

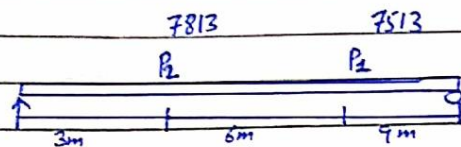
ID: 7313 Ahmad Faraz Khan.

Paper : Engineering Mechanics.

Q1: Find the support reaction - Show all your calculation.

$$P_1 = 200 + 5 \cdot ID, P_2 = 500 + 5 \cdot ID.$$

Sol:

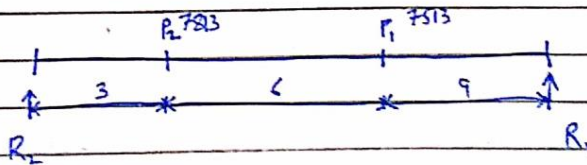


$$P_1 = 200 + 7313$$

$$\Rightarrow P_1 = 7513$$

$$P_2 = 500 + 7313$$

$$P_2 = 7813$$



Equation of equilibrium.

$$\sum F_H = 0 \Rightarrow \sum F_H = 0.$$

$$\sum F_V = 0.$$

$$\sum M = 0.$$

$$\sum F_V = 0.$$

$$\sum M_{R_1} = 0 \quad (\ominus \oplus)$$

$$7513 \times 9 + 15 \times 7813 - R_2 \times 18 = 0.$$

$$R_2 = \frac{67617 + 117195}{9}$$

$$R_2 = \frac{184812}{9} \text{ unit} \cdot \uparrow$$

$$\sum M_R = 0.$$

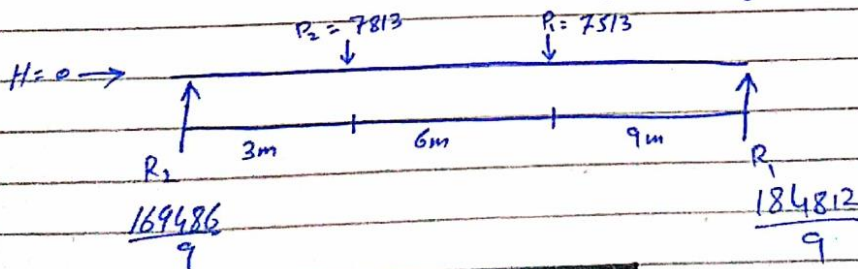
$$3 \times 7513$$

$$-\downarrow + \uparrow \sum F_v = 0.$$

$$R_2 - 7513 - 7813 + \frac{184812}{9} = 0.$$

$$R_2 = \frac{169486}{9} \text{ Unit} \uparrow$$

complet force body diagram.



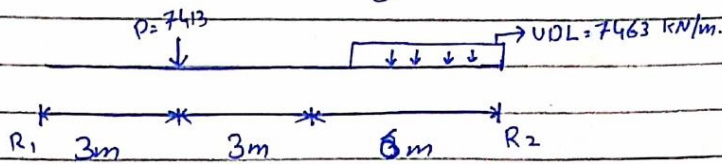
$$R_1 = 20534.66$$

Q.No: R: Draw neat Shear force diagram.  
Show calculation.

$$(100 + 7313), \text{ UDL} = (150 + 7313)$$

Sol:-

Free body diagram.



$$P = 100 + 7313 = 7413.$$

$$\text{UDL} = 150 + 7313 = 7463$$

$$\begin{aligned} \sum F_H &= 0 \\ \sum F_V &= 0 \\ \sum M &= 0 \end{aligned}$$

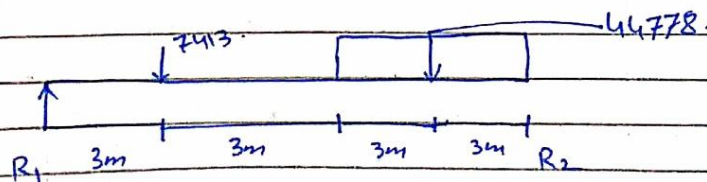
Diagram showing the 6m UDL section. The UDL is represented by four downward arrows. A resultant point load of  $44778$  is shown at the center of the 6m section. The UDL value is  $7463 \text{ kN/m}$ .

