

IQRA NATIONAL UNIVERSITY



Electro Magnetic Field **Mid Term Summer Paper 2020**

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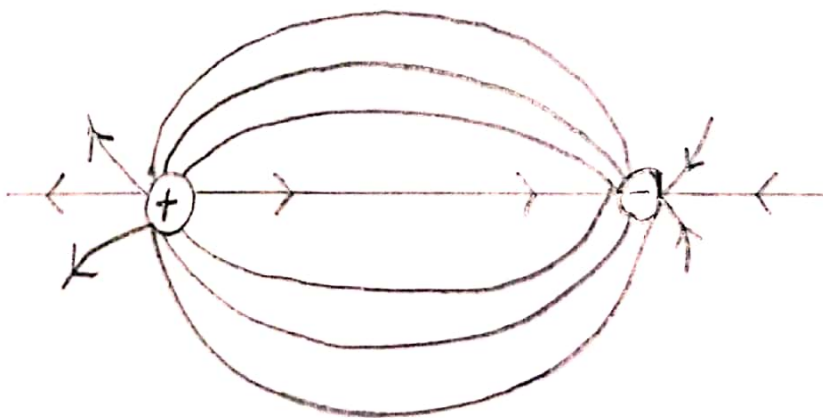
=> Question NO (1)

=> Part (A)

What is the difference between electric field and magnetic field?

Answer :- Electric Field

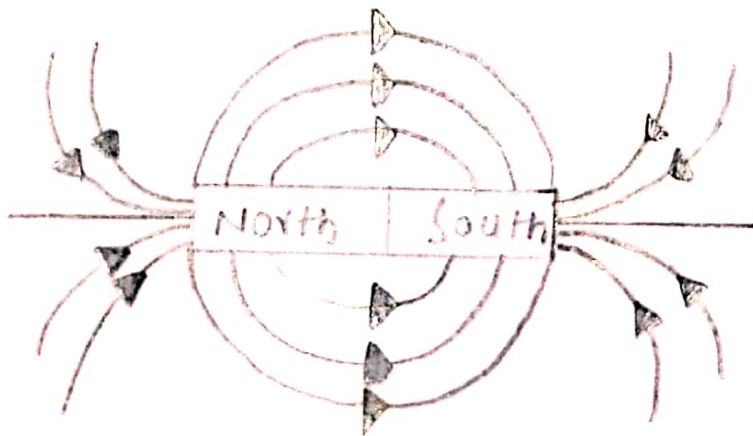
it is defined as the electric force per unit charge. The direction of the field is taken to be the direction of the force it would exert on a positive test charge. The electric field is radially outward from a positive charge and radially inward toward a negative point charge.



Diagram

=> Magnetic Field

A magnetic field is a vector field that describes the magnetic influence on an electric charge of other moving charges or magnetized materials. The effects of magnetic fields are commonly seen in permanent magnets which pull on magnetic material such as iron and attract or repel other magnets creating a torque.



Diagram

→ Difference between Electric Field and Magnetic Field

The magnetic field is an exerted area around the magnetic force it is obtained by moving electric charges. The direction of the magnetic field is indicated by lines while the electric fields are generated around the particles which obtain electric charge during this process. Positive charges are drawn while negative charges are repelled.

⇒ Electric Field VS Magnetic Field



⇒ Question No (1)

⇒ Part (B)

Given $A = 2ax - 3ay + az$ and $B = -4ax - 2ay + 5az$
Find $A \times B$

Solution :- $A \times B = (A_y B_z - A_z B_y) ax + (A_z B_x - A_x B_z) ay$
 $+ (A_x B_y - A_y B_x) az$

⇒ Put values

$$A \times B = ((-3)(5) - (1)(-2)) ax + ((1)(-4) - (2)(5)) ay$$

$$+ ((2)(-2) - (-3)(-4)) az$$

$$A \times B = (-15 + 2) ax + (-4 - 10) ay + (-4 - 12) az$$

$$A \times B = -13ax - 14ay - 16az$$

Answer



=> Question NO (2)

=> Explain the three coordinates in detail with vector representation?

