B*, and *C*.

#### **3–6** The Exclusive-OR and Exclusive-NOR Gates

Exclusive-OR and exclusive-NOR gates are formed by a combination of other gates already discussed, as you will see in Chapter 5. However, because of their fundamental importance in many applications, these gates are often treated as basic logic elements with their own unique symbols.

After completing this section, you should be able to

- Identify the exclusive-OR and exclusive-NOR gates by their distinctive shape symbols or by their rectangular outline symbols
- Describe the operations of exclusive-OR and exclusive-NOR gates
- Show the truth tables for exclusive-OR and exclusive-NOR gates
- Produce a timing diagram for an exclusive-OR or exclusive-NOR gate with any specified input waveforms
- Discuss examples of exclusive-OR and exclusive-NOR gate applications

#### The Exclusive-OR Gate

Standard symbols for an exclusive-OR (XOR for short) gate are shown in Figure 3–42. The XOR gate has only two inputs. The **exclusive-OR gate** performs modulo-2 addition (introduced in Chapter 2). The output of an exclusive-OR gate is HIGH *only* when the two

TABLE 3-10		
A	B	$\overline{A + B} = X$
0	0	$\overline{0+0} = \overline{0} = 1$
0	1	$\overline{0+1} = \overline{1} = 0$
1	0	$\overline{1+0} = \overline{1} = 0$
1	1	$\overline{1+1} = \overline{1} = 0$

#### InfoNote

Exclusive-OR gates connected to form an adder circuit allow a processor to perform addition, subtraction, multiplication, and division in its Arithmetic Logic Unit (ALU). An exclusive-OR gate combines basic AND, OR, and NOT logic. For an exclusive-OR gate, opposite inputs make the output HIGH.



FIGURE 3-42 Standard logic symbols for the exclusive-OR gate.

#### **TABLE 3–11**

Truth table for an exclusive-OR gate.

Inputs		Output
A	B	X
0	0	0
0	1	1
1	0	1
1	1	0

inputs are at opposite logic levels. This operation can be stated as follows with reference to inputs *A* and *B* and output *X*:

# For an exclusive-OR gate, output *X* is HIGH when input *A* is LOW and input *B* is HIGH, or when input *A* is HIGH and input *B* is LOW; *X* is LOW when *A* and *B* are both HIGH or both LOW.

The four possible input combinations and the resulting outputs for an XOR gate are illustrated in Figure 3–43. The HIGH level is the active or asserted output level and occurs only when the inputs are at opposite levels. The operation of an XOR gate is summarized in the truth table shown in Table 3–11.



#### MultiSim

**FIGURE 3-43** All possible logic levels for an exclusive-OR gate. Open file F03-43 to verify XOR gate operation.

#### EXAMPLE 3-20

A certain system contains two identical circuits operating in parallel. As long as both are operating properly, the outputs of both circuits are always the same. If one of the circuits fails, the outputs will be at opposite levels at some time. Devise a way to monitor and detect that a failure has occurred in one of the circuits.

#### **Solution**

The outputs of the circuits are connected to the inputs of an XOR gate as shown in Figure 3–44. A failure in either one of the circuits produces differing outputs, which cause the XOR inputs to be at opposite levels. This condition produces a HIGH on the output of the XOR gate, indicating a failure in one of the circuits.



#### FIGURE 3-44

#### **Related Problem**

Will the exclusive-OR gate always detect simultaneous failures in both circuits of Figure 3–44? If not, under what condition?

#### The Exclusive-NOR Gate

Standard symbols for an **exclusive-NOR** (XNOR) **gate** are shown in Figure 3–45. Like the XOR gate, an XNOR has only two inputs. The bubble on the output of the XNOR symbol indicates that its output is opposite that of the XOR gate. When the two input logic levels are opposite, the output of the exclusive-NOR gate is LOW. The operation can be stated as follows (*A* and *B* are inputs, *X* is the output):

For an exclusive-NOR gate, output X is LOW when input A is LOW and input B is HIGH, or when A is HIGH and B is LOW; X is HIGH when A and B are both HIGH or both LOW.





The four possible input combinations and the resulting outputs for an XNOR gate are shown in Figure 3–46. The operation of an XNOR gate is summarized in Table 3–12. Notice that the output is HIGH when the same level is on both inputs.



**FIGURE 3-46** All possible logic levels for an exclusive-NOR gate. Open file F03-46 to verify XNOR gate operation.

#### **TABLE 3-12**

Truth table for an exclusive-NOR gate.

Inputs		Output
A	В	X
0	0	1
0	1	0
1	0	0
1	1	1

#### MultiSim

#### **Operation with Waveform Inputs**

As we have done with the other gates, let's examine the operation of XOR and XNOR gates with pulse waveform inputs. As before, we apply the truth table operation during each distinct time interval of the pulse waveform inputs, as illustrated in Figure 3–47 for an XOR gate. You can see that the input waveforms *A* and *B* are at opposite levels during time intervals  $t_2$  and  $t_4$ . Therefore, the output *X* is HIGH during these two times. Since both inputs are at the same level, either both HIGH or both LOW, during time intervals  $t_1$  and  $t_3$ , the output is LOW during those times as shown in the timing diagram.





#### EXAMPLE 3-21

Determine the output waveforms for the XOR gate and for the XNOR gate, given the input waveforms, A and B, in Figure 3–48.



#### FIGURE 3-48

#### Solution

The output waveforms are shown in Figure 3–48. Notice that the XOR output is HIGH only when both inputs are at opposite levels. Notice that the XNOR output is HIGH only when both inputs are the same.

#### **Related Problem**

Determine the output waveforms if the two input waveforms, A and B, are inverted.

#### An Application

An exclusive-OR gate can be used as a two-bit modulo-2 adder. Recall from Chapter 2 that the basic rules for binary addition are as follows: 0 + 0 = 0, 0 + 1 = 1, 1 + 0 = 1, and 1 + 1 = 10. An examination of the truth table for an XOR gate shows that its output is the binary sum of the two input bits. In the case where the inputs are both 1s, the output is the sum 0, but you lose the carry of 1. In Chapter 6 you will see how XOR gates are combined to make complete adding circuits. Table 3–13 illustrates an XOR gate used as a modulo-2 adder. It is used in CRC systems to implement the division process that was described in Chapter 2.

TABLE 3-13				
An XOR gate used to add two bits.				
Input Bits		Output (Sum)		
A	В	Σ		
0	0	0		
0	1	1		
1	0	1		
1	1	0 (without		
	)]	the 1 carry bit)		