

$$\int_0^{\pi} \cos^{2n+1} x \, dx = \int_0^{\pi/2} \cos^{2n+1} x \, dx + \int_{\pi/2}^{\pi} \cos^{2n+1} (\pi-x) \, dx$$

$$= \int_0^{\pi/2} \cos^{2n+1} x \, dx + \int_0^{\pi/2} (-\cos x)^{2n+1} \, dx$$

$$= \int_0^{\pi/2} \cos^{2n+1} x \, dx - \int_0^{\pi/2} \cos^{2n+1} x \, dx$$

$$= 0 \quad \left( -(\cos x)^{2n+1} = -\cos^{2n+1} x \right)$$

Q1\* - Evaluate  $\int_{-1}^3 (x^3 + 3x^2) \, dx$

$$\int_{-1}^3 x^3 \, dx + \int_{-1}^3 3x^2 \, dx$$

$$= \left[ \frac{x^4}{4} \right]_{-1}^3 + \left[ x^3 \right]_{-1}^3 = (3)^4$$

$$= \left[ \frac{(3)^4}{4} - \frac{(-1)^4}{4} \right] + \left[ (3)^3 - (-1)^3 \right]$$

$$= \left[ \frac{81}{4} - \frac{1}{4} \right] + [27 - (-1)]$$

$$= \frac{80}{4} + (27+1)$$

Q2\*  $= 20 + 28 = 48$

Q2\*  $\int \frac{x^2 + 1}{x+1} \, dx = \int \frac{x^2 - 1 + 2}{x+1} \, dx$