

## Department of Electrical Engineering

### Assignment

Date: 07/05/2020

### Course Details

Course Title: Electrical Network Analysis  
 Instructor: \_\_\_\_\_

Module: 4th  
 Total: 20  
 Marks: \_\_\_\_\_

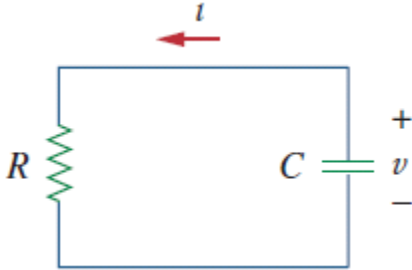
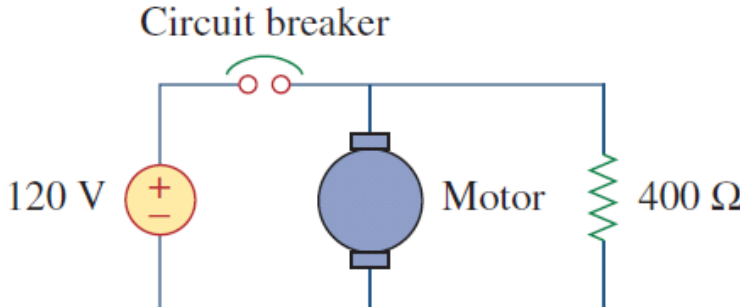
Submission Deadline: 05/06/2020

### Student Details

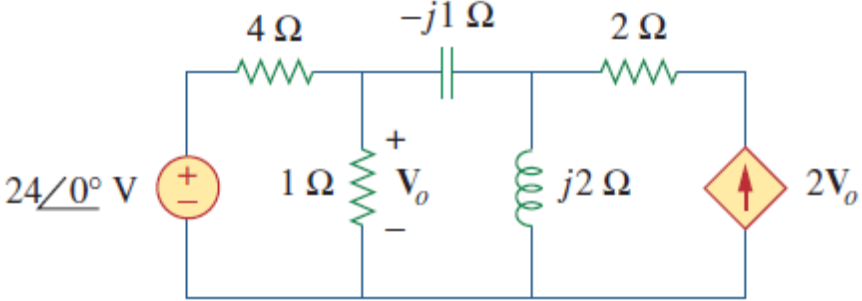
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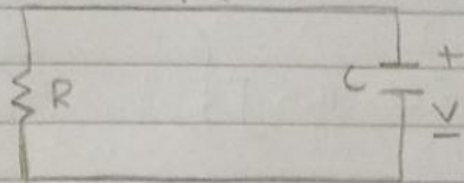
Q1.	<p>For the circuit in Fig. 1, if <math>v = 10e^{-4t}</math> V and <math>I = 0.2e^{-4t}</math>, <math>t &gt; 0</math></p> <p>(a) Find <math>R</math> and <math>C</math>.                      (b) Determine the time constant.                      (c) Calculate the initial energy in the capacitor.                      (d) Obtain the time it takes to dissipate 50 percent of the initial energy.</p> <div style="text-align: center;">  <p>Figure 1</p> </div>	<p>Marks 02</p> <p>CLO 01</p>
Q2.	<p>A 120-V dc generator energizes a motor whose coil has an inductance of 50 H and a resistance of 100 <math>\Omega</math>. A field discharge resistor 400 <math>\Omega</math> of is connected in parallel with the motor to avoid damage to the motor, as shown in Fig. 2. The system is at steady state. Find the current through the discharge resistor 100 ms after the breaker is tripped.</p> <div style="text-align: center;">  <p>Figure 2</p> </div>	<p>Marks 03</p> <p>CLO 03</p>

