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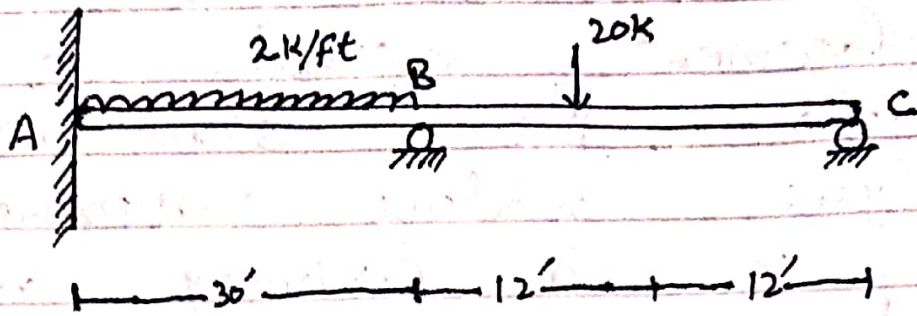
ID 7764

Sec A

Subject Structure II

Date 21/8/2020

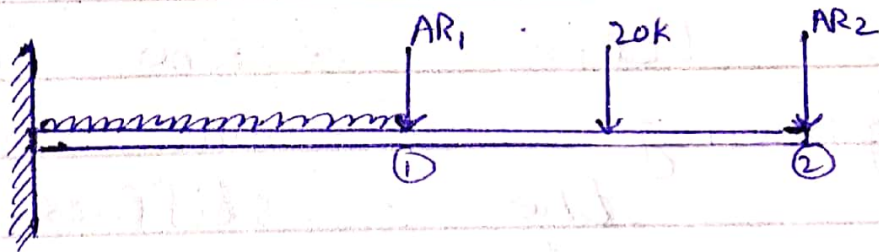
Q1.



Solution:-

Structure Indeterminacy = 2°

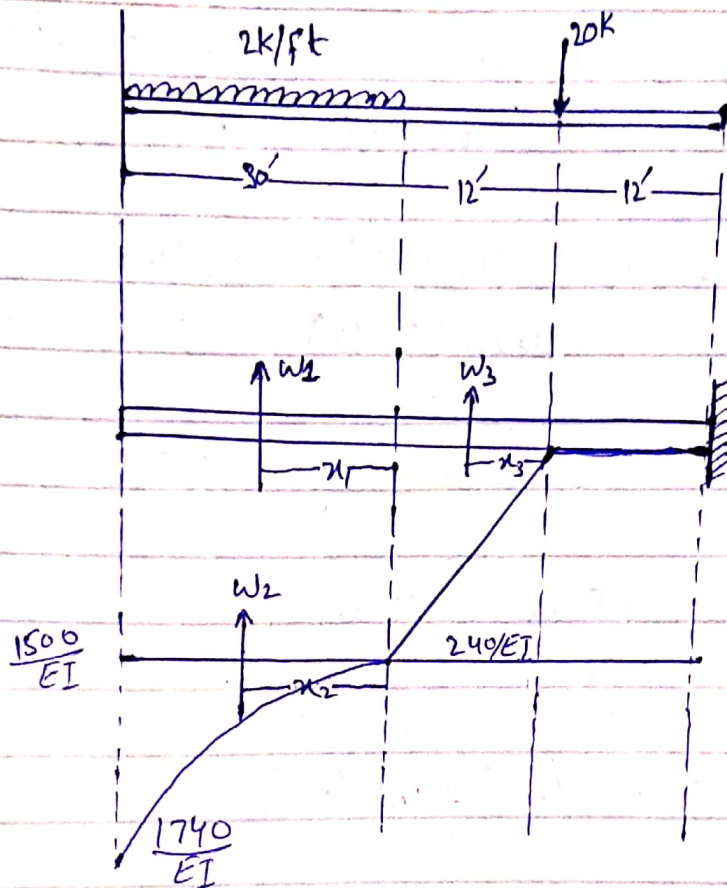
Step # 1. Select Redundant Action



$$\begin{bmatrix} DRS_1 \\ DRS_2 \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \end{bmatrix}, \quad \begin{bmatrix} AR_1 \\ AR_2 \end{bmatrix} = \begin{bmatrix} ? \\ ? \end{bmatrix}$$

