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Paper	<u>maths</u>



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$$Q1) \frac{3x^3 - 5x^2 + 5}{x^2 + 1}$$

let

$$\text{Sol: } y = \frac{3x^3 - 5x^2 + 5}{x^2 + 1}$$

diff w.r.t, x

$$\frac{dy}{dx} = \frac{d}{dx} \left( \frac{3x^3 - 5x^2 + 5}{x^2 + 1} \right)$$

$$= \frac{(x^2 + 1) \frac{d}{dx} (3x^3 - 5x^2 + 5) - (3x^3 - 5x^2 + 5) \frac{d}{dx} (x^2 + 1)}{(x^2 + 1)^2}$$

$$(x^2 + 1)^2$$

$$= \frac{(x^2 + 1) (3 \times 3x^{3-1} - 5 \times 2x^{2-1} + 0) - (3x^3 - 5x^2 + 5) (2x)}{(x^2 + 1)^2}$$

$$(x^2 + 1)^2$$

$$= \frac{(x^2 + 1) (9x^2 - 10x) - (6x^4 - 5x^3 + 10x)}{(x^2 + 1)^2}$$

$$(x^2 + 1)^2$$

$$= \frac{9x^4 - 10x^3 + 9x^2 - 10x - 6x^4 + 5x^3 - 10x}{(x^2 + 1)^2}$$

$$(x^2 + 1)^2$$

$$\frac{dy}{dx} = \frac{3x^4 - 5x^3 + 9x^2 - 20x}{(x^2 + 1)^2}$$

Q1 part B)

$$\frac{(x^2+1)^2}{x^2-1}$$

$$\text{let } y = \frac{(x^2+1)^2}{x^2-1}$$

diff w.r.t to, x

$$\frac{dy}{dx} = \frac{d}{dx} \left( \frac{(x^2+1)^2}{x^2-1} \right)$$

$$= \frac{(x^2-1) \frac{d}{dx} (x^2+1)^2 - (x^2+1)^2 \frac{d}{dx} (x^2-1)}{(x^2-1)^2}$$

$$= \frac{(x^2-1) 2(x^2+1) \frac{d}{dx} (x^2+1) - (x^2+1)^2 (2x)}{(x^2-1)^2}$$

$$= \frac{2(x^2-1)(x^2+1)(2x) - (x^4+1+2x^2)(2x)}{(x^2-1)^2}$$

$$= \frac{4x((x^2)^2 - (1)^2) - (2x^5 + 2x + 4x^3)}{(x^2-1)^2}$$

$$= \frac{4x(x^4 - 1) - 2x^5 - 4x^3 - 2x}{(x^2-1)^2}$$

$$= \frac{4x^5 - 4x - 2x^5 - 4x^3 - 2x}{(x^2-1)^2}$$

$$\frac{dy}{dx} = \frac{2x^5 - 4x^3 - 6x}{(x^2-1)^2} \text{ Ans.}$$

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f g dx + g

Q #2

part (a)

$$\text{if } y = (1+2\sqrt{x})^3 \cdot x^{\frac{2}{3}}$$

diff w, r, to, x

$$y = [(1)^3 + (2\sqrt{x})^3 + 3(1)(2\sqrt{x})(1+2\sqrt{x})] x^{3/2}$$

$$y = [1 + 8x^{3/2} + 6\sqrt{x}(1+2\sqrt{x})] \cdot x^{3/2}$$

$$y = [1 + 8x^{3/2} + 6\sqrt{x} + 12x] \cdot x^{3/2}$$

$$y = [1 + 8x^{3/2} + 6x^{1/2} + 12x] \cdot x^{3/2}$$

$$y = x^{3/2} + 8x^{\frac{3}{2}+\frac{3}{2}} + 6x^{\frac{1}{2}+\frac{3}{2}} + 12x^{1+\frac{3}{2}}$$

$$y = x^{3/2} + 8x^3 + 6x^2 + 12x^{5/2}$$

diff w, r, to, x

$$\frac{dy}{dx} = \frac{d}{dx} (x^{3/2} + 8x^3 + 6x^2 + 12x^{5/2})$$

$$\frac{dy}{dx} = \left( \frac{3}{2} x^{\frac{3}{2}-1} + 8 \times 3x^2 + 6 \times 2x + 12 \times \frac{5}{2} x^{\frac{5}{2}-1} \right)$$

$$\frac{dy}{dx} = \frac{3}{2} x^{1/2} + 24x^2 + 12x + 30x^{3/2} \quad \text{Ans}$$