Answer:- vector

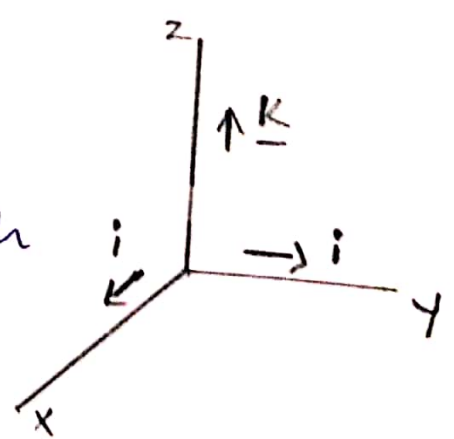
A quantity having direction as well as magnitude especially as determining the position of one point in space relative to another. is called vector.

=> Representation of vector

A vector is usually represented by arrows with their length representing the magnitude and their direction ->

=> unit vector

A vector of unit length



=> Base vectors for a rectangular

=> Coordinate System

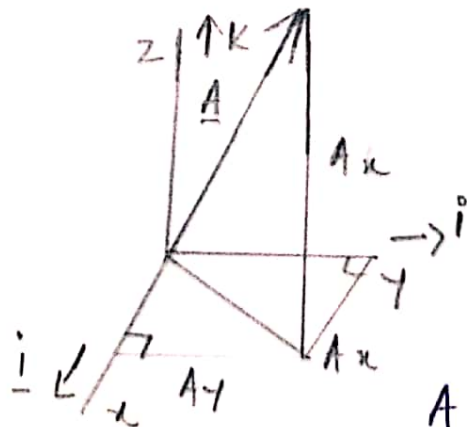
A set of three mutually orthogonal unit vectors

=> Right handed System

A coordinate system represented by base vectors which follow the right hand rule.

=> Rectangular Component of a vector

The projections of vector \underline{A} along the $x, y,$ and z directions are $A_x, A_y,$ and A_z respectively.



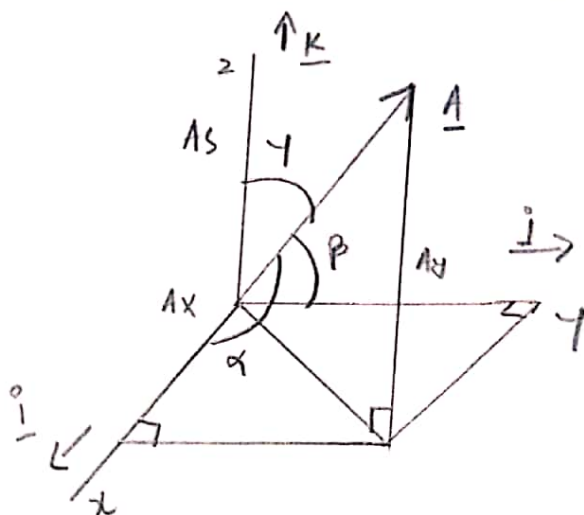
$$\underline{A} = A_x \underline{i} + A_y \underline{j} + A_z \underline{k}$$

⇒ Magnitude of a vector

$$A = \sqrt{A_x^2 + A_y^2 + A_z^2}$$

⇒ Direction of cosines

$\cos(\alpha)$, $\cos(\beta)$, $\cos(\gamma)$



$$\cos(\alpha) = \frac{A_x}{A}, \quad \cos(\beta) = \frac{A_y}{A}, \quad \cos(\gamma) = \frac{A_z}{A},$$

$$\cos^2(\alpha) + \cos^2(\beta) + \cos^2(\gamma) = 1$$

⇒ unit vector along a vector

The unit vector \underline{u}_A along the vector \underline{A} is obtained from

$$\Rightarrow \underline{u}_A = \frac{\underline{A}}{A} = \frac{A_x}{A} \underline{i} + \frac{A_y}{A} \underline{j} + \frac{A_z}{A} \underline{k} = \cos(\alpha) \underline{i} + \cos(\beta) \underline{j} + \cos(\gamma) \underline{k}$$

$$\Rightarrow \underline{A} = \frac{A \underline{u}_A}{A} = A(\cos(\alpha) \underline{i} + \cos(\beta) \underline{j} + \cos(\gamma) \underline{k})$$