$$\sum M_{R_1} = 0 \quad (-) \quad (+)$$

$$-3 \times 7413 - 9 \times 44778 + 12 \times R_2 = 0.$$

To find Point load — (2).

$$\text{Point load} = 7463 \times 6 = 44778.$$





$$\Rightarrow R_2 = \frac{3 \times 7413 + 9 \times 44778}{12}$$

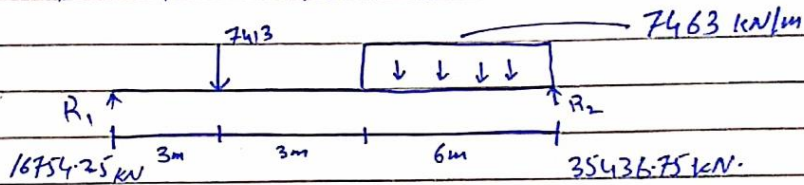
$$R_2 = 35436.75 \text{ kN.}$$

$$\begin{matrix} \text{-ive} \downarrow \\ \text{+ive} \uparrow \end{matrix} \sum F_v = 0.$$

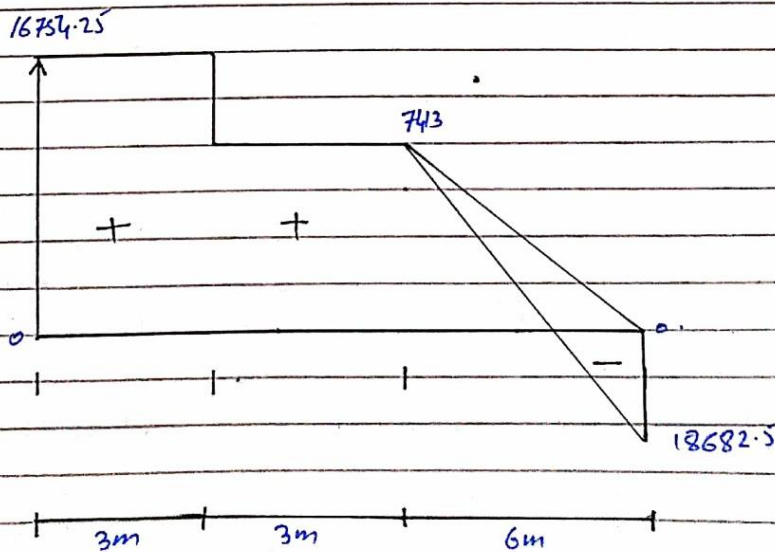
$$R_1 - 7413 - 44778 + 35436.75 = 0$$

$$\Rightarrow R_1 = 7413 + 44778 - 35436.75$$

$$\Rightarrow R_1 = 16754.25 \text{ kN.}$$



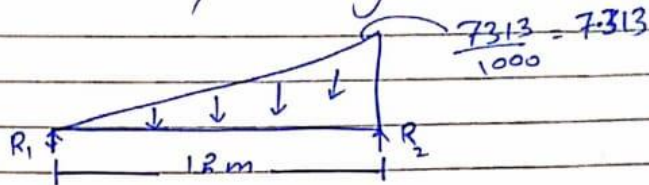
Shear force diagram.



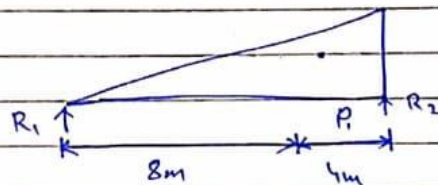
Q3: Draw neat shear force diagram and bending moment diagrams. Show calculations.  
 UVL = Student ID/1000.

Sol:-

Free body diagram.



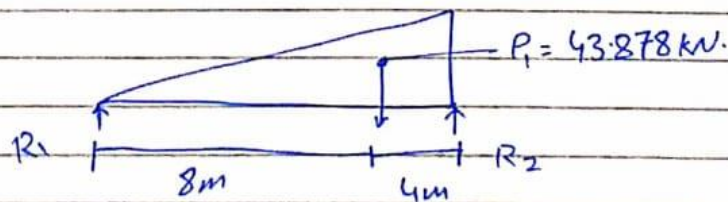
To find Point load.



