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P#1

NO: 1

The lowest value is 363 and the highest value is 431

By using given data  
A class interval of 10.

The interval for the first class is 360 to 369 and it includes 363.

The distribution table is.

observation	Tally	frequency
360-369		2
370-379		3
380-389		5
390-399		7
400-409		5
410-419		4
420-429		3
430-439		1

Total freq = 30

P#2

Calculate Mean.

$$\text{Mean} = \frac{\text{Sum of all number}}{\text{Total number.}}$$

$$\begin{aligned} \text{Sum} &= 423 + 369 + 387 + 411 + 493 + 394 + 374 \\ &+ 377 + 381 + 409 + 392 + 405 + 431 + 404 \\ &+ 363 + 391 + 405 + 382 + 400 + 381 + 399 \\ &+ 415 + 425 + 422 + 396 + 372 + 410 + 419 \\ &+ 380 + 390 = 11914 \end{aligned}$$

Sum = 11914 Put the values

$$\text{Mean} = \frac{11914}{30} = 397.1$$

$$\text{Mean} = 397.$$

$$\text{Mode: } L + \frac{f_m - f_{m-1}}{(f_m - f_{m-1}) + (f_m - f_{m+1})} \times w$$

$L$  is Lower class boundaries -

$f_{m-1}$  freq- of group before modal group

$f_m$  freq- of group ~~of~~ modal group

$f_{m+1}$  group after modal group

$w$  group width

P#3

$$M = 389.5 + 8 - 3/2(8) - 3.5(395.5 - 389.5)$$

$$= 389.5 + 5/16 - 8(11)$$

$$= 389.5 / 1 + 55/8$$

$$= 3131/8$$

$$= 391.8$$

Medium:

$$L = 389.5$$

$$n = 30$$

$$B = 2 + 3 + 5 = 10$$

$$W = 10$$

$$G = 7$$

$$= \frac{389.5 + (30/2) - 10 \times 10}{7}$$

$$= \frac{389.5 + (15) - 10 \times 10}{7}$$

$$= 389.5 + 0.7143$$

$$= 390.21$$

Quartile:

$$1 + h(f(q-c))$$

$$q = n/4 = 30/4$$

$$q = 7.5$$

$$Q_1 = 389.5 + 11(3(7.5-7))$$

$$Q_1 = 389.5 + 5.5/3$$

$$Q_2 = 11535.55/3 + 5.5/3$$

$$= 1148/3 = 382.66$$

$$Q_3 = 3n/4 = 3 \times 30/4$$

$$= 90/4$$

$$= 22.5$$

$$Q_3 = 406.5 + 11/5 (22.5 - 20)$$

$$Q_3 = 406.5 + 11/5 (2.5)$$

$$Q_3 = 406.5 + 27.5/5$$

$$= 2060/5$$

$$= 412$$

QNO2:

$$\text{Mean} = \frac{\text{Sum of all number}}{\text{Total number}}$$

$$\text{Mean} = \frac{3+6+2+1+7+5}{6} = \frac{24}{6} = 4$$

$$x = 4$$

$x_i$	$x_i - x$	$(x_i - x)^2$	$x_i^{n^2}$
3	$3 - 4 = -1$	1	9
6	$6 - 4 = 2$	4	36
2	$2 - 4 = -2$	4	4
1	$1 - 4 = -3$	9	1
7	$7 - 4 = 3$	9	49
5	$5 - 4 = 1$	1	25

$$S = \sqrt{\sum (x_i - x)^2 / n}$$

$$= \frac{\sqrt{28}}{6}$$

$$= \sqrt{4.66}$$

$$= 2.16$$

P#6

$$\text{Mean: } \frac{11+7+9+17+19+15}{6}$$

$$= 78/6$$

$$= 13$$

$X_i$	$x_i - \bar{x}$	$(x_i - \bar{x})^2$
11	$11 - 13 = -2$	4
17	$17 - 13 = 4$	16
9	$9 - 13 = -4$	16
7	$7 - 13 = -6$	36
19	$19 - 13 = 6$	36
15	$15 - 13 = 2$	4

