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Section "B"

Subject: D.E

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FORMATION OF PARTIAL DIFFERENTIAL EQUATIONS.

⇒ It is defined as an equation involving two or more independent variable like x, y, z, \dots & dependent variable like u and its partial derivatives,

⇒ Partial differential Equation can be formed either by elimination of the arbitrary constants OR by the elimination of arbitrary function from a relation involving three or more variables.

GENRA FORM.

⇒ The General form of a first order partial differential equation is

$$F(x, y, z, \frac{\partial z}{\partial x}, \frac{\partial z}{\partial y}) = F(x, y, z, p, q) = 0$$

where x, y are two independent variables

z is the dependent variable and

$$p = z_x \quad \text{and} \quad q = z_y$$

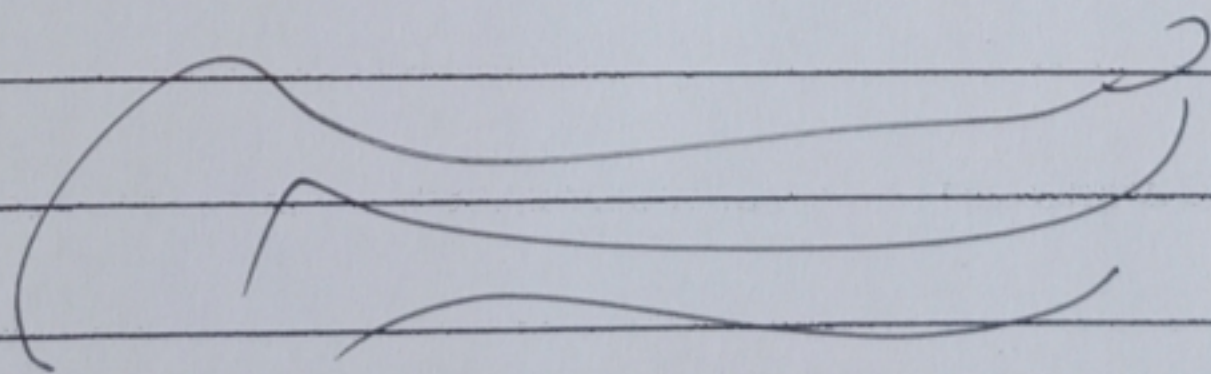
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INVENTION OF DIFFERENTIAL EQUATION.

⇒ In Mathematics the history of D.E traces the development of "Differential Equation" from Calculus, which itself was independently invented by English physicist Newton and German mathematician Gottfried Leibniz.

⇒ The history of the subject of D.E in concise form a synopsis of the recent article "The History of D.E 1670-1950"

⇒ D.E began with Leibniz. The Bernoulli brothers and other from the 1680's not long after Newton's functional equation in the 1670's



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Application of partial differential Equations.

PDES are used to model many system in many different fields of Science and Engineering.

Important Examples: \rightarrow

\Rightarrow Laplace Equation.

\Rightarrow Heat Equation.

\Rightarrow Wave Equation.

LAPLACE EQUATION \Rightarrow

\Rightarrow Laplace Equation is used to describe of heat in a body

\Rightarrow Also used to describe the steady state distribution of electrical charge in a body.

$$\frac{\partial^2 u(x, y, z)}{\partial x^2} + \frac{\partial^2 u(x, y, z)}{\partial y^2} + \frac{\partial^2 u(x, y, z)}{\partial z^2} = 0$$

Heat Equation: \rightarrow (4)

\Rightarrow The function $u(x, y, z, t)$ is used to represent the temperature at time t in a physical body at a point with coordinate (x, y, z) .

\Rightarrow α is the Thermal diffusivity, it is sufficient to consider the case $\alpha = 1$

$$\frac{\partial u(x, y, z, t)}{\partial t} = \alpha \left[\frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} + \frac{\partial^2 u}{\partial z^2} \right]$$

WAVE EQUATION: —

The function $u(x, y, z, t)$ is used to represent the displacement at time t of a particle whose position at rest is (x, y, z) .

\Rightarrow The constant (c) represent the propagation speed of the wave.

$$\frac{\partial^2 u(x, y, z, t)}{\partial t^2} = c^2 \left[\frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} + \frac{\partial^2 u}{\partial z^2} \right]$$

* Application in ⁽⁵⁾ daily life:

⇒ Partial derivatives are used in the basic laws of physics for example Newton laws of Linear motion, Maxwell's equation of Electromagnetism and Einstein equation in General Relativity.

* In Economiss field: ⇒

⇒ In the field of economics we used Partial differential equation to check what happen to other variable keeping one variable constant.

* Application in the field of Civil Engineering: ⇒

⇒ Differential equation are the true essence of the physical world.

They are used to describe the physical phenomenon which is encountered at microscopic as well as macroscopic level.

⇒ Differential Equation are extensively involved Civil Engineering.

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⇒ Civil Engineering Mostly Concerned With Building Structure and Geometrical Shapes, So any work revolved around modeling structure, fluids, pollutants and more can be modeled using differential equations, if you have any complicated geometries, which most realistic problems have you'll likely to use the said differential equations in an approximation frame work like that of finite (difference volume element) to approximately figure out a solution to a problem you care about.

* In the field of Mechanical Engineering:

* There are different order of the partial differential equation describing the rate of change of a function. That representing the Real life qualities.

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* The use of the separation of variable technique to solve partial differential equation relating to heat conduction in solids and the vibration of solid in multidimensional system.