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Q 2 part B

$$y = \sqrt{\frac{1-x}{1+x}}$$

Solution:  $y = \sqrt{\frac{1-x}{1+x}}$

let  $u = \frac{1-x}{1+x}$

So  $y = \sqrt{u}$

$$y = u^{1/2} \rightarrow (1)$$

~~So~~

$$u = \frac{1-x}{1+x}$$

diff w.r.t, to x

$$\frac{du}{dx} = \frac{d}{dx} \left( \frac{1-x}{1+x} \right)$$

$$\frac{du}{dx} = \frac{(1+x) \frac{d}{dx} (1-x) - (1-x) \frac{d}{dx} (1+x)}{(1+x)^2}$$

$$\frac{du}{dx} = \frac{(1+x)(0-1) - (1-x)(0+1)}{(1+x)^2}$$

$$\frac{du}{dx} = \frac{(1+x)(-1) - (1-x)(1)}{(1+x)^2}$$

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Q2 part B

$$\frac{du}{dx} = \frac{-1-x-1+x}{(1+x)^2}$$

$$\frac{du}{dx} = \frac{-2}{(1+x)^2} \rightarrow (11)$$

now

$$y = u^{1/2}$$

diff w.r.t. to  $u$

$$\frac{dy}{du} = \frac{d}{du} u^{1/2}$$

$$\frac{dy}{du} = \frac{1}{2} u^{1/2-1}$$

$$\frac{dy}{du} = \frac{1}{2} u^{-1/2}$$

$$\frac{dy}{du} = \frac{u^{-1/2}}{2}$$

$$\frac{dy}{du} = \frac{1}{2u^{1/2}}$$

$$\frac{dy}{du} = \frac{1}{2\sqrt{\frac{1-x}{1+x}}}$$

Apply Chain Rule

$$\frac{dy}{dx} = \frac{dy}{du} \cdot \frac{du}{dx}$$

$$= \frac{1}{2\sqrt{\frac{1-x}{1+x}}} \cdot \frac{-2}{(1+x)^2}$$

$$\frac{dy}{dx} = \frac{-1}{(1+x)^2 \sqrt{\frac{1-x}{1+x}}}$$

Ans.

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Q3: part A

$$\int \frac{1}{\sqrt{x^3}} dx$$

Solution:  $\int \frac{1}{\sqrt{x^3}} dx$

$$= \int x^{-3/2} dx$$

$$= \int x^{-3/2} dx$$

$$= \frac{x^{-\frac{3}{2} + 1}}{-\frac{3}{2} + 1} + C$$

$$= \frac{x^{-\frac{3+2}{2}}}{-\frac{3+2}{2}} + C$$

$$= \frac{x^{-\frac{1}{2}}}{-\frac{1}{2}} + C$$

$$= \frac{x^{-1/2}}{-1/2} + C$$

$$= \frac{x^{-1/2}}{-1/2} + C$$

$$= x^{-1/2} \div \left(-\frac{1}{2}\right) + C$$

$$= x^{-1/2} \times \left(-\frac{2}{1}\right) + C$$

$$= -2x^{-1/2} + C$$

$$= \frac{-2}{x^{1/2}} + C$$

$$= \frac{-2}{\sqrt{x}} + C$$

Ans.

Q3

part B

$$\int \frac{1}{(6x+7)^6} dx$$

$$\int (6x+7)^{-6} dx$$

let  $U = 3x-2$

$$\frac{dU}{3} = \frac{dx}{1}$$

$$dx = \frac{dU}{3}$$

$$dx = \frac{1}{3} dU$$

$$= \int U^{-6} \frac{1}{3} dU$$

$$= \frac{1}{3} \int U^{-6} dU$$

$$= \frac{1}{3} \frac{U^{-6+1}}{-6+1} + C$$

$$= \frac{1}{3} \frac{U^{-5}}{-5} + C$$

$$= \frac{-1}{15} U^{-5} + C$$

$$= \frac{-1}{15 U^5} + C$$

$$= \frac{-1}{15 (6x+7)} + C$$

Ans.