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**Program .....B-thec ( Electrical)**

**Subject ..... Power system analysis**

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Q No :- 1

Ans :-  
7

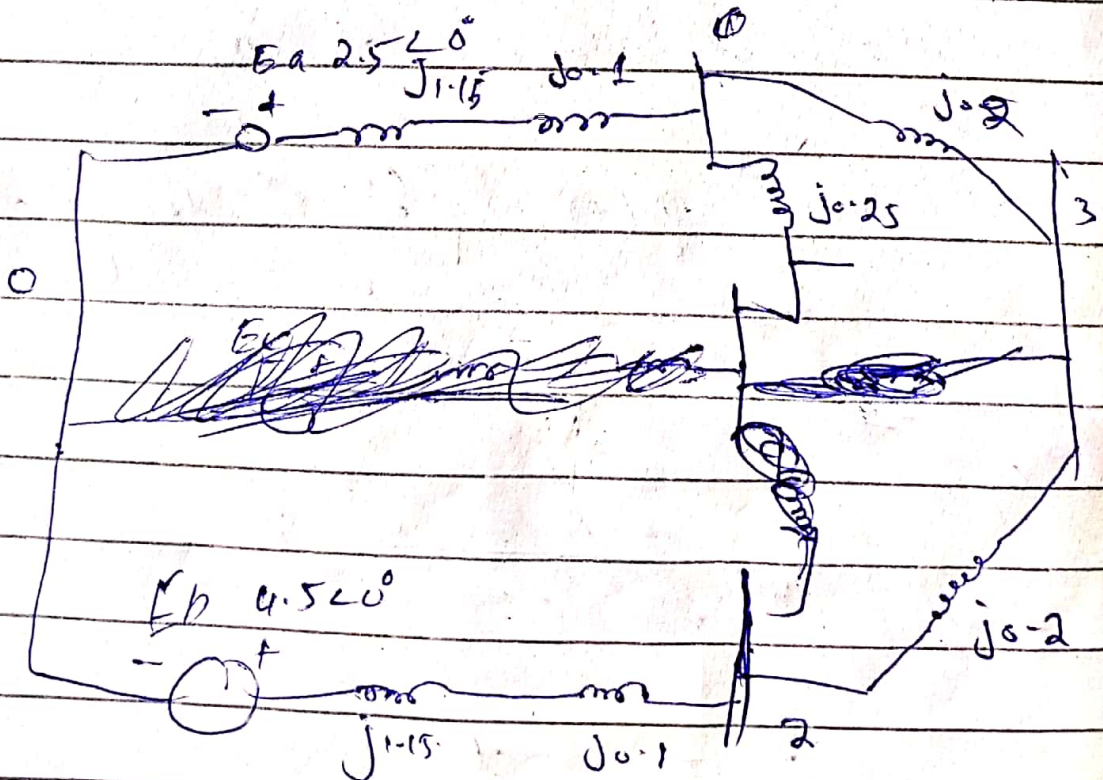
when

Write in matrix form the node equation necessary to solve for the voltage of the numbered buses of Figure shown network is equivalent as follows are