Q3.	<p>The responses of a series <math>RLC</math> circuit are  <math>v_c(t) = 30 - 10e^{-20t} + 30e^{-10t}</math> V  <math>i_L(t) = 40e^{-20t} - 60e^{-10t}</math> mA  where <math>v_c</math> and <math>i_L</math> are the capacitor voltage and inductor current respectively.  Determine the values of <math>R</math>, <math>L</math>, <math>C</math></p>	<p>Marks 02 CLO 01</p>
Q4.	<p>The circuit in Fig. 3 is the electrical analog of body functions used in medical schools to study convulsions. The analog is as follows:  <math>C_1</math> = Volume of fluid in a drug  <math>C_2</math> = Volume of blood stream in a specified region  <math>R_1</math> = Resistance in the passage of the drug from the input to the blood stream  <math>R_2</math> = Resistance of the excretion mechanism, such as kidney, etc.  <math>v_0</math> = Initial concentration of the drug dosage  <math>v(t)</math> = Percentage of the drug in the blood stream</p> <p>Find <math>v(t)</math> for <math>t &gt; 0</math> given that <math>C_1 = 0.5 \mu\text{F}</math>, <math>C_2 = 5 \mu\text{F}</math>, <math>R_1 = 5 \text{M}\Omega</math>, <math>R_2 = 2.5 \text{M}\Omega</math> and <math>v_0 = 60u(t)</math> V</p> <div data-bbox="532 745 1198 1008" data-label="Diagram"> </div> <p style="text-align: center;">Figure 3</p>	<p>Marks 03 CLO 03</p>
Q5.	<p>A power transmission system is modeled as shown in Fig. 4. Given the source voltage and circuit elements  Source voltage <math>V_s = 115 \angle 0</math> V,  Source impedance <math>Z_s = 1 + j0.5 \Omega</math> ,  Line impedance <math>Z_l = 0.4 + j0.3 \Omega</math> ,  Load impedance <math>Z_L = 23.2 + j18.9 \Omega</math> ,  find the load current <math>I_L</math></p> <div data-bbox="516 1312 1201 1690" data-label="Diagram"> </div> <p style="text-align: center;">Figure 4</p>	<p>Marks 02 CLO 03</p>

Q 6	<p>For the circuit in Fig. 5, find the average, reactive, and complex power delivered by the dependent current source.</p>  <p style="text-align: center;">Figure 5</p>	Marks 03 CLO 03
Q 7	<p>A balanced Y-load is connected to a 60-Hz three-phase source with <math>V_{ab} = 240 \angle 0^\circ</math> V. The load has <math>\text{pf} = 0.5</math> lagging and each phase draws 5 kW. (a) Determine the load impedance <math>Z_Y</math>. (b) Find <math>I_a</math>, <math>I_b</math>, and <math>I_c</math>.</p>	Marks 5 CLO02

Q1: For the circuit in fig #1  
if  $v = 10e^{-4t}$   $t > 0$

a) find  $R$   $\tau$   $C$  (b) — (c) — (d) —  
50% of the initial energy



STEP 1

(A)

$$\tau = RC = \frac{1}{4}$$

$$\Rightarrow -1 = C \frac{dv}{dt}$$

$$\Rightarrow -0.2e^{-4t} = C(10)(-4)e^{-4t}$$

$$\Rightarrow C = 5 \text{ mF}$$

$$R = \frac{1}{4C} = \boxed{50 \Omega}$$

STEP # 2:

$$B \quad \tau = RC = \frac{1}{4} = 0.250$$

STEP #3:

$$W_c(0) = \frac{1}{2} C V^2$$

$$\Rightarrow \frac{1}{2} (5 \times 10^{-3}) (100)$$

$$\Rightarrow 250 \text{ mJ}$$

STEP #4:

$$(B) W_R = \frac{1}{2} \times \frac{1}{2} C V_0^2$$

$$\Rightarrow \frac{1}{2} C V_0^2 (1 - e^{-2t})$$

$$0.5 = 1 - e^{-8t} \Rightarrow e^{-8t_0} = \frac{1}{2}$$

OR

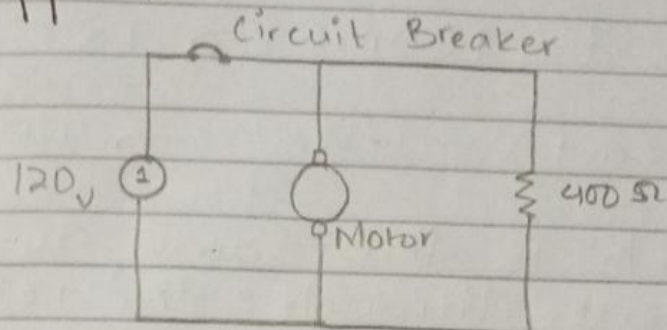
$$e^{8t} = 2$$

$$t_0 = \frac{1}{8} (\ln 2)$$

$$\Rightarrow 86.6 \text{ ms}$$



Q2 A 120-v dc generator energize a motor coil — the breaker is tripped?



STEP #1.