$$[DRS] = [DRL] + [F] \times [AR]$$

Step#2 Compute the values of [DRL]



$$20 \times 12 = 240$$

$$20 \times (12 + 30) +$$

$$2 \times 30 \times 15 = 1740$$

$$W_1 = 1500 \times 30 = 45000$$

$$W_2 = \frac{1}{3} \times 30 \times 240 = 2400$$

$$W_3 = \frac{1}{2} \times 12 \times 240 = 1440$$

$$x_1 = \frac{b}{2} = \frac{30}{2} = 15'$$

$$x_2 = \frac{3}{n+2} \times l = \frac{3}{2+2} \times 30 = 22.5'$$

$$x_3 = \frac{2}{3} \times L = \frac{2}{3} \times 12 = 8'$$

Now Finding DRL:-

$$DRL_2 = W_1 \times (x_1 + 24) + W_2 \times (x_2 + 24) + W_3 \times (x_3 + 12)$$

$$= 45000(15 + 24) + 2400(22.5 + 24) + 1440(8 + 12)$$

$$= 1755000 + 111600 + 28800$$

$$DRL_2 = 1895400/EI$$

$$DRL_1 = W_1(x_1) + W_2(x_2)$$

$$= 45000(15) + 2400(22.5)$$

$$= 675000 + 54000$$

$$= 729000$$

So,

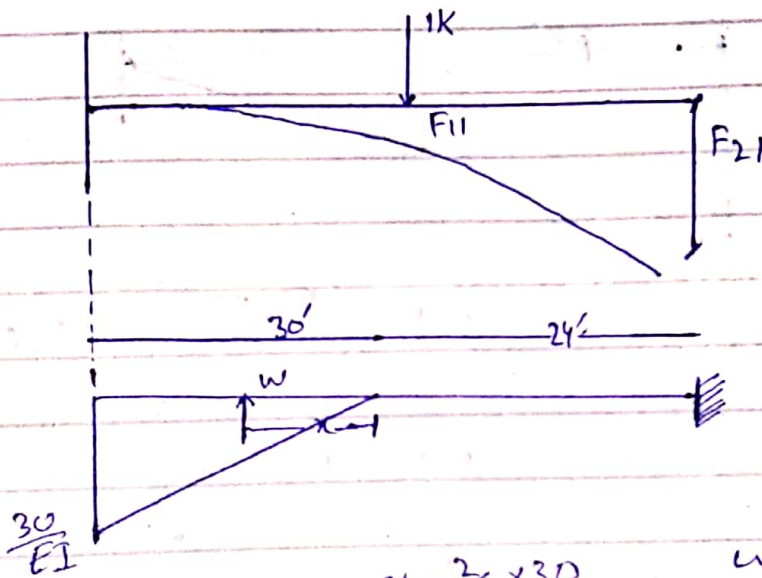
$$DRL = \frac{1}{EI} \left[ \frac{729000}{1895400} \right]$$



