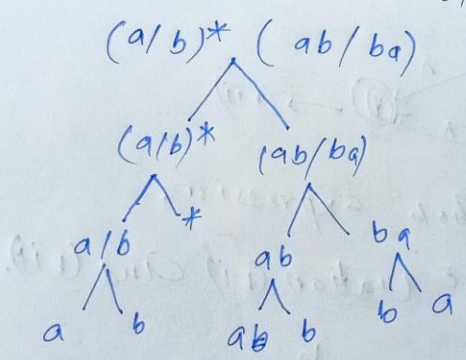


NAME. M. NAEEM.
 ID # 14146
 Subject Theory of Automata.

Q1: Parse The Given PE into its Individuals OR Atomic Symbols and Then design an NFA? $(a/b)^*(ab/ba)$.

Ans:



=> NFA For a as;
 $\rightarrow (i) \xrightarrow{a} (ii) \rightarrow (i)$

=> NFA For b as;
 $\rightarrow (i) \xrightarrow{b} (ii) \rightarrow (i)$

=> NFA For ab as;
 Now combining eq (i) and eq (ii).

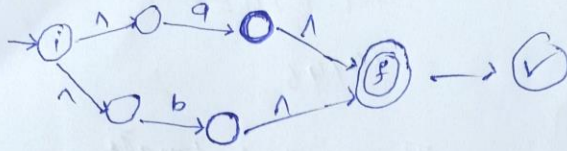
$\rightarrow (i) \xrightarrow{a} (ii) \xrightarrow{b} (iii)$

=> NFA For ba as;
 $\rightarrow (i) \xrightarrow{b} (ii) \xrightarrow{a} (iii)$

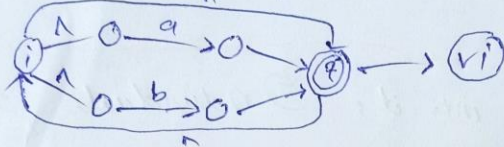
Pto

⇒ Now NFA for ab ;

(2)

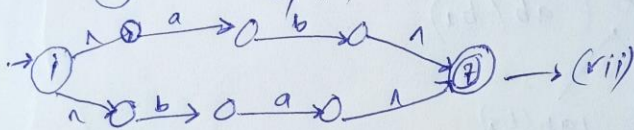


⇒ Now NFA for $(a/b)^*$



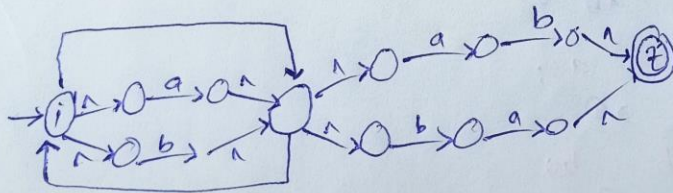
⇒ NFA for (ab/ba)

Combining (iii) Eq (iv)



⇒ NFA for whole expression.

By combining equation (vi) and (vii).



⇒ This is

the final

NFA for the

Given

Expression

$(a/b)^* (ab/ba)$

Q2: Design RE for each of the following. (3)

Ans: (i) RE for all the optional words over $\{a, b\}$.

Ans: $(a|b)^*$

(ii) RE for all the optional words over $\{a, b\}$ with an Even Number of "a".

Ans: $b^* (a b^* a)^+ b^*$

(iii) RE for all the optional words over $\{a, b\}$ with in Odd Number of 'a'.

Ans: $b^* a (b^* a b^* a b^*)^*$

(iv) RE for all the optional words over $\{a, b\}$ where Last Symbol must be "b".

Ans: $(a+b)^+ b$

(v) RE for all optional words over $\{a, b\}$ where First Symbol must be "b".

Ans: $b (a+b)^*$

Q3: A): prove that $(a|b)^* \neq a^* b^*$

4

Ans: $(a|b)^*$

$$(a|b)^0 = 1$$

$$(a|b)^1 = a \text{ or } b, a, b.$$

$$(a|b)^2 = \{aa, ab, ba, bb\}$$

$$(a|b)^* = \{1, a, b, aa, ab, \dots\}$$

$$a^* b^*$$

$$a^0 b^0 = 1$$

$$a^1 b^1 = ab$$

$$a^* b^* = \{1, a, ab, b, b^2, \dots\}$$

Hence it is prove that $(a|b)^*$ is Not Equal to $a^* b^*$.

B): Q3: (i) $(a|b)(a|b)b(a|b)^*$

Ans: Language for words over $\{a, b\}$ which starts with "aa" or "ab" or "ba" or "bb" followed by b and ends with any letter.

(ii) $(a|b)^* b (a|b) (a|b)$

Ans: The language $L = \{a, b\}$ where strings starts with any letter followed by "b" and ends with "aa" or "ab" or "ba" or "bb".

(iii) $(a|b)^* (aa|bb)$

Ans: Language $L = \{a, b\}$ where last symbol must be two 'aa' or two b's. ~~the~~ string must end with "aa" or "bb".

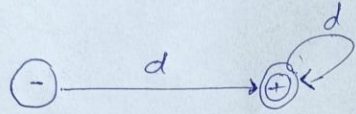
(iv) $(aa|bb)(a|b)^*$

Ans: Language $L = \{a, b\}$ where first symbol must be aa or bb string must start with "aa" or "bb".

Q4: Design NFA For The following without parsing? (5)

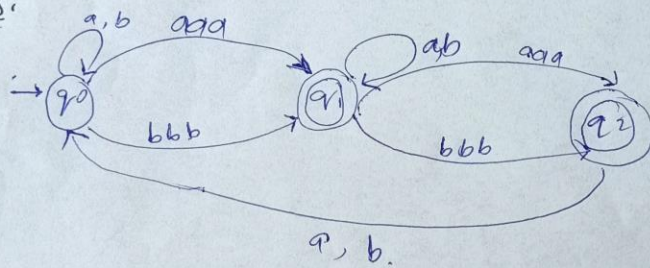
(i) $(+/-)d^+$ (ii) $(a/b)^*(aaa/bbb)(a/b)^*$

Ans:



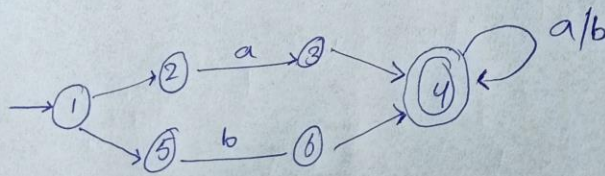
(ii): $(a/b)^*(aaa/bbb)(a/b)^*$

Ans:



(ii) $(a/b)^*(aaa/bbb)(a/b)^*$

Ans:



{ aaa, bbb, aaaa bb aaa bbb ... }