Let the inductor current for  $t < 0$

$$i(0) = \frac{120}{100} = 12$$

$$\Rightarrow \frac{6}{5} = 1.2 \text{ SA}$$

For  $t > 0$  we have an RL circuit

$$\tau = \frac{L}{R} = \frac{50}{100 + 400}$$

$$= \frac{50}{500} = \frac{1}{10}$$

$$\Rightarrow \frac{1}{10} = 0.1$$

$$i(\infty) = 0$$



$$i(t) = i(\infty) + [i(0) - i(\infty)]e^{-t/\tau}$$

$$i(t) = 1.2 e^{-10t}$$

$$\text{At } t = 100\text{ms} = 0.1\text{ s}$$

$$i(0.1) = 1.2e^{-1} = 0.441\text{ A}$$

Which is the same as the current through the resistor

STEP #2

(B)

$$\tau = R_{\text{eq}} C = 60\mu\text{s}$$

An integrator

$$T < 0.1 \quad \tau = 60\mu\text{s}$$

$$T_{\text{Max}} = 60\mu\text{s}$$

x \_\_\_\_\_ x

### QUESTION # 3.

The response of Series RLC Circuit the value of  $R, L, C$

STEP # 1:

Series RLC circuit.

$$V(t) = 30 - 10e^{-20t} + 30e^{-10t} \text{ V}$$

$$v(t) = v_i + A_1 e^{s_1 t} + A_2 e^{s_2 t} \quad [\alpha > \omega]$$

$$40e^{-20t} - 60e^{-30t} \text{ mA}$$

$$\Rightarrow i(t) = A_1 e^{s_1 t} + A_2 e^{s_2 t} \quad [\alpha > \omega]$$

Comparing these eq.... we get

$$v_s = 30$$

$$A_1 = -10 ; A_2 = 30 ;$$

$$s_1 = -20 ; s_2 = -10 \rightarrow (a)$$

$$A_1' = 40 ; A_2' = -60 ;$$

$$s_1' = -20 ; s_2' = -10 \rightarrow (b)$$

STEP # 2

Now eq (a) & (b)

$$s_1 = -\alpha + \sqrt{\alpha^2 - \omega^2} \quad \text{And} \quad s_2 = -\alpha - \sqrt{\alpha^2 - \omega^2}$$

$$s_1 + s_2 = -2\alpha \quad \text{If} \quad s_1, s_2 = \alpha^2$$



$$\left[ \text{where } \alpha = \frac{R}{2L} ; \omega_0 = \frac{1}{\sqrt{LC}} \right]$$

$$\Rightarrow -30 = -2\alpha$$

$$\Rightarrow \alpha = 15$$

$$200 = \alpha^2 \Rightarrow \frac{1}{LC} = 200 \rightarrow (d)$$

STEP #3

$$i(t) = C \frac{dv(t)}{dt} = C [200e^{-20t} - 300e^{-30t}]$$

$$(A_1' e^{s_1 t} + A_2' e^{s_2 t}) \times 10^{-3} \text{ A} = C [200e^{-20t} - 300e^{-30t}]$$

OR

$$[s_1 = s_1' ; s_2 = s_2']$$

$$\Rightarrow 200C = A_1' = 40 \times 10^{-3}$$

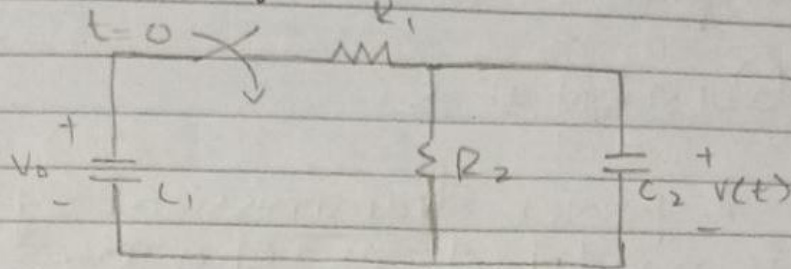
$$\Rightarrow C = 200 \times 10^{-6} \text{ F} \Rightarrow C = \boxed{200 \mu\text{F}}$$

Using eq (c) & (d)

$$L = \frac{1}{200C} = \frac{1}{200 \times 200 \times 10^{-6}} \Rightarrow L = \boxed{25 \text{ H}}$$

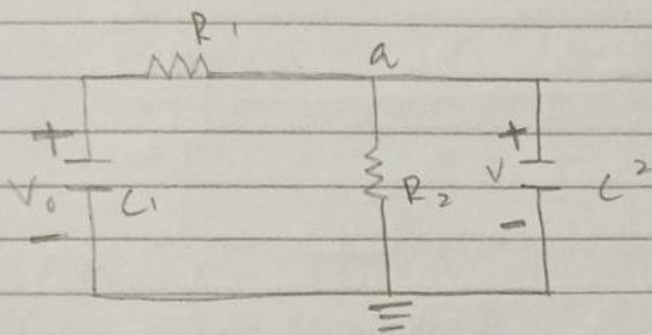
$$\& \text{ } R = 30L = 30 \times 25 = \boxed{750 \Omega}$$