### Step 3. Flexibility Matrix

$$[F]_{2 \times 2} = \begin{bmatrix} F_{11} & F_{12} \\ F_{21} & F_{22} \end{bmatrix}$$

a) Applying unit load on  $AR_1$



$$n = \frac{2}{3} \times 30$$

$$n = 20$$

$$w = \frac{1}{2} \left( \frac{30}{EI} \times 30 \right)$$

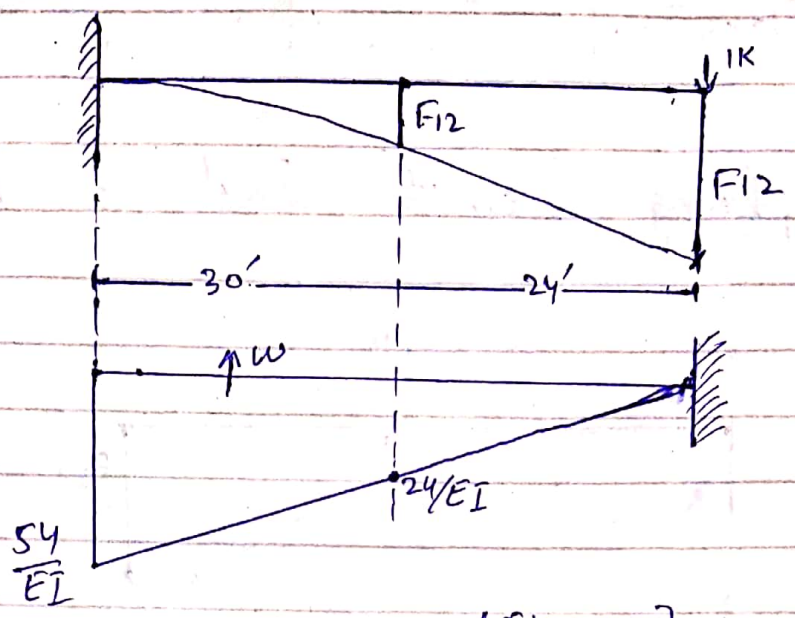
$$w = 450/EI$$

So,

$$F_{11} = \frac{450}{EI} (20) = 9000/EI$$

$$F_{21} = \frac{450}{EI} (20 + 24) = 19800/EI$$

Now Apply unit load on AR<sub>2</sub>.



$$W = \left( \frac{54 + 24}{EI} \right) \times 30$$

$$W = 1170/EI$$

Now the distance,

$$x = \frac{L}{3} \left[ \frac{b + 2(a)}{a + b} \right]$$

$$= \frac{30}{3} \left[ \frac{24 + 2(54)}{54 + 24} \right] = 16.92'$$

$$\Rightarrow F_{12} = \frac{1170}{EI} \times 16.92 = \frac{19796.4}{EI}$$

$$\Rightarrow F_{22} = \frac{1170}{EI} \times (16.92 + 24) = \frac{47876.4}{EI}$$

Hence

$$F_{2 \times 2} = \begin{bmatrix} 9000 & 19796.4 \\ 19800 & 47876.4 \end{bmatrix} \frac{1}{EI}$$

Step #4:-

Compute the values of AR

$$[DRS] = [DRL] + [F] \times [AR]$$

$$[AR] = [DRS - DRL] \times [F]^{-1}$$

$$[F]^{-1} = \frac{1}{|F|} \times \text{Adj } F$$

$$= \frac{1}{\begin{vmatrix} 9000 & 19796.4 \\ 19800 & 47876.4 \end{vmatrix}} \times \text{Adj} \begin{bmatrix} 9000 & 19796.4 \\ 19800 & 47876.4 \end{bmatrix}$$

$$|F| = (9000 \times 47876.4 - 19796.4 \times 19800)$$

$$= (430887600 - 391968780)$$

$$\Rightarrow |F| = 38918880$$

$$\Rightarrow \text{Adj } A = \begin{bmatrix} 47876.4 & -19796.4 \\ -19800 & 9000 \end{bmatrix}$$



