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Section

A

Subject

PRCD I

Submitted
to

Sir Fawad

Semester

6th

Given Data

3 equal span concrete slab

Clear span b/w supports = 15 ft

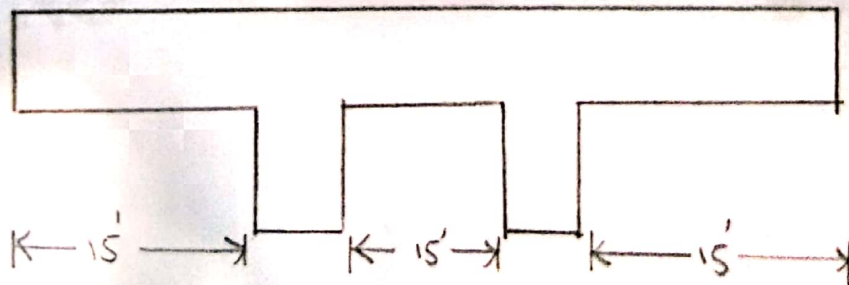
Factored live load = 1600 lb/ft^2

Service floor finish load = 20 lb/ft^2

$$f'_c = 4000 \text{ psi}$$

$$f_y = 40 \text{ ksi}$$

Solution



Step # 01 Minimum thickness

By Using formula

$$t_{\min} = L/28 = 15/28 = 6.4 \approx 6.5$$

$$P = 2$$

As $f_y \rightarrow 40 \text{ ksi}$

So we will multiply a factor with this thickness

$$\begin{aligned} \text{Factor} &= \left[0.4 + \frac{f_y}{100} \right] \\ &= 0.4 + \frac{40}{100} = 0.8 \end{aligned}$$

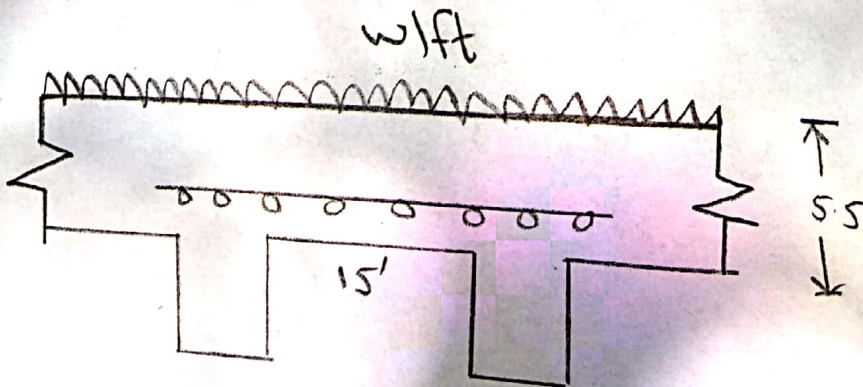
Hence the minimum thickness will be

$$6.5 \times 0.8$$

$$t_{\min} = 5.2 \approx 5.5''$$

$$t_{\min} = 5.5''$$

Step #2 Effective depth



By formula

$$P = 3$$

By formula

$$d = t - \text{clear cover} - \frac{1}{2} (\text{dia of main bar})$$
$$= 5.5 - 0.75 - \frac{1}{2} \left(\frac{5}{8} \right)$$

$$\boxed{d = 4.5''}$$

Step #03 (self weight of slab)

By formula

$$t/12 + \gamma_{\text{concrete}}$$

$$= \frac{5.5}{12} \times 150$$

$$= \boxed{68.75 \text{ lb/ft}^2}$$

Step #04 (Total Factored load)

$$\text{Factored live load} = 160 \text{ lb/ft}^2$$

So the factored Dead load will be

IV

$$P = 4$$

$$D.L = 1.2(20 + 68.75) = 106.5 \text{ lb/ft}^2$$

$$\text{Total factored load} = D.L + L.L$$

$$= 106.5 + 160$$

$$= 266.5 \text{ lb/ft} = 0.2665 \text{ k/ft}^2$$

Step #05 Ultimate moment

By using formula

$$M_u = \frac{w_u \times L^2}{8} \times 12 = \frac{0.2665 \times (15)^2}{8} \times 12$$

$M_u = 89.94 \text{ kip-inches}$

Step #06 Area of Steel For main Bar by trial ϵ_s

Repeat Method

Trial #01

let depth of Compressive block
 $a = 0.2 \times t$

$$P = 5$$

$$0.2 \times 5.5 = 1.1''$$

$$A_{st} = \frac{M_u}{\phi \times f_y \times (d - a/2)} = \frac{89.94}{0.90 \times 40 \times (4.5 - \frac{1.1}{2})}$$

$$A_{st} = 0.63 \text{ in}$$

Trail #02

$$a = \frac{A_{st} \times f_y}{0.85 \times f'_c \times b} = \frac{0.63 \times 40}{0.85 \times 4 \times 12} \Rightarrow 0.62 \text{ in}^2$$

