

Division:  $(2, 6) \div (3, 7)$   $\frac{2+6i}{3+7i} \times \frac{3-7i}{3-7i}$  (2)

$$\frac{(2+6i)(3-7i)}{(3)^2 - (7i)^2} = \frac{(2)(3) + (2)(-7i) + (6i)(3) + (6i)(-7i)}{9 - (-49)}$$

$$= \frac{6 - 14i + 18i + 42i^2}{9 + 49} = \frac{36 + 4i}{58}$$

$a^2 - b^2 = (a+b)(a-b)$  (411)

Multiplicative Inverse: M.I is  $(1, 0)$

1) Multiplicative inverse of  $(a, b)$  is  $\left(\frac{a}{a^2+b^2}, \frac{-b}{a^2+b^2}\right)$

2) Additive identity is  $(0, 0)$ , Additive inverse of Every complex number  $(a, b)$  is  $(-a, -b)$   $\left\{[(a, b) + (-a, -b)] = (0, 0)\right\}$

b) Find multiplicative inverse  $(-4, 7)$

$$\left(\frac{a}{a^2+b^2}, \frac{-b}{a^2+b^2}\right) = \left(\frac{-4}{(-4)^2+(7)^2}, \frac{-7}{(-4)^2+(7)^2}\right) = \left(\frac{-4}{16+49}, \frac{-7}{16+49}\right)$$

$$= \left(\frac{-4}{65}, \frac{-7}{65}\right)$$

Additive inverse:  $(-4, 7) = (4, -7)$  ✓

Questions: i)  $(\sqrt{2}, -\sqrt{5})$  (ii)  $(1, 0)$  (iii)  $-3-5i$  (iv)  $(1, 2)$

$$a^2 + 4b^2 = (a)^2 + (2b)^2 + 4ab - 4ab = (a+2b)^2 - 4ab$$

Question: separate into real and imaginary parts (write as a simple complex number).

Solution:  $\frac{2-7i}{4+5i} \times \frac{4-5i}{4-5i} = \frac{(2)(4) + 2(-5i) - (7i)(4) + (-7i)(-5i)}{(4)^2 - (5i)^2}$

$$\frac{2-7i}{4+5i} = \frac{8 - 10i - 28i - 35}{16 + 25} = \frac{-27 - 38i}{41} = \frac{-27}{41} - \frac{38i}{41}$$

Questions: (i)  $(-2+3i)$  (ii)  $\frac{1}{i}$