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$$\begin{bmatrix} AR_1 \\ AR_2 \end{bmatrix} = \begin{bmatrix} 0 - 729000 \\ 0 - 1895400 \end{bmatrix} \frac{1}{EI} \times \frac{1}{38918880} \begin{bmatrix} 47876.4 & -19796.4 \\ -19800 & 9000 \end{bmatrix}$$

$$\begin{bmatrix} 47876.4 & -19796.4 \\ -19800 & 9000 \end{bmatrix}$$

$$= \begin{bmatrix} -729000 \\ -1895400 \end{bmatrix} \frac{1}{EI} \times \frac{1}{38918880} \begin{bmatrix} 47876.4 & -19796.4 \\ -19800 & 9000 \end{bmatrix}$$

$$\boxed{\begin{bmatrix} AR_1 \\ AR_2 \end{bmatrix} = \begin{bmatrix} 66.193 \\ -67.505 \end{bmatrix}}$$



Q. 2.

Force Method	Displacement Method.
→ $D_s < D_k$	→ $D_s > D_k$
→ Force and redundant are unknowns	→ Displacement and redundant are unknowns
→ Starts with equilibrium of forces.	→ Starts with compatible deformation
→ Forces found by compatibility of displacements.	→ Displacement found by equilibrium of forces.
→ no. of redundant = $D_s$	→ no. of redundant = $D_k$
→ Not suitable for compatibility.	→ Not suitable for stresses.

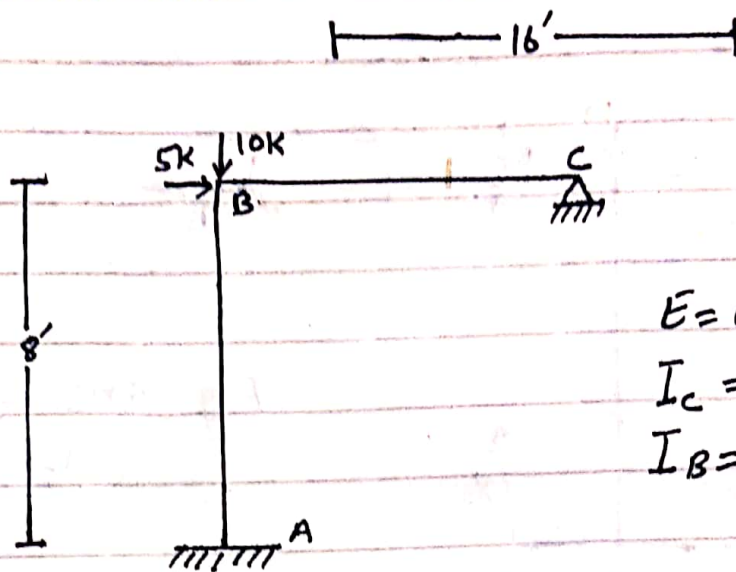
## Stiffness Method:-

It is called displacement method is more suitable for structure analysis matrix approach, as it is a primary method used in matrix analysis.

The main advantage of this method over flexibility method is that it is conducive to computer programming. Once the analytical model of the structure has been defined, no further engineering decisions are required in the stiffness method in order to carry out the analysis.



## Q3. Problem.



$$E = \text{constant}$$

$$I_c = I$$

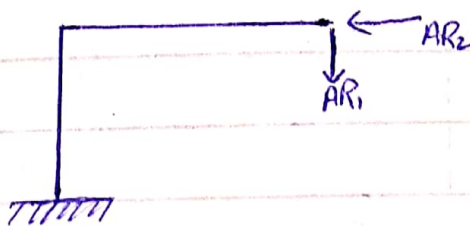
$$I_B = 2I$$

Solution:-

Total statical indeterminate

$$\Rightarrow R - 3 = 5 - 3 = 2$$

Step #1. Identify Redundant action



$$\begin{bmatrix} AR_1 \\ AR_2 \end{bmatrix} = \begin{bmatrix} ? \\ ? \end{bmatrix}, \quad \begin{bmatrix} DRS_1 \\ DRS_2 \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \end{bmatrix}$$

Step #2. Compute value of [DRL]



Step #2. Compute value of [DRU]