$$A_{st} = \frac{M_u}{\phi \times f_y \times (d - \frac{a}{2})} = \frac{89.94}{0.90 \times 40 \times (4.5 - \frac{0.6}{2})}$$

$$A_{st} = 0.59 \text{ in}^2$$

Trail #03

$$a = \frac{0.59 \times 40}{0.85 \times 4 \times 12} = 0.57''$$

$$A_{st} = \frac{89.94}{0.90 \times 40 \times (4.5 - \frac{0.57}{2})} = 0.59 \text{ in}^2$$

$$p = 6$$

So we will use $A_{st} = 0.59 \text{ in}^2$

Step #07

Area of steel for distribution reinforcement

By formula

$$A_{min} = 0.002 \times b \times t \rightarrow (\text{For Grade 40 steel})$$
$$= 0.002 \times 12 \times 5.5 = 0.132 \text{ in}^2$$

Step #08

Spacing for main bars

By formula

$$\text{Spacing} = \frac{A_b}{A_{st}} \times 12$$

We use #6 bar dia $(\frac{6}{8})''$

$$\text{Area} = \frac{\pi}{4} \left(\frac{6}{8}\right)^2 = 0.442 \text{ in}^2$$

Step #09

Spacing for distribution bars

Spacing $\frac{A_b}{A_{st}}$ we use #5 bar so

$$P = 7$$

$$\text{dia} = \left(\frac{5}{8}\right)''$$

$$\text{Area} = \frac{\pi}{4} \left(\frac{5}{8}\right)'' = 0.31 \text{ in}^2$$

$$\text{Spacing} = \frac{0.31}{0.132} \times 12 = 2.81'' \approx 2.8'' \text{ c/c}$$

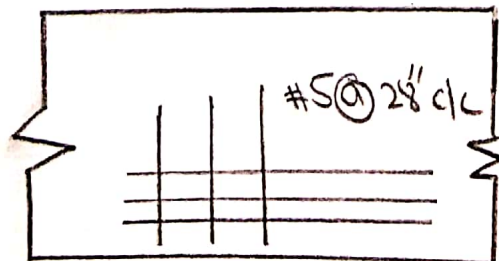
Step #10

Find sketch

$$f'_c = 4 \text{ ksi}, f_y = 40 \text{ ksi}$$

Main steel #6 at 9" c/c

Distribution steel #5 at 2.8" c/c



$$P = 8$$

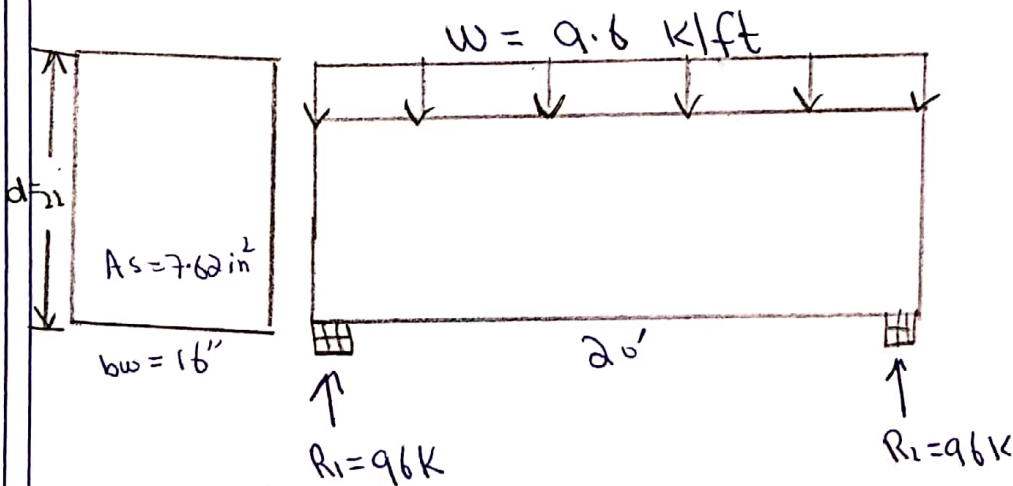
Sol First of all find the Unit load of beam

So

$$b \times V_c$$

$$= \frac{16}{12} \times 150 \Rightarrow 200 \text{ lb/ft} = 0.2 \text{ K/ft}$$

$$\begin{aligned} \text{So total factored load} &= 9.4 + 0.2 \\ &= 9.6 \text{ K/ft} \end{aligned}$$