⇒ Addition of vectors

The resultant vector $\underline{F_R}$ obtained from the addition of vectors $\underline{F_1}$, $\underline{F_2}$ and $\underline{F_n}$ is given by

$$\underline{F_R} = \sum \underline{F} = \sum F_x \underline{i} + \sum F_y \underline{j} + \sum F_z \underline{k}$$

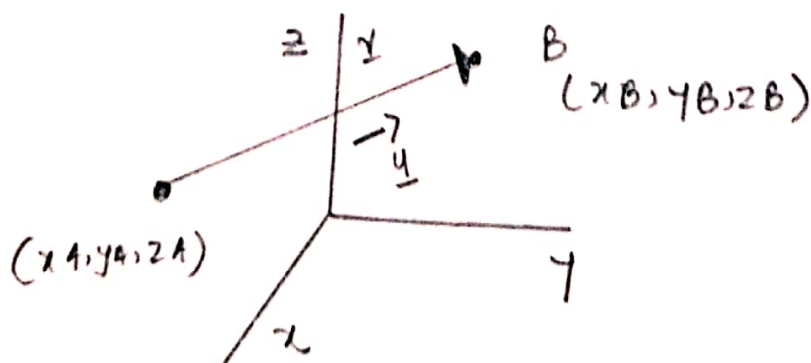
⇒ Coordinates of points in space

The triplet (x, y, z) describe the coordinates point

⇒ The vector connecting two points.

The vector connecting point A to point B is given by.

$$\underline{r} = (x_B - x_A) \underline{i} + (y_B - y_A) \underline{j} + (z_B - z_A) \underline{k}$$



⇒ A unit vector along the line A-B

A unit vector along the line A-B is obtained from.

$$\underline{u} = \frac{\underline{r}}{r}$$

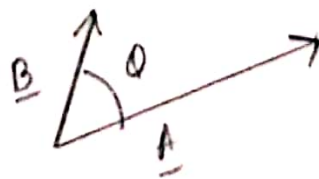
⇒ A vector along A-B

A vector \underline{F} along the line A-B and of magnitude F can be obtained

from $\underline{F} = F \frac{\underline{r}}{r} = F \underline{u}$

⇒ The dot product

The dot product of vector \underline{A} and \underline{B} is given by



$$\underline{A} \cdot \underline{B} = AB \cos(\theta) = A_x B_x + A_y B_y + A_z B_z.$$

ID# 13170

⑩

\Rightarrow Projection of a vector by using the dot product

The projection of vector \underline{A} along the unit vector \underline{u} is given by.



$$\underline{A} \cdot \underline{u} = A \cos(\theta)$$



⇒ Question No (3)

⇒ Part (A)

Explain in detail Electrical Field Intensity and electric flux density.

Answer :- Electric Field Intensity

The space around an electric charge in which its influence can be felt is known as the electric field. The electric field intensity at a point is the force by a unit positive charge placed at that point.

- Electric Field Intensity is a vector quantity
- it is denoted by E
- Formula: Electric Field = F/q
- unit of E is Nc^{-1} or Vm^{-1}

- \Rightarrow Due to point charge q the Intensity of the electric field at a point d units away from it is given by the expression.
- \Rightarrow Electric Field Intensity $(E) = q / [4\pi\epsilon_0 d^2] \text{ NC}^{-1}$
- \Rightarrow The Intensity of the electric field at any point due to a number of Charges is equal to the vector sum of the sum intensities produced by the separate charges.
- \Rightarrow and a measure of the force exerted by one charged body to another. The electric field Intensity (voltage) at any location is the force (newtons) that would be experienced by unit test charge (coulombs).

→ Electric Flux density

Electric Flux density is defined as the amount of flux passes through unit surface area in the space imagined at right angle to the direction of electric field the expression of electric field at a point is given

$$E = \frac{Q}{4\pi \epsilon_0 \epsilon_r r^2}$$

where Q is the charge of the body by which the field is created R is the distance of the point from the center of the charged body

→ As we know, $Q = qV$

The above equation can be written as

$$\Rightarrow E = \frac{q}{4\pi\epsilon_0\epsilon_r r^2} \Rightarrow \epsilon_0\epsilon_r E = \frac{q}{4\pi r^2}$$

This is the expression of flux per unit area since $4\pi r^2$ is the surface area of the imaginary sphere of radius r .