Point load

$$P_1 = \frac{1}{2} (7.313) \times 12$$

$$P_1 = 43.878 \text{ kN.}$$



To find the Reaction.

$$\sum M_{R_1} = 0.$$

$$-8 \times P_1 + 12 \times R_2 = 0.$$

$$12R_2 = 8P_1$$

$$\Rightarrow 12R_2 = 8(43.878)$$

$$12R_2 = 351.024.$$

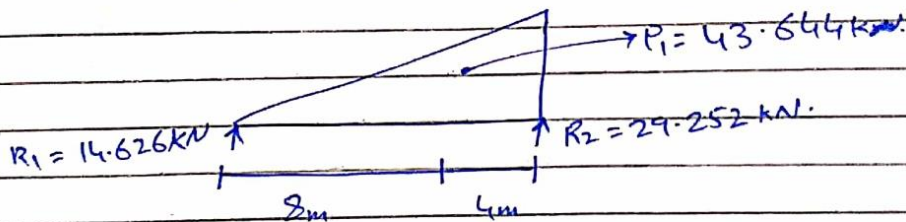
$$R_2 = 29.252 \text{ kN.}$$

$$\sum F_v = 0$$

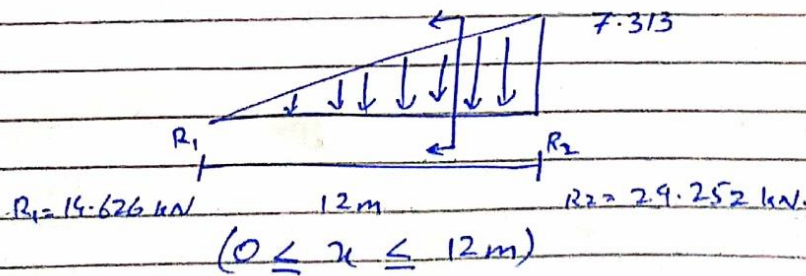
$$R_1 - 43.878 + R_2 = 0.$$

$$R_1 - 43.878 + 29.252 = 0.$$

$$R_1 = 14.626 \text{ kN.}$$

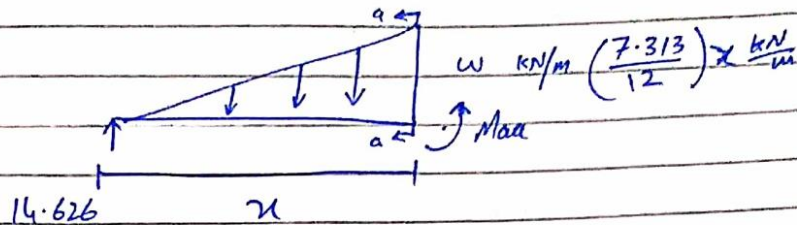


Force shear force diagrams at different section.



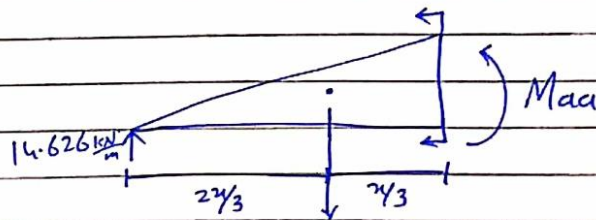


Take section  $a=a$ .



From law of similar triangle.

$$\frac{7.313 \text{ kN/m}}{12 \text{ m}} = \frac{7.313/12}{x}$$



$$M_{aa} + \left(\frac{2x}{3}\right) (P_1 - 14.626)x = 0.$$

$$P_1 = \left(\frac{7.313}{12}\right) \frac{x \times x}{2}$$

$$P_1 = \frac{7.313 x^2}{24}$$

$$\Rightarrow M_{aa} = -\frac{x}{3} \left[ \frac{7.313 x^2}{24} - 14.626x \right]$$

$$M_{aa} = -\frac{x}{3} \left[ 7.313 \frac{x^2}{24} - 14.626x \right]$$

$$M_{aa} = \frac{x^3}{72} \left[ 7.313 - 14.626 \times 3 \right]$$

$$M_{aa} = \frac{-7.313 x^3}{72} + 14.626x \quad \text{--- (a)}$$

at  $x = 0\text{m}$ .

