

Program: BS (CS-SE-EE)

Total Marks: 30

Time Allowed: 6 days

Note: Attempt all Questions:

Q 1: a) Define differential equation along with 2 examples? **(1+1 Marks)**

b) Define a Separable Differential Equation (DE)? **(1+4+3 Marks)**

- i. Solve the following **Initial Value Problem (IVP)** using **separable DE** and find the interval of validity of the solution.

$$(a) \quad y' = \frac{xy^3}{\sqrt{1+x^2}} \quad y(0) = -1$$

$$(b) \quad y' = e^{-y} (2x - 4) \quad y(5) = 0$$

Q 2: a) Solve the following IVP using Linear Differential method **(2+5+3 Marks)**

(i) Explain the steps for solving Linear Differential Equation.

(ii) $\cos(x)y' + \sin(x)y = 2\cos^3(x)\sin(x) - 1 \quad y\left[\frac{\pi}{4}\right] = 3\sqrt{2}, \quad 0 \leq x \leq \frac{\pi}{2}$

(iii) $x' + 2x = \sin t$

Q 3: Solve the following IVP for the exact equation and find the interval of validity for the solution. **(5+5 Marks)**

(i) $2xy - 9x^2 + (2y + x^2 + 1)\frac{dy}{dx} = 0, \quad y(0) = -3$

(ii) $\frac{2ty}{t^2+1} - 2t - (2 - \ln(t^2 + 1))y' = 0 \quad y(5) = 0$