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Pg# 1

Subject = Plain Reinforced Concrete Design I

COND:1 A rectangular beam that must carry a service load 2.47 kips/ft and a calculated dead load 1.05 kips/ft (without self wt) on 18-ft simple span is limited to 10 inches width and 20 inches total depth. For architectural reasons if $f_y = 60000$ psi and $f_c = 40000$ psi. Calculate steel area? Draw sketch final design.

Solution

Given data:-

$$L.L = 2.47 \text{ kips/ft}$$

$$D.L = 1.05 \text{ kips/ft (without self wt)}$$

$$L = 18'$$

$$b = 10''$$

$$h = 20''$$

$$f_c = 4 \text{ ksi}$$

$$f_y = 60 \text{ ksi}$$

$$\text{Required } A_{st} = ?$$

Sol Step No:1 Size and dimension

As due to architectural size cannot be changed so

$$b = 10'' \quad h = 20''$$

Step 2: load and bending moment

Self wt

Self wt = unit wt of concrete \times volume of beam \times section

$$\text{So } 150 \text{ lb/ft}^3 \times \left(\frac{10}{12} \times \frac{20}{12} \times 18 \right) =$$

$$3750 \text{ lb} \Rightarrow \frac{3750}{1000} = \boxed{3.750 \text{ kips}}$$

Change this point load to U.D.L

$$\text{So } \frac{\text{Self wt}}{\text{span length}} = \frac{3.750}{18}$$

$$\text{self wt} = 0.2083 \text{ kips/ft}$$

Therefore total D.L will be

$$\text{D.L} = (1.05 + 0.2083)$$

$$\text{D.L} = 1.2583 \text{ kips/ft}$$

and

$$\text{L.L} = 2.47 \text{ kips/ft}$$

$$\text{Wu} = 1.2 \text{ D.L} + 1.6 \text{ L.L} = 1.2 \times 1.2583 + 1.6 \times 2.47$$

$$\boxed{\text{Wu} = 5.462 \text{ kips/ft}}$$

$$M_u = \frac{W_u l^2}{8} = \frac{5.462 \times 324}{8} = 221.211$$

$$M_u = 221.211 \text{ k-ft} \times 12$$

$$\boxed{M_u = 2654.532 \text{ kips-inch}}$$

Step 2 - Min. AS_{Ty} (d = 9/16)

$$\text{Let } a = 0.2d$$

$$a = 3.5''$$

$$d = h - 2.5 = 20 - 2.5 = 17.5$$

Putting value of a in

$$AS = \frac{M_u}{0.7y(d-a)}$$

$$AS = \frac{2654.532}{0.9 \times 60 (17 - 3.5)} \Rightarrow AS = 3.721 \text{ in}^2$$

Now calculate A from

$$a = \frac{ASy}{0.85 \times 4 \times 10} = \frac{3.721 \times 60}{0.85 \times 4 \times 10} \Rightarrow a = 5.5076 \text{ in}^2$$

Now again

$$AS = \frac{M_u}{0.7y(d-a)} = \frac{2654.532}{0.9 \times 60 (17.5 - \frac{5.5076}{2})} \Rightarrow AS = 3.33 \text{ in}^2$$

$$\text{For } a = \frac{3.33 \times 60}{0.85 \times 4 \times 10} = 5.88 \text{ in}^2$$

Again

$$AS = \frac{M_u}{0.7y(d-a)} = \frac{2654.532}{0.9 \times 60 (17.5 - \frac{5.88}{2})} = 3.376 \text{ in}^2$$

$$a = \frac{3.376 \times 60}{0.85 \times 4 \times 10} = 5.96 \text{ in}^2$$

Again

$$AS = \frac{2654.332}{0.9 \times 60 (17.5 - \frac{5.96}{2})} = 3.325 \text{ in}^2$$

$$Q = \frac{3.385 \times 60}{0.25 \times 4 \times 10} = 5.97 \text{ in}^2$$

Again

$$A_s = \frac{2654.332}{0.9 \times 60 \left(17.5 - \frac{5.97}{2}\right)} = 3.386 \text{ in}^2$$