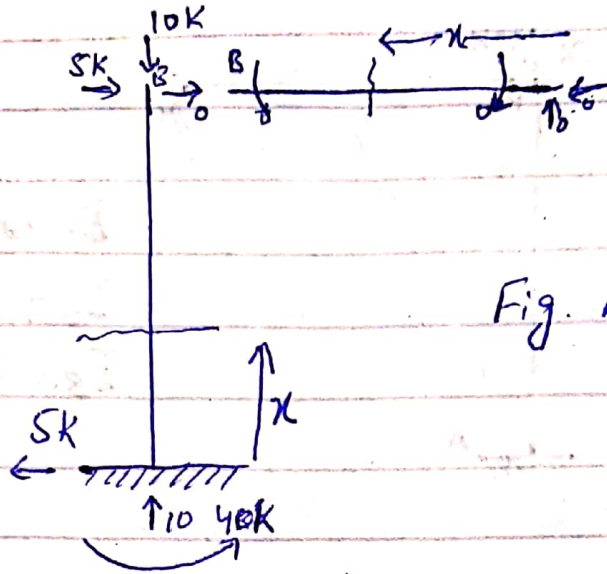


Fig. AML values (M-values)

Step #3. [F] or [AMR]

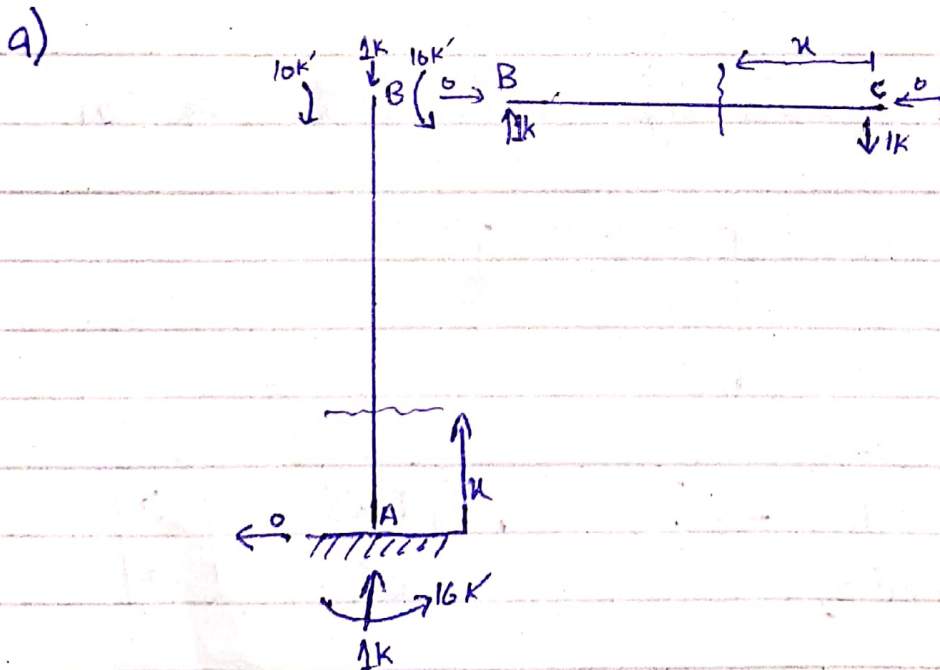


Fig. AMR-value (m<sub>1</sub> values)

b)

