

NAME

ASAD-ullah.

Section

B.

ID

7938.

Paper

Fluid mechanics

Q: 1:

①

Part A:

Energy head:

It is the sum of all energy head at a point in a point.

Forms of Energy head:

There are various forms of Energy head, which are in following.

- i) Kinetic head.
- ii) Potential head.
- iii) Pressure head.

Kinetic Head:

It is the kinetic energy per unit weight of the fluid.

Mathematical form:

$$\frac{K.E}{W} = \frac{\frac{1}{2} m v^2}{m g} = \frac{1}{2} \frac{v^2}{g}$$

This is also known as velocity Head.

Unit:

The unit is meter (m)

### Potential Head:

It is the potential energy per unit weight of the fluid.

Mathematically form:

$$\frac{P \cdot E}{w} = \frac{mgh}{mg} = h.$$

### Pressure head:

The vertical height of the free surface above any point in a liquid at rest is pressure head.

OR.

Level of fluid due to pressure exerted by fluid.

Mathematically form: (3)

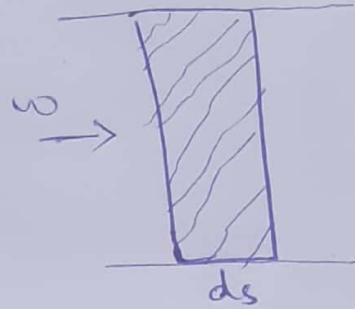
$$\text{Pressure head} = \frac{P \cdot E}{\text{weight}} = \frac{P}{\gamma}$$

OR.

$$= \frac{F \cdot ds}{w}$$

$$= \frac{P \cdot A \cdot ds}{w}$$

$$= \frac{P \cdot v}{w} = \frac{P}{\gamma} \text{ is pressure}$$



Part B:

Hydraulic grade line:

The surface or profile of water flowing in an open channel or a pipe flowing partially full. If a pipe is under pressure, the hydraulic grade line is that level water would rise to in a small, vertical tube connected to the pipe also see energy grade line.

## Hydraulic radius

(4)

The ratio of the cross-sectional area of a channel or pipe in which a fluid is flowing to the wetted perimeter of the conduct.

## Energy grade line:

A line that represented the elevation of energy head (in feet or meters) of water flowing in a pipe, or channel. The line is drawn above the hydraulic grade line a distance equal to the velocity head ( $v^2/2g$ ) of the water flowing at each section or point along the pipe or channel.

5

$$Q = 2 \text{ m}^3/\text{s}$$

Part A:

Given:

$$\text{velocity} = v = 2 \text{ m/s}$$

$$\text{Pressure} = P = 300 \text{ kPa}$$

$$\text{datum} = Z = 5 \text{ m}$$

Sol

$$H = \text{pressure head} + \text{K.E} + \text{P.E}$$

$$H = \frac{P}{\gamma} + \frac{v^2}{2g} + Z$$

$$H = \frac{30 \times 10^3}{9810} + \frac{2^2}{2 \times 9.81} + 5$$

$$H = 35.7849 \text{ m}$$

Q No 2:

(6)

Part B%

Given Data:

$$\text{Diameter} = d_1 = 300 \text{ mm}$$

$$\text{Diameter} = d_2 = 200 \text{ mm}$$

$$\text{Pressure} = P_1 = 300 \text{ kPa} = 300 \times 10^3 \text{ N/m}^2$$

$$P_2 = 120 \text{ kPa} = 120 \times 10^3 \text{ N/m}^2$$

$$\text{Datum} = Z = ?$$

$$Q = \frac{40}{1000} \text{ m}^3/\text{sec.}$$

$$d_1 = 300 \text{ mm} = 0.3 \text{ m}$$

$$d_2 = 200 \text{ mm} = 0.2 \text{ m}$$

Required:

$$Z = ?$$

Soln

$$A_1 = \frac{\pi d_1^2}{4}$$

$$A_1 = \frac{3.14 \times (0.3)^2}{4}$$

$$A_1 = 0.0706 \text{ m}^2$$

$$A_2 = \frac{\pi d_2^2}{4}$$

7

$$A_2 = \frac{3.14 \times (0.2)^2}{4}$$

$$A_2 = 0.0314 \text{ m}^2$$

As we know that

$$Q_1 = v_1 A_1$$

$$v_1 = \frac{Q}{A_1} \quad Q = \frac{40}{1000} = 0.04$$

$$v_1 = \frac{0.04}{0.0706} = \cancel{0.04}$$

$$v_1 = 0.566 \text{ m}^3$$

$$v_2 = \frac{Q}{A_2}$$

$$v_2 = \frac{0.04}{0.03144}$$

$$v_2 = 1.27 \text{ m}^3$$



Now

8

$$\frac{P_1}{\gamma} + \frac{v_1^2}{2g} + Z_1 = \frac{P_2}{\gamma} + \frac{v_2^2}{2g} + Z_2$$

$$Z_1 = 0, \quad \gamma = 9810$$

$$\frac{300 \times 10^3}{9810} + \frac{0.566}{2(9.81)} + 0 = \frac{120 \times 10^3}{9810} + \frac{1.27}{2(9.81)} + Z_2$$

$$30.60 + 0 = 12.314 + Z_2$$

$$\Rightarrow \boxed{Z_2 = 18.286 \text{ m}}$$

Q 3%

(9)

→ Given Data:

length of Pipe =  $L = 500\text{ m}$ .

Diameter =  $d = 0.2\text{ m}$ .

specific gravity of oil =  $0.9\text{ m}$

Flow rate =  $Q = 0.06\text{ m}^3/\text{s}$ .

viscosity =  $\mu = 6 \times 10^{-5}\text{ N}\cdot\text{s}/\text{m}^2$

Required:

Pressure loss =  $\Delta P = ?$

As we know

$$f \left( 0.0032 + \left( \frac{0.221}{R^{0.237}} \right) \right)$$

where  $R = \text{Reynold's no}$  & is give as

$$R = \frac{v \times d}{\nu} \rightarrow \textcircled{1}$$

$$\& \quad \nu = \frac{\mu}{\rho} = \frac{6 \times 10^{-5}}{900}$$

$$\nu = 6.67 \times 10^{-8}\text{ m}^2/\text{s}$$

and  $v = \frac{Q}{A}$

For circular pipe

$$A = \frac{\pi d^2}{4}$$

$$V = \frac{0.06}{0.031} = \frac{\pi}{4} (0.02)^2 \quad (10)$$

$$A = 0.031 \text{ m}^2$$

$$V = \frac{0.06}{0.031}$$

$$V = 1.95 \text{ m/s}$$

no eq (1)

$$R = \frac{1.95 \times 0.2}{6.67 \times 10^{-5}} = 5.73 \times 10^6$$

now

$$f = 0.0032 + \frac{0.221}{(5.73 \times 10^6)^{0.237}}$$

$$f = 8.79 \times 10^{-3}$$

$$\boxed{f = 0.00879}$$

now from Bernoulli's equation

$$\text{Head loss} = h_L = \frac{f L V^2}{2gD} \rightarrow (11)$$

Putting the value in eq (11)

(1)

$$h_L = \frac{(0.00879 (500) (1.95)^2)}{2(9.81)(0.2)}$$

$$h_L = 4.259 \text{ m}$$

Now to find pressure loss due Friction

Pressure head formula is used

$$h_L = \frac{\Delta P}{\rho g}$$

$$\Delta P = h_L \times \rho g$$

Putting the value.

$$\Delta P = 4.259 \times 900 \times 9.81$$

$$\Delta P = 37602.7 \text{ Pa}$$

$$\Delta P = 37.602 \text{ kPa}$$