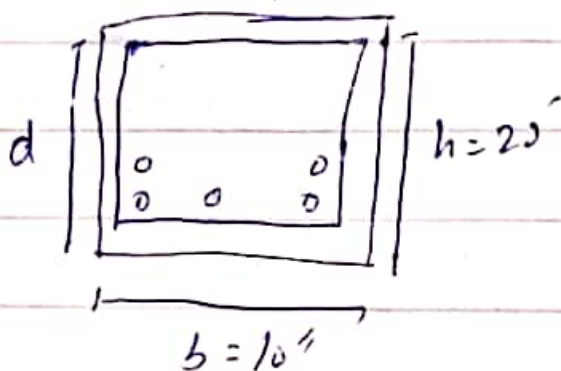
$$Q = \frac{3.386 \times 60}{0.25 \times 4 \times 10} = 5.977 \text{ in}^2$$

Again

$$A_s = \frac{2654.332}{0.9 \times 60 \left(17.5 - \frac{5.977}{2}\right)} = 3.387 \text{ in}^2$$

using ~~7~~ 8 bars so

$$\text{No } 9 \text{ bars} = \frac{3.387}{0.79} = 4.29 \times 5 \text{ bars}$$



the bar are provided into 2 layer

Q.No. 2

Bond stress and development length

(a) Bond stress :: the stress which is acting on the outer interface to the surrounding concrete over a certain length. ~~Concrete~~ is called bond stress. ~~the force~~ in this length of bar required to transfer the force in the bar to the surrounding concrete through bond is called development length.

(b) Doubly reinforcement.

Doubly reinforced section are generally resorted to in situation where the cross sectional dimension of beam are restricted (by architectural or other construction) where singly reinforced section is not adequate in terms of moment resisting capacity.

(3) D. T beam

(1) T beam having beam and slab composite section

(2) T beam is more economical than rectangular beam

(3) T beam are used in larger spans ~~can take a load~~

Rectangular beam

(1) Rectangular beam having compression in top and tension in bottom

(2) Rectangular beam is less economical than T beam

(3) Rectangular beam are more

T beam

rectangular

span such as bridge
there are always precast
reinforcement

① in case of T beam slabs
are connected with one another
and act as one member

often used in office
or commercial building. this can
be cast in using standard rebar

① in case of rectangular beam slabs are
placed on the beam so that there
is no connection b/w slabs and beam

① effect of strength reduction factor flexural strength

in the design of flexural strength the strength
reduction decrease from tension to control section to
the compression control section the increase with safety
and decrease with ductility this show to determine
the reduction factor for flexural strength of reinforced
concrete

(e) design method

there are ~~two~~ ^{two} methods

1) ASD method

2) USD method

① ASD method

ASD method is also known as working
stress method. it is based on principle
that stresses develop in the structural member

in this method all load are taken are service load and no factor is applied to increase service load

(2) ~~USD~~ USD method

Ultimate strength design method is also known as load factor method is also known as load factor for the structural subjected to large external load the ultimate strength is determine by the inelastic ~~USD~~ USD method

QNO: 3

Given data c/c distance = 10 ft

Total span = $L = 37$

Slab = $h_f = 6$ inch

width = $b_w = 14$ inch

depth = $h = 28$ inch

D.C = $50 \text{ psc} = 50 \text{ lb/ft}^2$

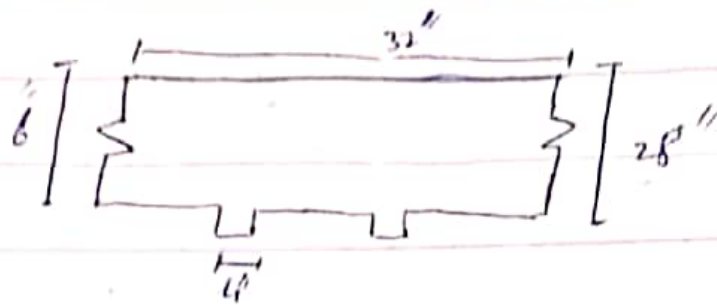
C.L $225 \text{ psc} = 225 \text{ lb/ft}^2$