$$\Rightarrow M_{aa} = 0 \text{ kN/m}.$$

at  $x = 12\text{m}$ .

$$\Rightarrow M_{aa} = 0 \text{ kN/m}.$$

Are the points where the bending moment is zero.

$$\downarrow F_v = 0.$$

$$14.626 - 7.313 \frac{x^2}{24} - V = 0.$$

at  $V = 0$ .

$$14.626 - 7.313 - V = 0.$$

$$14.626 - 7.313 \frac{x^2}{24} - 0 = 0.$$

$$\left(\frac{x^2}{24}\right) 7.313 = 14.626.$$

$$0.304 x^2 = 14.626.$$

$$x^2 = \frac{14.626}{0.304}$$

$$x^2 = 48.11$$

$$\sqrt{x^2} = \sqrt{48.11}$$

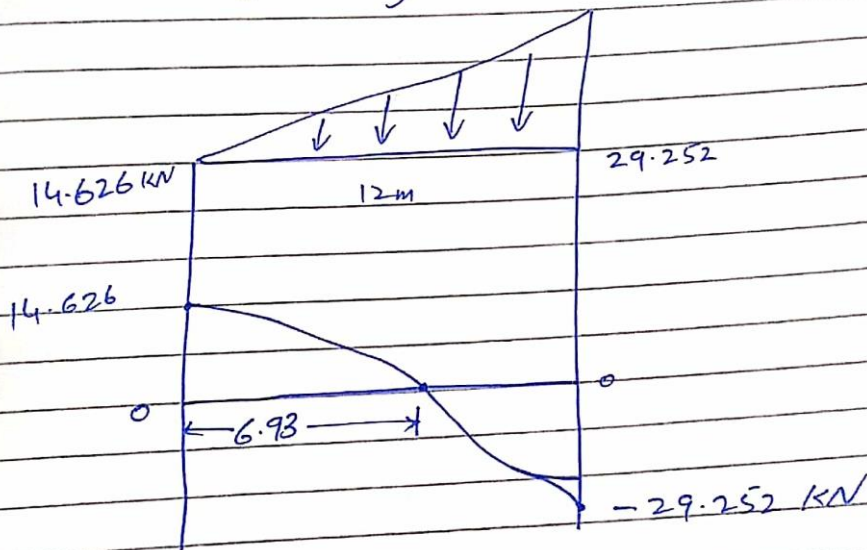
at  $x = 6.93 \quad V = 0$ .



