

Course:-

Electrical Network  
Analysis

Module : 4<sup>th</sup> semester.

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Question No 1: -

Assume that a 2000-kW turbine generator of 0.85 power factor operates at the rated load.

→ An additional load of 300kW at 0.8 power factor is added. What KVAR of Capacitor is required to operate the turbine generator but keep it from being overload?

⇒ Solution: -

Original load:-

$$P_1 = 2000 \text{ kW} \cdot \cos\phi_1 = 0.85$$

$$\phi_1 = 31.79^\circ$$

$$S_1 = \frac{P_1}{\cos\phi_1} = 2352.94 \text{ KVA}$$

$$Q_1 = S_1 \sin\phi_1 = 1239.5 \text{ KVAR}$$

Additional load:

$$P_2 = 300 \text{ kW} \quad \cos \theta_2 = 0.8 \rightarrow \\ \theta_2 = 36.87^\circ$$

$$S_2 = \frac{P_2}{\cos \theta_2} = 375 \text{ kVA}$$

$$Q_2 = S_2 \sin \theta_2 = 225 \text{ kVAR}$$

Total load:

$$S = S_1 + S_2 = (P_1 + P_2) + j(Q_1 + Q_2) = P + jQ$$

$$P = 2000 + 300 = 2300 \text{ kW}$$

$$Q = 1239.5 + 225 = 1464.5 \text{ kVAR}$$

Minimum operation pf for a 2300 kW load and not exceeding the kVA rating of the generator is

$$\cos \theta = \frac{P}{S_1} = \frac{2300}{2352.94} = 0.9775$$

$$\theta = 12.177^\circ$$

The maximum load kVAR for this condition is:-

$$Q = S_i \sin \phi = 2352.94 \sin \phi$$

$$Q = 496.313 \text{ kVAR.}$$

The capacitor must supply the difference between the total kVAR. (i.e.  $Q$ ) and the permissible generator kVAR. Thus,

$$Q_c = Q - Q_m = 968.2 \text{ kVAR.}$$

Question No 4:-

Apply Laplace transform and calculate the output voltage  $V_o(t)$  in the circuit of figure below.

Solutions:-

At node 1

$$\frac{10 - V_1}{s} - \frac{V_1 - V_o}{s} + \frac{s}{2} V_1 = 10 = (s+1)V_1$$

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$$\frac{s+1}{(s+1)^2 + 0.7071^2} - \frac{1.414 \cdot 0.7071}{(s+1)^2 + 0.7071^2}$$

Taking the inverse laplace transform

$$V_o(t) = \frac{20}{3} \left[ 1 - e^{-t} \cos(0.7071t) - 1.414 e^{-t} \sin(0.7071t) \right] u(t) \text{ V}$$

Question No 5:-

Solution:-

Source impedance  $Z_s = R_s - jX_s$

Load impedance  $Z_L = R_L + jX_L$

For maximum load transfer

$$Z_L = Z_s^* \rightarrow R_L = R_s, X_L = X_s$$

$$\omega = \frac{1}{\sqrt{LC}} = 2\pi f$$

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$$\omega = \frac{1}{\sqrt{LC}} = 2\pi f$$

$$f = \frac{1}{2\pi\sqrt{LC}} = \frac{1}{2\pi\sqrt{(80 \times 10^{-3})(40 \times 10^{-9})}}$$

$$= 2.814 \text{ kHz}$$

$$(b) P = \left[ \frac{V_s}{10+4} \right]^2 4 = \left[ \frac{4.6}{14} \right]^2 4 = 431.8 \text{ mW}$$

(sin  $V_s$  is in rms).

Question No 2:-

A balanced abc sequence one line voltage of a balanced Y-connected source is  $V_{AB} = 180 \angle -20^\circ \text{ V}$ . If the source is connected to a  $\Delta$ -connected load of  $20 \angle 40^\circ \Omega$ , find that phase and line currents.

Solution:-

$$\text{Line voltage } V_{AB} = 180 \angle -20^\circ \text{ V}$$

$$Z_{\Delta} = 20 \angle 40^\circ \Omega$$

Using formula.

$$V_L = \sqrt{3} V_p \angle 30^\circ \Rightarrow V_p = \frac{V_L}{\sqrt{3} \angle 30^\circ}$$



$$V_{an} = \frac{180 \angle -20^\circ}{\sqrt{3}} \angle -30^\circ = 103.9 \angle -50^\circ \text{ V}$$

$$Z_y = \frac{Z_A}{3} = \frac{20 \angle 40^\circ}{3} = 6.67 \angle 40^\circ \Omega$$

Line current:

$$I_a = \frac{V_{an}}{Z_A/3} = \frac{103.9 \angle -50^\circ}{6.67 \angle 40^\circ}$$



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$$I_b = I_a \angle -120^\circ = 15.59 \angle +150^\circ \text{ A}$$

$$I_c = I_a \angle +120^\circ = 15.59 \angle 30^\circ \text{ A}$$

Phase current:

$$I_{AB} = 15.57 \angle -90^\circ \angle 30^\circ = 9 \angle -60^\circ \text{ A}$$

$$I_{BC} = I_{AB} \angle -120^\circ = 9 \angle -180^\circ \text{ A}$$

$$I_{CA} = I_{AB} \angle +120^\circ = 9 \angle 60^\circ \text{ A}$$

Question No 3:-

Solutions:-

$$V_{rms} = 110 \angle 85^\circ \text{ V.}$$

$$I_{rms} = 0.4 \angle -15^\circ \text{ A.}$$

The complex power is

$$\textcircled{a} \quad S = V_{rms} I_{rms}$$

$$S = (110 \angle 85^\circ)(0.4 \angle -15^\circ)$$

$$S = 110 \times 0.4 \angle (85^\circ - 15^\circ)$$

$$S = \underline{44 \angle 70^\circ \text{ VA}}$$

The apparent power is

$$S = |S|$$

© The power factor is

$$PF = \cos(70^\circ)$$

$$\therefore PF = \underline{0.342 \text{ lagging}}$$

The power factor is lagging as the reactive power is positive.

The load impedance is:

$$Z = \frac{V}{I}$$

$$V = \sqrt{2} V_{rms}$$

$$I = \sqrt{2} I_{rms}$$