1. The circuit in Fig. 3 is the electrical analogy of body function?



For  $t=0$ ,  $v(0)=0$

For  $t > 0$  the circuit is shown below.



$$V_0 - v/R_1 = (v/R_2) + C_2 dv/dt$$

$$V_0 = v(1 + R_1/R_2) + R_1 C_2 dv/dt$$

$$60 = (1 + 5/2.5) + (5 \times 10^6 \times 5 \times 10^{-6}) \frac{dv}{dt}$$

$$60 = 3v + 25 dv/dt$$

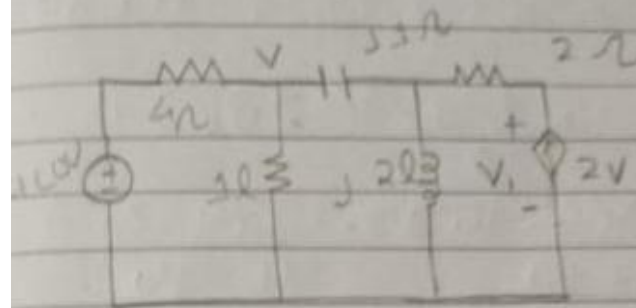
$$v(t) = V_s + [Ae^{-3t}/25]$$

$$3V_s = 60 \text{ volts } V_s = 20.$$





For the circuit in Fig #5  
 Find the average power  
 dependent current source?



Consider the circuit as shown  
 At node 0

$$\frac{24 - V_0}{4} = \frac{V_0}{3} + \frac{V_0 - V_1}{5}$$

$$24 = (5 + j4)V_0 - j4V_1 \rightarrow (1)$$

At node 1.

$$\frac{V_0 - V_1}{-j} + 2V_0 = \frac{V_1}{j2}$$

$$V_1 = (2 - j4)V_0 \rightarrow (2)$$

Substituting (2) into (1)

$$24 = (5 + j4 - j8 - 16)V_0$$

$$V_0 = \frac{-24}{11 + j4}, \quad V_1 = \frac{(-24)(2 - j4)}{11 + j4}$$

Voltage across the dependent  
 source is

$$V_2 = V_1 + (2)(2V_0) = V_1 + 4V_0$$

$$V_2 = \frac{-24}{11+j4} (2 - j4) = \frac{(-24)(6-j4)}{11+j4}$$

$$S = \frac{1}{2} V_2 I = \frac{1}{2} V_2 (2V_0)$$

$$S = \frac{(-24)(6-j4)}{11+j4} \cdot \frac{-24}{11-j4}$$

$$= \left( \frac{576}{137} \right) (6-j4)$$

$$S = 25.23 - j16.82 \text{ VA}$$

x

x



## QUESTION # 7.

A balance  $\Delta$ -load to a 60Hz  
three phase ----- phase draw  
5KW.

(a) determine the load impedance

(b) Find  $I_a$   $I_b$   $I_c$

(a) STEP # 1.

$$|V_{\Delta}| = \sqrt{3}V_p = 240 \rightarrow V_p = \frac{240}{\sqrt{3}} = 138.56$$

$$V = V_p \angle -30^\circ$$

$$P_f = 0.5 = \cos \phi$$

$$P = S \cos \phi \rightarrow S = \frac{P}{\cos \phi} = \frac{5}{0.5} = 10 \text{ KVA}$$

$$Q = S \sin \phi = 10 \sin 60 = 8.66$$

$$S_p = 5 + j8.66 \text{ KVA}.$$

But

$$S_p = \frac{V_p^2}{Z_p} \rightarrow Z_p = \frac{V_p^2}{S_p} = \frac{138.56^2}{(5 + j8.66) \times 10^3}$$

(B) STEP 2 :

$$I_a = \frac{V}{Z_r} = \frac{138.56 \angle -30^\circ}{0.96 + j1.6627} = 72.17 \angle 90^\circ \text{ A}$$

$$I_b = I_a \angle -120^\circ = 72.17 \angle -210^\circ \text{ A}$$

$$I_c = I_a \angle +120^\circ = 72.17 \angle 30^\circ \text{ A.}$$

x ————— x