$$M_{aa} = \frac{-7.343 (6.93)^3 + 14.626 (6.93)}{72}$$

$$M_{aa} = 67.55 \text{ kN/m}$$

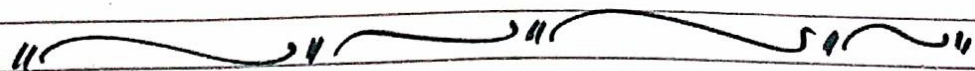
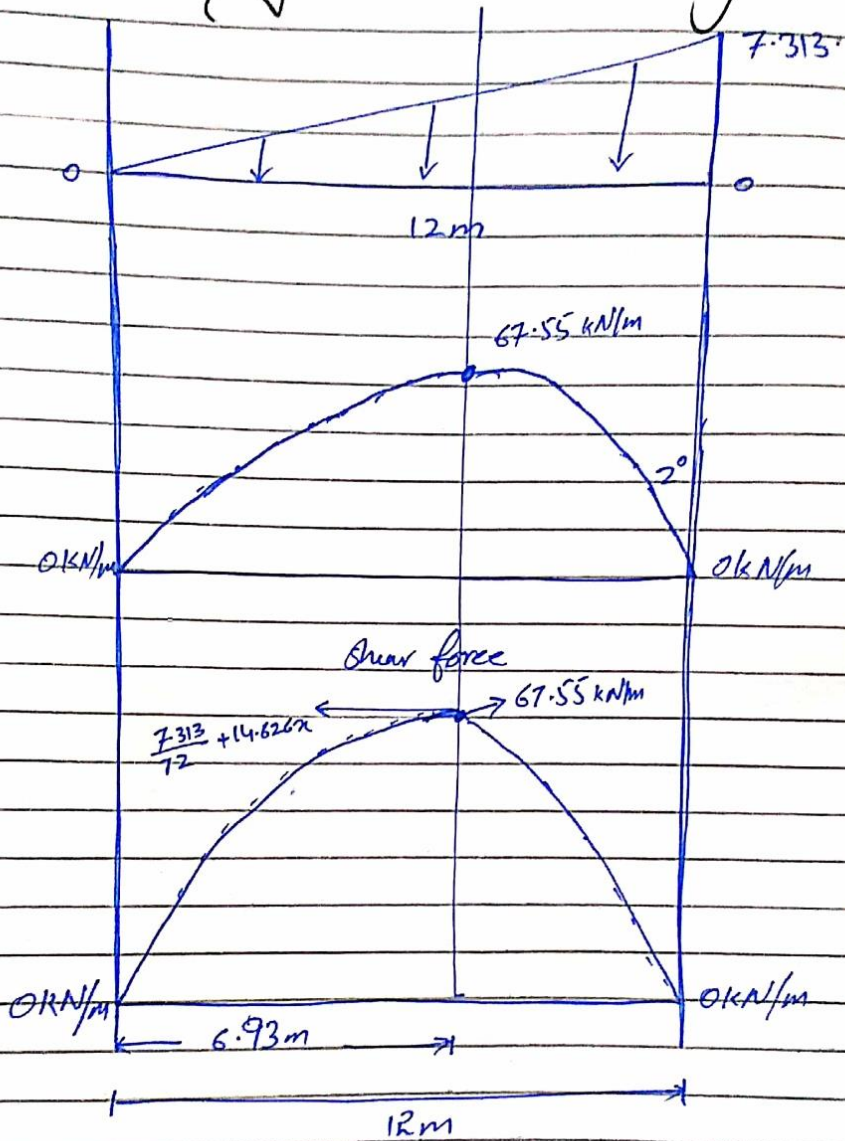
Shear force diagram.



Bending moment diagram.

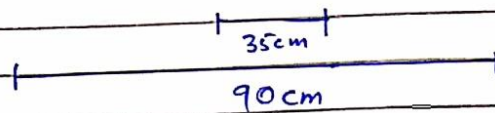
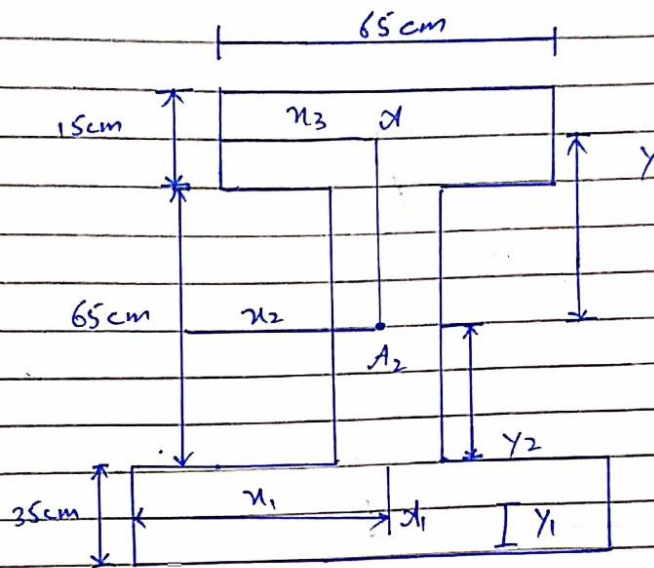
P.T.O.

# Bending Moment Diagram.



Q4: Find the centroid of the given shape.