the EMFs shown in figure

a)  $E_a = 2.5 \angle 0^\circ$

b)  $E_b = 4.5 \angle 0^\circ$  all in per unit



Sol

the current source are

$$I_1 = I_3 \frac{2.5 \angle 0^\circ}{j12.5}$$

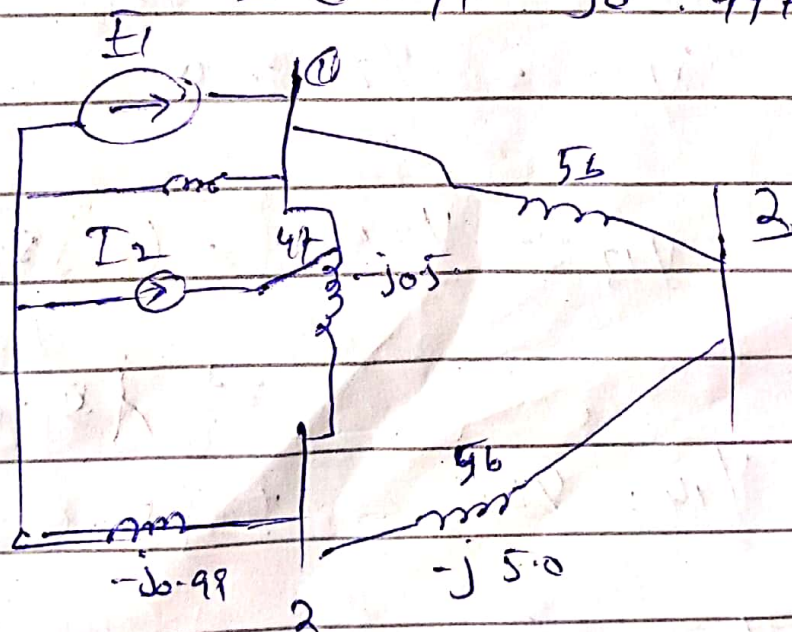
$$= 1.2 \angle -90^\circ$$

$$= 0 - j1.26 \text{ p.u.}$$

$$I_2 = \frac{4.5 \angle 0^\circ}{j1.25}$$

$$= 1.3 \angle -136.87^\circ$$

$$= 0.91 - j0.99 \text{ p.u.}$$





Self-admittance in p.u area

$$Y_{11} = -j0.99 - j0.5$$

$$Y_{11} = -j0.94$$

$$Y_{22} = -j0.5 - j2.7$$

$$Y_{22} = -j1.2$$

$$Y_{33} = j4.0 - j2.5$$

$$Y_{33} = j15.3$$

$$Y_{12} = Y_{21} = 0$$

$$Y_{13} = Y_{31} = -(-j5.0)$$

$$= +j5.0$$

$$Y_{14} = Y_{41} = +j5.0$$

$$Y_{23} = Y_{32} = +j2.7$$

$$Y_{24} = Y_{42} = +j5.0$$

$$Y_{34} = Y_{43} = +9.0$$

The node equation in matrix form

are

$$\begin{bmatrix} 0 - j1.50 \\ -0.94 - j0.006 \\ 0 - j1.20 \end{bmatrix} = \begin{bmatrix} -9.8 & j0.0 & j4.0 \\ j0.0 & -j8.3 & j2.5 \\ j4.0 & j2.5 & -j15.3 \end{bmatrix} \begin{bmatrix} V_1 \\ V_2 \\ V_3 \end{bmatrix}$$

Multiply b/g of matrix by the inverse of bus admittance matrix

$$\text{i.e. } A^{-1} = \frac{1}{\det A} \text{adj} A$$

$$\begin{bmatrix} j0.4777 & j0.376 & j0.4020 \\ j0.3706 & j0.4892 & j0.3922 \\ j0.4146 & j0.3922 & j0.4558 \end{bmatrix} \begin{bmatrix} 0 - j1.20 \\ -0.94 - j0.006 \\ 0 - j1.20 \end{bmatrix}$$

$$= \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \\ 0 & 0 & 0 \end{pmatrix} \begin{pmatrix} v_1 \\ v_2 \\ v_3 \end{pmatrix}$$

$$v_1 = 0 - 2668^\circ \text{ P.O}$$

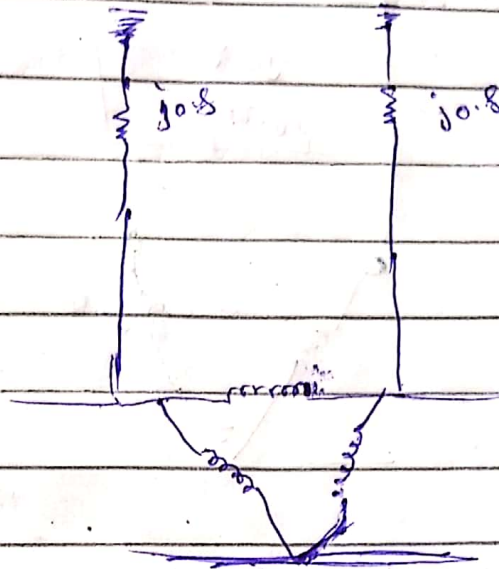
$$v_2 = 0 - 3508^\circ \text{ P.O}$$

$$v_3 = 1 - 36^\circ \text{ P.O}$$



Q No: - 2:

