

NAME

ADNAN

ID

13507

Q1.

Solution.

where $s = \{ (1,1), (1,2), (1,3), (1,4), (1,5), (1,6), (1,7), (1,8),$
 $(2,1), (2,2), (2,3), (2,4), (2,5), (2,6), (2,7), (2,8)$
 $(3,1), (3,2), (3,3), (3,4), (3,5), (3,6), (3,7), (3,8),$
 $(4,1), (4,2), (4,3), (4,4), (4,5), (4,6), (4,7), (4,8),$
 $(5,1), (5,2), (5,3), (5,4), (5,5), (5,6), (5,7), (5,8),$
 $(6,1), (6,2), (6,3), (6,4), (6,5), (6,6), (6,7), (6,8),$
 $(7,1), (7,2), (7,3), (7,4), (7,5), (7,6), (7,7), (7,8),$
 $(8,1), (8,2), (8,3), (8,4), (8,5), (8,6), (8,7), (8,8)\}.$

Let $A = \{ \text{the sum is 7} \}$, $B = \{ \text{the sum is even} \}$, $c = \{ \text{the sum is greater than 8} \}$ and $D = \{ \text{the two dice had the same outcomes} \}$. Then

$A = \{ (1,6), (2,5), (3,4), (4,3), (5,2), (6,1), (4,3) \}$,

$B =$

$\{ (1,1), (1,3), (1,5), (2,2), (1,7), (2,2), (2,4), (2,6), (2,8), (3,1), (3,3), (3,5), (3,7), (4,2), (4,4), (4,6), (4,8), (5,1), (5,3), (5,5), (5,7), (6,2), (6,4), (6,6), (6,8), (7,1), (7,3), (7,5), (7,7), (8,2), (8,4), (8,6), (8,8) \}$.

C =

{(1,8),(2,7),(2,8),(3,6),(3,7),(3,8),(4,5),(4,6),(4,7),(4,8),(5,4),(5,5),(5,6),(5,7),(5,8),(6,3),(6,4),(6,5),(6,6),(6,7),(6,8),(7,2),(7,3),(7,4),(7,5),(7,6),(7,7),(7,8),(8,1),(8,2),(8,3),(8,5),(8,6),(8,7),(8,8)}

D = { (1,1),(2,2),(3,3),(4,4),(5,5),(6,6),(7,7),(8,8)}.

$$A \cap B = \{\}$$

$$A \cap C = \{\}$$

$$A \cap D = \{\}$$

$$P(A) = 6/64 \text{ , } P(B) = 32/64$$

$$P(C) = 36/64 \text{ , } P(D) = 8/64$$

$$P(A \cap B) = 0 \text{ , } P(A \cap C) = 0 \text{ , } P(A \cap D) = 0$$

Hence

$$P(A/B) = P(A \cap B) / P(B) = 0 * 32/64$$

$$P(A/B) = 0.$$

$$P(A/C) = P(A \cap C) / P(C) = 0 * 36/64$$

$$P(A/C) = 0.$$

$$P(A/D) = PA \cap D / P(D) = 0 * 8/64$$

$$P(A/D) = 0.$$

ANS.

Q2.

SOLUTION.

Now we find

P(sum greater than 7)

P(sum less than 7)

P(sum Exactly equal to 7)

1	1	2	3	4	5	6
2	2	3	4	5	6	7
3	3	4	5	6	7	8
4	4	5	6	7	8	9
5	5	6	7	8	9	10
6	6	7	8	9	10	11
7	7	8	9	10	11	12

Total sum = 6/36=1/6

Favrrable outcomes/possible outcomes

$$P(\text{sum greater than } 7) = 15/36$$

$$P(\text{sum less than } 7) = 10/36 = 5/18$$

$$P(\text{sum Exactly equal to } 7) = 6/36 = 1/6 \text{ ANS.}$$

Q3.

Solution.