Sol:-



$$A_1 \quad 3150 \text{ cm}^2 \quad x_1 \quad 45 \quad y_1 = 17.5$$

$$A_2 \quad 2275 \text{ cm}^2 \quad x_2 \quad 45 \quad y_2 = 50$$

$$A_3 \quad 975 \text{ cm}^2 \quad x_3 \quad 45 \quad y_3 = 107.5$$

$$\Sigma A \quad 6400 \text{ cm}^2$$

$$x_c = \frac{A_1 x_1 + A_2 x_2 + A_3 x_3}{A_1 + A_2 + A_3}$$

$$y_c = \frac{A_1 y_1 + A_2 y_2 + A_3 y_3}{A_1 + A_2 + A_3}$$





Q4: b: for mid area - - - - - moduli.

Sol:-

Given data!

$$\text{area} = 65 \times 35.$$

Required = ?

Moment of Inertia = ?

Radius of gyration = ?

Section of moduli = ?

For moment of inertia.

$$I_x = \frac{1}{3} b h^3$$

$$= \frac{1}{3} (65) \times (35)^3$$

$$\frac{1}{3} (65) (35)^3 = 928958 \text{ mm}^4$$

$$I_y = \frac{1}{3} b^3 h$$

$$\frac{1}{3} (65)^3 (35) = 3203958 \text{ mm}^4$$

$$I_{x'} = \frac{1}{12} b h^3$$

$$= \frac{1}{12} (65) (35)^3 = 6635.41 \text{ mm}^4$$

$$I_{y'} = \frac{1}{12} b^3 h.$$

$$\frac{1}{12} (65)^3 (35) = 800989 \text{ mm}^4$$

$$\bar{J}_c = \frac{1}{12} bh (b^2 + h^2)$$

$$\frac{1}{12} (65) (35) ((65)^2 + (35)^2)$$

$$= 1033229.16 \text{ mm}^4$$

|| ~~~~~ || ~~~~~ || ~~~~~ ||



Q5: Explain work, Energy & Power.....  
..... daily life.

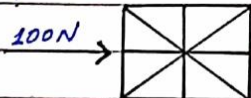
### Work:-

The application of a force through certain distance is known as work. It measured in Joules (J).

Work = Force  $\times$  Distance travelled in direction of force.

### Example:

A box is pushed across a floor by a constant force of 100 N. what is the work done by the force to move the box 5m?



Force = 100 N.  
distance = 5 m.

$$W = Fs$$

$$W = 100 \times 5$$

$$W = 500 \text{ J.}$$

### Energy :-

Energy is the measure of the ability of an object or a system to perform.

There are many types of energy.

### Kinetic Energy :-

Energy of an object due to its speed.

## Gravitational potential energy:

Energy of an object due to position in a gravitational field.

## Elastic Potential energy:

Energy stored when an object is stretched or compressed.

## Chemical energy:-

Energy stored in chemical bonds.

## Nuclear Energy:-

Energy stored in nuclei.

## Heat Energy:-

Hot things have more energy than their cold counterparts.

## Example:-

1 joule is the MKS unit of energy is equal to the force of one newton acting through one meter.

## Energy transfer:

- 1 Gravitational Energy.
- 2 Kinetic Energy
- 3 Light Energy
- 4 Heat Energy.



### Example:-

A supermarket employ lifts a barrel bean tin weight 250 g from the floor to a shelf 2m high. How much gravitational potential energy does it gain?  $g = 9.81 \text{ N/kg}$ .

Soln.

$$\Delta E_p = mgh.$$

$$0.250 \times 9.81 \times 2$$

$$= 4.9 \text{ J}$$

### Power:-

Power is the rate at which work is done, or the rate at which energy is transferred.

Power = work done / time taken.

$$P = \frac{W}{t}$$

where:

Power is measured in watts (W).

Work done or energy transfer is measured in joules (J)

Time is measured in seconds (s).

### Example:-

A crane lifts a load of 1500 kg to a height of 15m at a steady rate, in a time of 2min



what is the power of crane.

$$\Delta E_p = mgh.$$

$$W = 1500 \times 9.81 \times 25$$

$$W = 367875 \text{ J.}$$

$$P = \frac{W}{t} \rightarrow \frac{367875}{120}$$

$$P = 3066 \text{ W.}$$