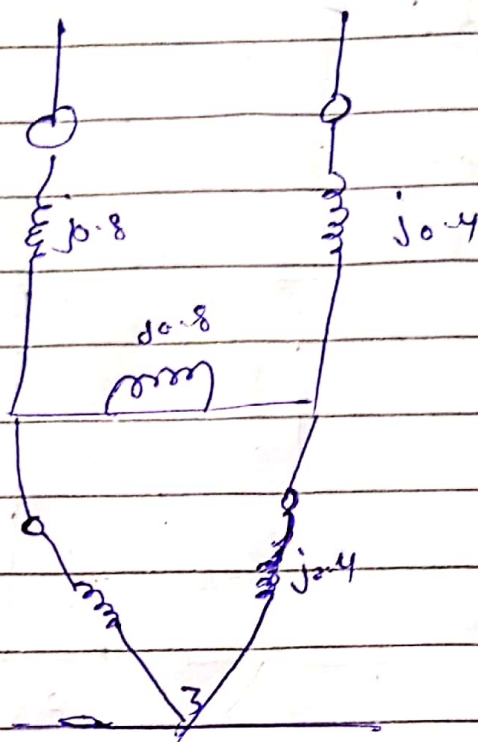
Ans Solution



Z-base

$$Z_{base} = Y_{bus}$$

Z base	$Z_{11}$	$Z_{12}$	$Z_{13}$
	$Z_{21}$	$Z_{22}$	$Z_{23}$
	$Z_{31}$	$Z_{32}$	$Z_{33}$



$V_1$	$Z_{11}$	$Z_{12}$	$Z_{13}$
$V_2$	$Z_{21}$	$Z_{22}$	$Z_{23}$
$V_3$	$Z_{31}$	$Z_{32}$	$Z_{33}$

$$V_1 = Z_{11} I_1 + Z_{12} I_2 + Z_{13} I_3 \quad \text{--- (1)}$$

$I_1$
$I_2$
$I_3$

$$V_2 = Z_{21} I_1 + Z_{22} I_2 + Z_{23} I_3 \quad \text{--- (2)}$$

$$V_3 = Z_{31} I_1 + Z_{32} I_2 + Z_{33} I_3 \quad \text{--- (3)}$$



Q No:-3

Ans :-

\* A generator of 10 kW Feeding to connected in 11 kV Busbar injecting real power  $P_{gk}$  and reactive power  $Q_{gk}$

\* A 20 kW load are connected which take  $P_{lk}$ ,  $Q_{lk}$  from the 11 kV bus bar.

\* This 11 kV bus bar is connected to other 11 kV bus bar  $i, j$  and through lines

$\Rightarrow$  the voltage at bus bar is  $V_k$  where  $\theta_k$  is equal to the magnitude  $V_k$  and the angle  $\theta_k$

$\Rightarrow$  one think we see that 10 kW generator injecting  $P_{gk}$  and  $Q_{gk}$  while 20 kW load takes  $P_{lk}$  and  $Q_{lk}$  from the bus bar. then we can take the algebraic sum of generation and 20 kW loads. i.e subtract the 20 kW loads from

11 KV generation

i.e.