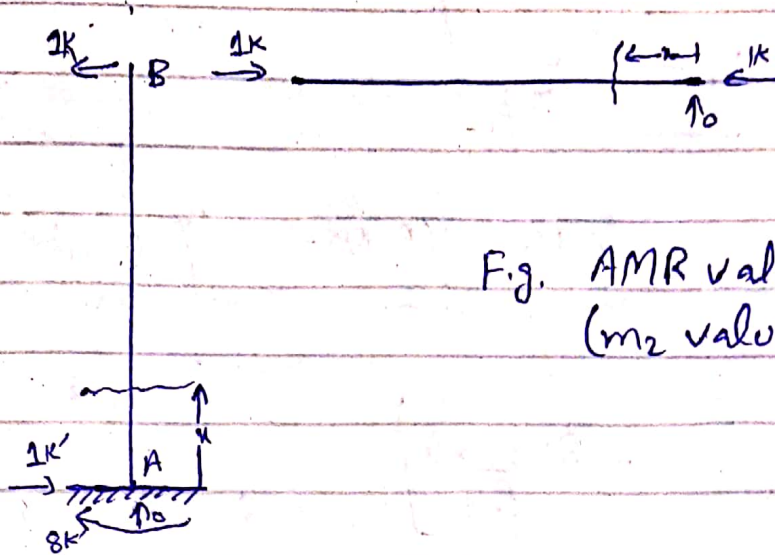


Fig. AMR values  
( $m_2$  values)

Member	AB	BC
select origin (should be selected the support)	A	C
Limits	0-8	0-16
I	I	I
Take $x$ -section from origin Find moment	$8x-40$	0
$m_1$	-16	0
$m_2$	$8-x$	0

→ For Finding value of DRL:-

$$DRL_1 = \int_0^8 \frac{M_{AB} \cdot m_1(AB)}{EI} dx + \int_0^{16} \frac{M_{BC} \cdot m_2(BC)}{EI} dx$$

$$= \int_0^8 \frac{(8x-40)(-16)dx}{EI} + \int_0^{16} \frac{0 \cdot x dx}{E(2I)}$$

$$\boxed{DRL_1 = \frac{2560}{EI}}$$

$$DRL_2 = \int_0^8 \frac{(5n-40)(8-x)dx}{EI} + \int_8^{16} \frac{0.0 dx}{E(2I)}$$

$$\boxed{DRL_2 = -\frac{853.33}{EI}}$$

⇒ Compute Flexibility Matrix:-

$$F_{2 \times 2} = \begin{bmatrix} F_{11} & F_{12} \\ F_{21} & F_{22} \end{bmatrix}$$

$$\begin{aligned} \Rightarrow F_{11} &= \int_0^8 \frac{m_1^2(AB)}{EI} + \int_0^{16} \frac{m_1^2(BC)}{EI} \\ &= \int_0^8 \frac{(-16)^2 dx}{EI} + \int_0^{16} \frac{x^2}{E(2I)} \end{aligned}$$

$$F_{11} = \frac{2730.67}{EI}$$

$$\begin{aligned} F_{12} - F_{21} &= \int_0^8 m_1(AB) \cdot m_2(AB) + \int_0^{16} m_1(BC) \cdot m_2(BC) \\ &= \int_0^8 \frac{(-16)(8-x) dx}{EI} + \int_0^{16} \frac{(x)(0)}{2EI} dx \end{aligned}$$

$$\boxed{F_{12} - F_{21} = -\frac{512}{EI}}$$



$$F_{gg} = \int_0^8 (m_2)^2_{AB} dx + \int_0^{16} (m_2)^2_{BC} dx$$

$$= \int_0^8 \frac{(8-x)^2}{EI} dx + \int_0^{16} \frac{0^2}{2EI} dx$$

$$F_{gg} = 170.67$$

As we know that

$$[DRS] = [DRL] + [AR] \times [F]$$

$$\Rightarrow [AR] = \frac{[DRS] - [DRL]}{[F]}$$

$$\Rightarrow [AR] = [F]^{-1} \times [DRS - DRL]$$

$$= \begin{bmatrix} 2730.67 & -512 \\ -512 & 170.67 \end{bmatrix} \times \begin{bmatrix} 0 - 2560 \\ 0 + 853.33 \end{bmatrix}$$

$$\begin{bmatrix} AR_1 \\ AR_2 \end{bmatrix} = \begin{bmatrix} -0.00005 \\ 4.997 \end{bmatrix} = \begin{bmatrix} 0 \\ 5 \end{bmatrix}$$