$f_c =$ $4000 \text{ psi} = 4 \text{ ksi}$

$f_y =$ $60000 \text{ psi} = 60 \text{ ksi}$

effective depth = $h - 3$

$$28 - 3 = 25 \text{ inch}$$



Step 1

To find factored load

To find beam self wt

$$\Rightarrow W_t = b \times h \times \rho_c$$

$$W_t = 14 \frac{1}{2} \times 28 \frac{1}{2} \times 150 \text{ lb/ft}^2$$

$$W_t = 408.33 \text{ lb/ft}$$

Total factored load

$$W_u = 1.2 \text{ D.L.} + 1.6 \text{ L.L.}$$

$$1.2 (50 \times 408.33 + 1.6 \times 225)$$

$$W_u = 909.996 \text{ lb/ft} \quad \Rightarrow W_u = 0.911 \text{ kip/ft}$$

Step 2

ultimate factored moment

$$M_u = \frac{W_u l^2}{8} = \frac{0.911 (32)^2 \times 12}{8} \quad \Rightarrow M_u = 1397.76 \text{ kip/ft}$$

Step 3: effective depth (d)

$$18 \times h_f + b_w$$

$$(1) 16 \times 6 + 14 \Rightarrow 110 \text{ inch}$$

$$(2) \text{ c/c distance} \Rightarrow 10 \times 12 = 120 \text{ inch}$$

$$(3) \frac{S_{pcom}}{4} = \frac{32}{4} = 8' = 8 \times 12 = 96''$$

Then the $b_c = 96 \text{ inch}$

Step 1

To Check Which type of analysis is required

$$\text{Trial 01: } Q = h_f = 6''$$

$$\text{Then } AST = \frac{M_U}{0.75 \phi (d - a/2)} = \frac{1397.76}{0.9 \times 60 (25 - 6/2)}$$

$$AST = 1.177 \text{ in}^2$$

Trial 2

$$Q = \frac{AST + z_y}{0.25 \times \phi \times b} = \frac{1.177 \times 60}{0.25 \times 4 \times 96} \Rightarrow Q = 0.216'' < h_f = 6''$$

$$AST = \frac{1397.76}{0.9 \times 60 (25 - \frac{0.216}{2})} \quad | \quad AST = 1.04 \text{ in}^2$$

Trial 3

$$Q = \frac{1.04 \times 60}{0.25 \times 4 \times 96} = 0.19 \text{ in}^2$$

$$AST = \frac{1397.76}{0.9 \times 60 (25 - \frac{0.191}{2})} \quad | \quad AST = 1.04 \text{ in}^2$$

Steps:- to find f_{max} and f_{min}

$$f_{max} = 0.25 \times \beta \times \frac{L}{f_y} \left(\frac{z_u}{z_u + z_y} \right)$$

$$f_{max} = 0.25 \times 0.25 \times \frac{4}{6} \left(\frac{0.003}{0.0010075} \right)$$

$$f_{max} = 0.0121$$

$$f_{min} = \frac{200}{f_y} - \frac{200}{60000} = 0.0033$$

As we know that

$$f = \frac{AST}{bed} = \frac{1.04}{14.25}$$

$$f = 0.00297$$

So ~~f~~ $f_{min} < f < f_{max}$ OK

Now $f_{min} = \frac{AST}{bed} = AST \Rightarrow bed \geq f_{min}$
 61825×0.0033

$$AST \Rightarrow 1155 \text{ in}^2$$

Step 6 No 9 bar and bar section

let #8 bar use

$$\text{No 9 bar} = 1.47 \approx 2$$

We take 2 #8 bar as main bar

Step 7 minimum width

$$b_{min} = 2 \times C.C + 2 \times \text{strip} + 2 \times \text{main bar} + 1 \times \text{spacing}$$

$$b_{min} = (2 \times 1.5) + (2 \times 3/8) + 2 \left(\frac{3}{8} \right) \left(1 + \frac{3}{8} \right)$$

$$b_{min} = 675 < 111''$$

So the main bar are good

2#8



Step 3 Design moment

$$M_d = \phi \times 7y \times AS (d - \frac{y}{2})$$

$$0.9 \times 60 \times 1.57 \left(25 - \frac{0.289}{2} \right)$$

$$M_d = 2160.24$$

$$M_d > M_u$$

Design ok