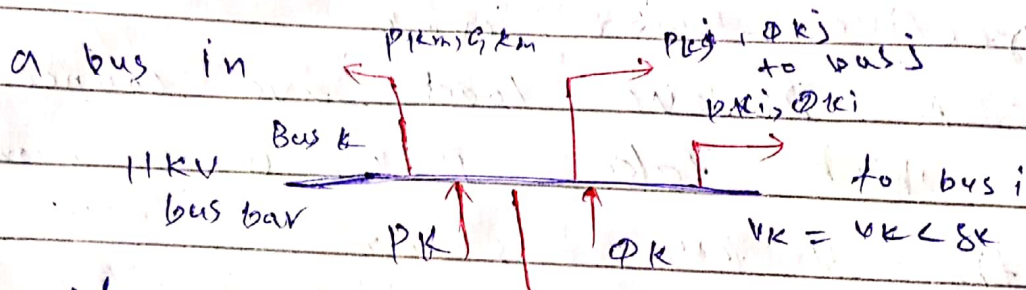
$$P_k = P_{gk} - P_{Lk}$$

∴ real power injecting

Similarly Reactive Power injecting is

$$Q_k = Q_{gk} - Q_{Lk}$$

then the diagram becomes



Now we will say the injecting into the bus bar rather saying the 11KV generation and 20KW load

at a particular bus bar there is no generation 11KV input and only 20KW load is connected then the injecting

$$\therefore P_k = 0 - P_{Lk}$$

$$P_k = -P_{Lk}$$

$$\therefore Q_k = 0 - Q_{Lk}$$

$$Q_k = -Q_{Lk}$$

So, load can be considered as Negative injection



$\Rightarrow$  From the diagram we see that we have three lines, one going to bus bar  $i$ , 2nd to  $j$  and to 3rd one to  $m$ . These lines will carry the power  $P_{ki}, Q_{ki}$  to bus  $i$ ,  $P_{kj}, Q_{kj}$  to bus  $j$  and  $P_{km}, Q_{km}$  to bus  $m$ .

$\Rightarrow$  Some of these power may be in the reverse directions i.e. they may be coming from bus  $j$  to bus  $k$ , in that case the value of  $P_{kj}, Q_{kj}$  will be negative.

So, 
$$P_k = P_{ki} + P_{kj} + P_{km}$$

$$Q_k = Q_{ki} + Q_{km}$$

$\therefore$  Real and Reactive power is equal to the algebraic sum of  $P, Q, \phi$  Power going out.

Power Flow equation

we should that power flow equation are coming from the Network equation

i.e. 
$$I_{bus} = Y_{bus} \cdot V_{bus} \rightarrow (1)$$



Where  $I_{Bus}$  is the vector of current injection into the bus bars  $Y_{Bus}$  is the  $n \times n$  matrix of the admittance and  $V_{Bus}$  is the voltage power at the  $n$  buses of the power system

$\Rightarrow$  For a particular bus  $k$ , we can write the equation as,

$$I_k = \sum_{n=1}^N Y_{kn} V_n \rightarrow (2)$$

where  $N = \text{no of bus bars}$ .

$Y_{kn}$  = admittance of the  $kn$  element  
From equation we can write the complex power injection at bus bar  $k$  is

$$S_k = P_k + jQ_k = V_k I_k^* \rightarrow (3)$$

$$P_k + jQ_k = V_k \left[ \sum_{n=1}^N Y_{kn} V_n \right]^*$$

where  $k = 1, 2, \dots, N$

$V_n$  is a phasor which has a magnitude and an angle

$$V_n = V_n e^{j\delta_n}$$

$$\text{and } Y_{kn} = Y_{kn} e^{j\phi_{kn}}, \quad k, n = 1, 2, \dots, N$$

Substituting  $V_n$  and  $Y_{kn}$  value in eq (3)

$$P_k + jQ_k = V_k \sum_{n=1}^N Y_{kn} V_n e^{j\delta_n} \quad (S_k - S_n - \phi_{kn})$$

∴ All angle  $\delta_k$  with  $V_k$   
 $\delta_n$  with  $V_n$

All Negative bk of conjugates,  
we can separate out the real &  
imaginary parts - then we can write  
the real power injection into Bus k

a)

$$P_k = V_k \sum_{n=1}^N Y_{kn} V_n \cos(\delta_k - \delta_n - \theta_{kn}) \quad (4) \leftarrow$$