Given that $p = 2/3$ $n = 8$

- $q = 1 - p$
- put values in q
- $= 1 - 2/3$
- $Q = 1/3$

Now find x denotes the number of games won by A then

$$(1) \quad P(x=4)$$

$$(8) \quad \binom{8}{4} \left(\frac{2}{3}\right)^4 \left(\frac{1}{3}\right)^4$$

$$4$$

$$= \frac{1120}{8561}$$

$$= 0.1707$$

$$(2) \quad (p \ x > - 4)$$

- $1 - (x < 4)$

$$\begin{aligned}
& \bullet = 1 - \sum_{X=0}^3 (8/x)(2/3)^x(1/3)^{8-x} \\
& X=0 \\
& = 1 - [(1/3)^8 + 8(2/3)(1/3)^7 + 28(2/3)^2(1/3)^6 + 56(2/3)^3(1/3)^5] \\
& = 1 - 1/6561 [1 + 16 + 112 + 448] \\
& = 1 - 577/6561 \\
& = 6561 - 577/6561 \\
& = 5984/6561 \\
& \mathbf{0.9121}
\end{aligned}$$

(3)

$$\begin{aligned}
& P(3 < -x < -6) \\
& \Sigma \\
& X=3 (8) (2/3)^x(1/3)^{8-x} \\
& X
\end{aligned}$$

$$\begin{aligned}
& = (8/3)(2/3)^3(1/3)^5 + (8/4)(2/3)^4(1/3)^4 + (8/5)(2/3)^5(1/3)^3 + (8/6)(2/3)^6(1/3)^2 \\
& = 8/3^8 [56 + 140 + 224 + 224] \\
& = 8 * 664/6561 = 5152/6561 = \mathbf{0.7852} \text{ ANS.}
\end{aligned}$$

Q5.

ANS.

Derive Binomial distribution:

A **binomial distribution** can be thought of as simply the probability of a SUCCESS or FAILURE outcome in an experiment or survey that is repeated multiple times. The **binomial** is a type of **distribution** that has two possible outcomes.

Now we find mean and variance of binomial distribution.

Mean

$$n = 5$$

$$p = 60$$

$$q = 40$$

we know that mean formula

$$\mu_x = np$$

put values in Mean formula

$$= 5(60)$$

$$\mu_x = 300$$

now find variance of the above mean value

$$\mu_x = np$$

put values

$$= 5(60)$$

$$= 300$$

variance formula

$$\mu_x^2 = npq$$

put values

$$= 5(60)(40)$$

$$\mu_x^2 = 12000$$

now taking variance square

$$\mu_x = \sqrt{npq}$$

$$= \sqrt{12000}$$

$$\mu_x = 109.5445$$

ANS.

Q6.

ANS.

Differentiate between Bi-nominal frequency distribution and Bi-nominal distribution:

Bi-nominal frequency distribution

- If the binominal probability distribution is multiplied by N the numbers of experiments or sets.
- The resulting distribution is known as binominal frequency distribution.
- X is numbers of success and N is a numbers of experiments.
- Formula
- $N \binom{n}{x} p^x q^{n-x}$

Bi-nominal distribution:

- Binomial distribution summarizes the number of trials, or observations when each trial has the same probability of attaining one particular value. ...

- When $p = 0.5$, the **distribution** is symmetric around the mean. When $p > 0.5$, the **distribution** is skewed to the left. When $p < 0.5$, the **distribution** is skewed to the right.

Formula

$$\mu_x = np$$

$$\mu_x^2 = npq$$

Q7.

PROBLEM SOLUTION.

In this problem, you were asked to:

- Find the CV for each data set

In order to do this, we only need to plug the **sample** standard deviation and mean of each data set into the formula given above.

Measure	Data Set A	B	C	D
Coefficient of Variation	CV= $3/45 * 100$ CV = 6.7	CV = $11/60 * 100$ CV=18.3	CV= $5/30 * 100$ CV= 10	CV= $15/25 * 100$ CV= 60

In this case, the data set with the lowest CV is data set A, followed by C, D and D. Meaning, set A has the lowest variation amongst these data sets.

ANS.

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