This is the flux passing through per unit area at a distance r from the center of the charge. This is called electric flux density.

\Rightarrow we generally denoted it with english letter D . Therefore

$$\Rightarrow D = \epsilon_0\epsilon_r E$$

From the above expression of D it is clear that electric field intensity and electric field density are in same phase.



⇒ Question No (3)

⇒ part (B)

Point charge 5nC and -2nC are located at $(2,0,4)$ and $(-3,0,5)$ respectively

(i) Determine the force on 1nC point charge located at $(1, -3, 7)$

(ii) Find electric field \vec{E} at $(1, -3, 7)$

Solution

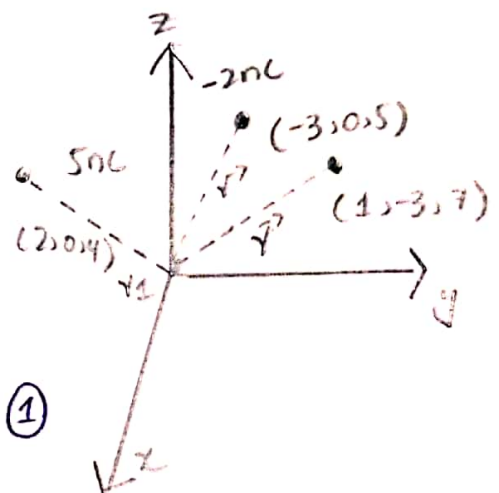
(i) As $Q_1 = 5\text{nC}$, $Q_2 = -2\text{nC}$

$$\vec{r} = a_x - 3a_y + 7a_z$$

$$r_1 = 2a_x + 4a_z$$

$$r_2 = -3a_x + 5a_z$$

$$\vec{F} = \frac{Q_1 Q_2 (\vec{r} - \vec{r}_1)}{4\pi\epsilon_0 (\sqrt{|\vec{r} - \vec{r}_1|})^3} \rightarrow \textcircled{1}$$



Put values in $\textcircled{1}$

$$\vec{F} = \frac{(1 \times 10^{-9})(5 \times 10^{-9})}{4\pi(10^{-9})} \frac{(a_x - 3a_y + 7a_z) - (2a_x + 4a_z)}{(\sqrt{-a_x - 3a_y + 3a_z})^3}$$

$$+ \frac{(1 \times 10^{-9})(-2 \times 10^{-9})}{4\pi(10^{-9})} \frac{(a_x - 3a_y + 7a_z) - (-3a_x + 5a_z)}{(\sqrt{4a_x - 3a_y + 2a_z})^3}$$

$$\Rightarrow \vec{F} = \frac{(45 \times 10^{-9}) (\vec{a}_x + 3\vec{a}_y + 3\vec{a}_z)}{(19)^{3/2}} - \frac{(18 \times 10^{-9}) (4\vec{a}_x - 3\vec{a}_y + 2\vec{a}_z)}{(29)^{3/2}} \quad (16)$$

$$\vec{F} = \frac{(-45, -135, 135)}{(19)^{3/2}} - \frac{(72, -54, 36)}{(29)^{3/2}}$$

$$\vec{F} = (-0.543, -1.630, 1.630) - (0.461, -0.346, 0.23) \text{ nN}$$

$$\vec{F} = -1.004\vec{a}_x - 1.284\vec{a}_y + 1.4\vec{a}_z \text{ nN}$$

Answer.

$$\Rightarrow \text{(ii)} \quad \text{Electric Field} = \vec{E} = \vec{F}/q$$

Put the values

$$\vec{E} = \frac{\vec{F}}{q} = \frac{-1.004\vec{a}_x - 1.284\vec{a}_y + 1.4\vec{a}_z}{1 \times 10^{-9}} \times 10^{-9}$$

$$\vec{E} = -1.004\vec{a}_x - 1.284\vec{a}_y + 1.4\vec{a}_z \text{ V/m}$$

Answer.

Thank You