Similarly the reactive power injection is

$$Q_k = V_k \sum_{n=1}^N Y_{kn} V_n \sin(\delta_k - \delta_n - \theta_{kn}) \quad (5) \leftarrow$$

So we can see that these injections  
is related to that the voltage  
magnitude and angle at  $V$  carries bus base

Eq (4) & (5) is said as the power  
Flow equation for the Power Network



Q No: - 4

Ans:

These is one problem in doing power solution as the load are known to us but generation are in over control and one can say that all generation know to us but there is one problem - the problem is still all the generation are available we don't know what is the loss in the system we cannot know how much generation belong losses must be equal to the total generation

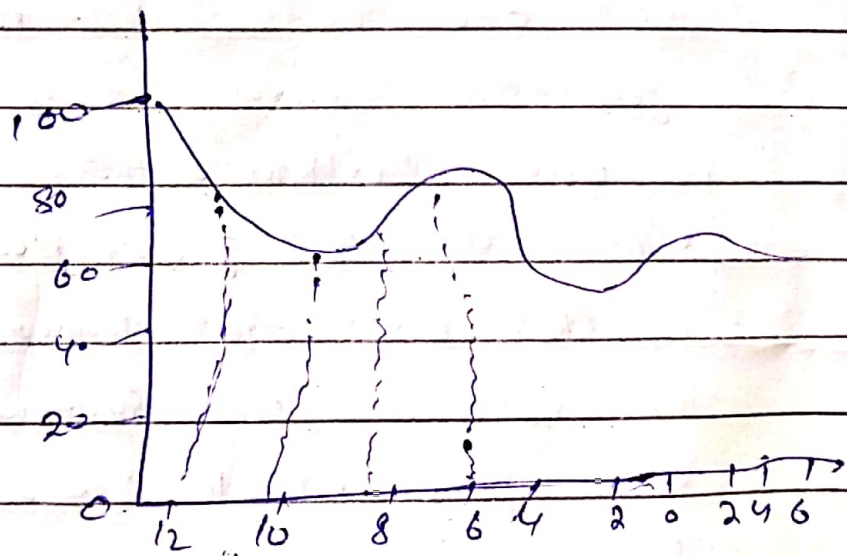
Solution:

In over come this we choose one bus as a reference bus which take up all these cases which can find after solution so at one bus we can not ~~sep~~ sep edify the generation this is bus which frame very



Large generation available so that there will be no problem for it to take a loss as this bus is power system terminology is called a slack bus

### Load curve



Q no:- 5

Ans:-

this method we find of the power flow equation for these method start again with the losses of network equation

I.e,  $I_{Bus} = Y_{Bus} = V_{Bus}$

and for any particular Bus

is

$$I_k = \sum_{n=1}^n Y_{kn} V_n$$

the complex power  $P_k + jQ_k = V_k I_k$

$$P_k + jQ_k = V_k \left\{ \sum_{n=1}^n Y_{kn} V_n \right\}$$

where  $k = 1, 2, \dots, N$

From complex power

$$I_k = \frac{P_k - jQ_k}{V_k}$$

$$* I_k = \sum_{r=1}^n Y_{kr} V_r$$

$$P_k = Y_{k1} V_1 + Y_{k2} V_2 + Y_{kN} V_N +$$

From the above equation

$$V_k = \frac{1}{Y_{k0}} \left( I_k - \left( \sum_{n=1}^{k-1} Y_{kn} \right) V_n \right)$$

$$\sum_{n=k+1}^N V_{kn} V_n$$

or

$$V_k = \frac{1}{Y_{k0}} \left( \frac{P_k - jQ_k}{V_k} \left( \sum_{n=1}^{k-1} Y_{kn} V_n \right) + \sum_{n=k+1}^N Y_{kn} V_n \right)$$

Where  $k = 1, 2, \dots, N$

F



# Flow Chart Gross Social

