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Subject

Probability &
Statistics.

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Submitted To

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QNO # 01Solution:-

X	Y	XY	X ²
53	20	1060	2809
62	32	1984	3844
57	45	2565	3249
71	60	4260	5041
78	80	6240	6084
51	100	5100	2601
86	120	10320	7396
87	140	12180	7569
96	160	15360	9216
91	180	16380	8281
94	200	18800	8836
94	210	11280	8836
Σ 920	Σ 1347	Σ 105529	Σ 73762

$$y = a + bx \rightarrow (i)$$

$$a = \bar{y} - b\bar{x} \rightarrow (ii)$$

So

$$\bar{y} = \frac{\sum y}{n} = \frac{1347}{12} = 112.25 \rightarrow (iii)$$

$$\bar{x} = \frac{\sum x}{n} = \frac{920}{12} = 76.66 \rightarrow (iv)$$

where

$$b = \frac{n \sum xy - \sum x \sum y}{n \sum x^2 - (\sum x)^2}$$

$$b = \frac{12(105529) - 920 \times 1347}{12(73762) - 846400}$$

$$b = 0.699 \rightarrow (v)$$

Putting equation (iii), (iv) & (v)
in equation (ii)

$$a = \bar{y} - b\bar{x}$$

$$a = 112.25 - 0.699 \times 76.66.$$

$$a = 58.664.$$

Hence the derived estimated
regression line y and x is

$$\hat{y} = 58.66 + 0.699x$$

The estimated regression
co-efficient, $b = 0.699$, which
indicate that the value of y
increases by 0.699 unit for a unit increase
in x .

★ QNO # 02 (a) ★

Solution :-

$$n(S) = \binom{13}{3} = 286$$

let A = Donate all ball are of different colour.

$$n(A) = \binom{4}{1} \binom{4}{1} \binom{5}{1} = 4 \times 4 \times 5 = 80$$

$$P(A) = \frac{n(A)}{n(S)} = \frac{80}{286} = 0.28.$$

$$2 \times 2 \times 2 = 8$$

$$3 \times 2 \times 2 = 12$$

$$3 \times 3 \times 2 = 18$$

even \times even \times even = even

odd \times even \times even = even

odd \times odd \times even = even

Interpretation :-

There are 28% chances that all the ball are different colours.

ii) let B = Donate all the ball of same colour.

$$n(B) = \binom{4}{3} \text{ or } \binom{4}{3} \text{ or } \binom{5}{3}$$

$$\approx \binom{4}{3} + \binom{4}{3} + \binom{5}{3} = 4 + 4 + 10 = 18.$$

$$P(B) = \frac{n(B)}{n(S)} = \frac{18}{286} = 0.063.$$

Interpretation:-

There are 6.3% chances
that all the balls of same colour.

★ ————— ★

QNO # 02 (b).

Solution:-

$$n(S) = \binom{12}{4} = 495$$

Let $A =$ denote the event that exactly one egg is bad.

$$n(A) = \binom{2}{1} \binom{10}{3} = 2 \times 120 = 240$$

$$P(A) = \frac{n(A)}{n(S)} = \frac{240}{495} = 0.48.$$

Interpretation:-

There are 48% chances that exactly one egg is bad.

(ii) Let $B =$ be the event that at least one bad egg is selected.

$$n(B) = \binom{2}{1} \binom{10}{3} + \binom{2}{2} \binom{10}{2}$$

$$= 2 \times 120 + 1 \times 45 = 240 + 45 \\ = 285$$

$$P(B) = \frac{n(B)}{n(S)} = \frac{285}{495} = 0.58$$

Interpretation:-

There are 58% chances
at least one bad egg is
Selected.

$$\text{Range} = X_m - X_0$$

$$\begin{aligned}\text{Range of A} &= X_m - X_0 \\ &= 199 - 6 \\ &= 193.\end{aligned}$$

$$\begin{aligned}\text{Range of B} &= X_m - X_0 \\ &= 51 - 3 \\ &= 48\end{aligned}$$

$$\begin{aligned}\text{Range of C} &= X_m - X_0 \\ &= 51 - 4 \\ &= 47.\end{aligned}$$

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Batsman A		Batsman B		Batsman C	
X	X ²	Y	Y ²	Z	Z ²
12	144	47	2209	15	225
15	225	12	144	23	529
6	36	76	5776	52	2704
73	5329	48	2304	4	16
51	2601	51	2601	51	2601
199	39601	37	1369	74	5476
36	1296	48	2304	52	2704
84	7056	13	169	13	169
29	841	3	9	4	16
$\Sigma X = 512$	$\Sigma X^2 = 57178$	$\Sigma Y = 339$	$\Sigma Y^2 = 16901$	$\Sigma Z = 312$	$\Sigma Z^2 = 15016$

Batsman A =

$$\bar{x} = \frac{\Sigma X}{n} = \frac{512}{10} = 51.2$$

Batsman B :-

$$\bar{Y} = \frac{\sum Y}{n} = \frac{339}{10} = 33.9$$

Batsman C :-

$$\bar{Z} = \frac{\sum Z}{n} = \frac{312}{10} = 31.2$$

For Batsman A :-

$$S_x = \sqrt{\frac{\sum x^2}{n} - \left(\frac{\sum x}{n}\right)^2}$$
$$= \sqrt{\frac{57178}{10} - \left(\frac{512}{10}\right)^2}$$

$$S_x = 55.64.$$

$$C.V = \frac{55.64 \times 100}{51.2}$$

$$C.V = 108.76\%$$

For Batsman B :-

$$S_y = \sqrt{\frac{\sum y^2}{n} - \left(\frac{\sum x}{n}\right)^2}$$

$$= \sqrt{\frac{16901}{10} - \left(\frac{339}{10}\right)^2}$$

$$= 23.25\%$$

$$C.V = \frac{23.25 \times 100}{33.9}$$

$$C.V = 68.58\%$$

For Batman C:-

$$S_z = \sqrt{\frac{\sum z^2}{n} - \left(\frac{\sum z}{n}\right)^2}$$

$$S_z = \sqrt{\frac{15016}{10} - \left(\frac{312}{10}\right)^2}$$

$$S_z = 22.98$$

$$C.V = \frac{S_z}{\bar{z}} = \frac{22.98}{31.2} \times 100$$

$$C.V = 73.65\%$$

Batsman B is more consistent
as its value of Co-efficient
of Variance is smallest

Compare A with B.

B is consistent

Compare B with A.

B is more consistent

Compare A with C.

C is more consistent.