$$S = \sqrt{\sum (x_i - \bar{x})^2 / n}$$

$$= \sqrt{112/6}$$

$$= 4.32$$

QNO 3:

class	Frequency	$x_i$	$F x_i$	$x_i^2$	$F x_i^2$
64-84	15	74	1110	5476	82140
85-104	18	94.5	1701	8930.25	160744.5
105-124	27	114.5	3091.5	13110.25	353976.75
125-144	10	134.5	1345	18090.25	180902.5
145-164	6	154.5	947	23870.25	143221.5
165-184	5	174.5	872.5	30450.25	152251.25
185-204	13	194.5	2528.05	37830.25	491793.25

$$\sum f = 94$$

$$\sum (f x_i) = 11575.5$$

$$\sum (f x_i^2) = 1565029.75$$

$$S^2 = \frac{\sum f x_i^2}{n} - \left( \frac{\sum f x_i}{n} \right)^2$$

$$S^2 = 1565029.75/60 - \left( 11575.5/60 \right)^2$$

$$= 26083.82 - 3720.05$$

$$\text{Variance} = S^2 = 22363.77$$

$$\text{Standard Deviation} = \sqrt{22363.77}$$

$$= 149.54$$

QNO4:

When two dice are thrown simultaneously, thus number of event can be  $6^2 = 36$  because each die has 1 to 6 number on its faces. Then the possible outcomes are shown in the below table.

Probability - Sample space for two dice (outcomes).

	1	2	3	4	5	6
1	(1,1)	(1,2)	(1,3)	(1,4)	(1,5)	(1,6)
2	(2,1)	(2,2)	(2,3)	(2,4)	(2,5)	(2,6)
3	(3,1)	(3,2)	(3,3)	(3,4)	(3,5)	(3,6)
4	(4,1)	(4,2)	(4,3)	(4,4)	(4,5)	(4,6)
5	(5,1)	(5,2)	(5,3)	(5,4)	(5,5)	(5,6)
6	(6,1)	(6,2)	(6,3)	(6,4)	(6,5)	(6,6)

Note:

- (i) The outcomes (1,1), (2,2), (3,3), (4,4), (5,5), and (6,6) are called doublets.
- (ii) The pair (1,2) and (2,1) are different outcomes.



Sum of 8.

Let  $E_5$  = event of getting a sum of 8. The number which is a sum of 8 will be  $E_5 = [(2,6), (3,5), (4,4), (5,3), (6,2)] = 5$

Therefore, probability of getting a sum of 8'

$$P(E_5) = \frac{\text{Number of favorable outcomes}}{\text{Total number of possible outcomes}}$$

$$= \frac{5}{36}$$

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If it is a double six, then only one occurrence has this condition out of the 36 possibilities for a roll.

Therefore the frequentist probability is  $\frac{1}{36}$

Q105: Let  $C_1, C_2, \dots, C_m$  be a partition of the sample space  $S$  and  $A$  and  $B$  be two events. Suppose we know that

- \*  $A$  and  $B$  are conditionally independent given  $C_i$  for all  $i \in \{1, 2, \dots, m\}$

Prove that  $A$  and  $B$  are independent.

Solution.

Since the  $C_i$ 's form a partition of the sample space, we can apply the law of total probability for  $A \cap B$

$$\begin{aligned} P(A \cap B) &= \sum_{i=1}^m P(A \cap B | C_i) P(C_i) \\ &= \sum_{i=1}^m P(A | C_i) P(B | C_i) P(C_i) \end{aligned}$$

$A$  and  $B$  are conditionally independent

$$\begin{aligned} &= \sum_{i=1}^m P(A | C_i) P(B) P(C_i) \quad (B \text{ is independent of } C_i) \\ &= P(B) \sum_{i=1}^m P(A | C_i) P(C_i) \\ &= P(B) P(A) \end{aligned}$$

law of total probability.