Step # 01

Find the value of R_1 & R_2

$$\text{Total load} = 9.6 \times \frac{20}{2} = 96 \text{ K}$$

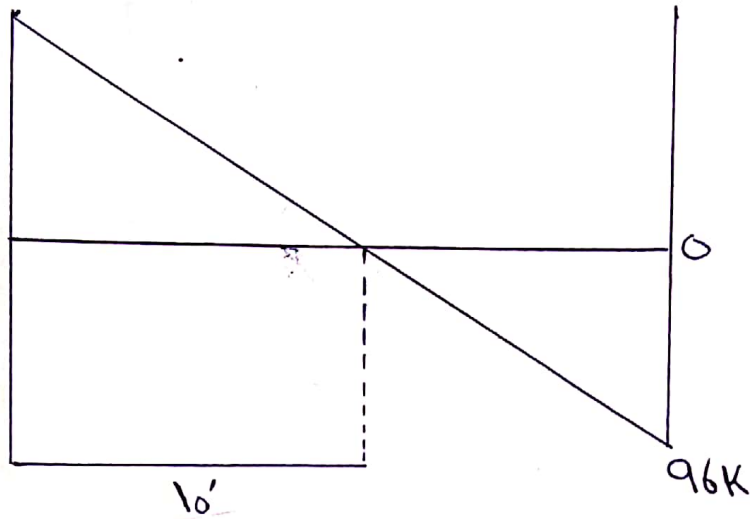
Step # 02

Draw it shear force diagram

B

$$P = 9$$

S.F.D
(kips)

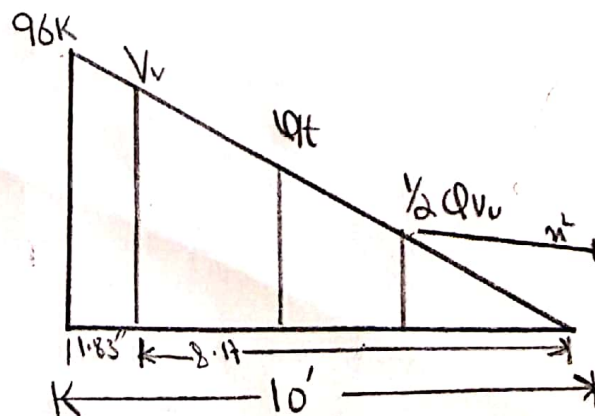


Step #03

Find the value of Critical Stress " V_u "
& its location

As we know that critical section is located at distance " d " from face of support

$a = 2d = 1.83'$ value of Critical Shear at distance ' d ' by similarity of triangles



$$P = 10$$

From Similar Δ 's $\frac{96}{10} = \frac{V_v}{8.17}$

$$V_v = 78.43 \text{ K}$$

Step # 04

Find the value of " ϕ_{vc} " & $\frac{1}{2} \phi_{vc}$ & also its distance from zero shear to right side

$$\phi_{vc} = \phi \times 2 \times \sqrt{f_c'} \times b \times d \Rightarrow \frac{0.75 \times 2 \times \sqrt{4000 \times 16 \times 2}}{1000}$$

$$\phi_{vc} = 33.40 \text{ K}$$

location of ϕ_{vc} by similarity of Δ s.

$$\frac{96}{10} = \frac{33.40}{n_1}$$

$$n_1 = 3.48'$$

$$\text{Now } \frac{1}{2} \phi_{vc} = \frac{33.40}{2} = 16.70 \text{ K}$$

$$\text{Location of } \frac{1}{2} \phi_{vc} \Rightarrow \frac{96}{10} = \frac{16.70}{n_2}$$

$$n_2 = 1.74'$$

Step # 05

Value of ϕ_{Vs} ($V_v = \phi_{Vs} + \phi_{Vc}$)

$$\text{So } \phi_{Vs} = V_v - \phi_{Vc}$$

$$\phi_{Vs} = 78.43 - 33.40$$

$$\boxed{\phi_{Vs} = 45.03 \text{ K}}$$

Step # 06

check on section adequacy.

$$\Rightarrow \phi \times 8 \times \sqrt{f_c'} \times b \times d = \frac{0.75 \times 8 \times \sqrt{4000} \times 16 \times 22}{1000} = 133.57 \text{ K}$$

As $\phi \times 8 \sqrt{f_c'} \times b \times d > \phi_{Vs}$ It means section is adequate.

Step # 07

check on min spacing for stirrups.

$$\phi \times 4 \times \sqrt{f_c'} \times b \times d = \frac{0.75 \times 4 \times \sqrt{4000} \times 16 \times 22}{1000} = 66.79 \text{ K}$$

As $\phi \times 4 \sqrt{f_c'} \times b \times d > \phi_{Vs} = 45.03 \text{ K}$

$$P = 12$$

Thus max spacing will be selected from the following four condition

$$1) S_{max} = 24''$$

$$2) \frac{d}{2} = \frac{22}{2} = 11''$$

$$3) S_{max} = \frac{A_v \times f_y}{0.75 \times \sqrt{f'_c} \times b_w} = 0$$

$$A_v = \frac{\pi}{4} \left(\frac{3}{8}\right)^2 = \frac{0.22 \times 60000}{0.75 \times \sqrt{4000} \times 16} = 17.40''$$

$$A_v = 0.11 \times 2$$
$$A_v = 0.22$$

$$4) S_{min} = \frac{A_v \times f_y}{50 \times b_w} = \frac{0.22 \times 60000}{50 \times 16} = 16.50$$

From above four condition, least value of spacing from #3 U-shaped will be selected so, $S_{min} = 11''$ c/c

Step #08

Spacing of stirrup from / at critical section ↙

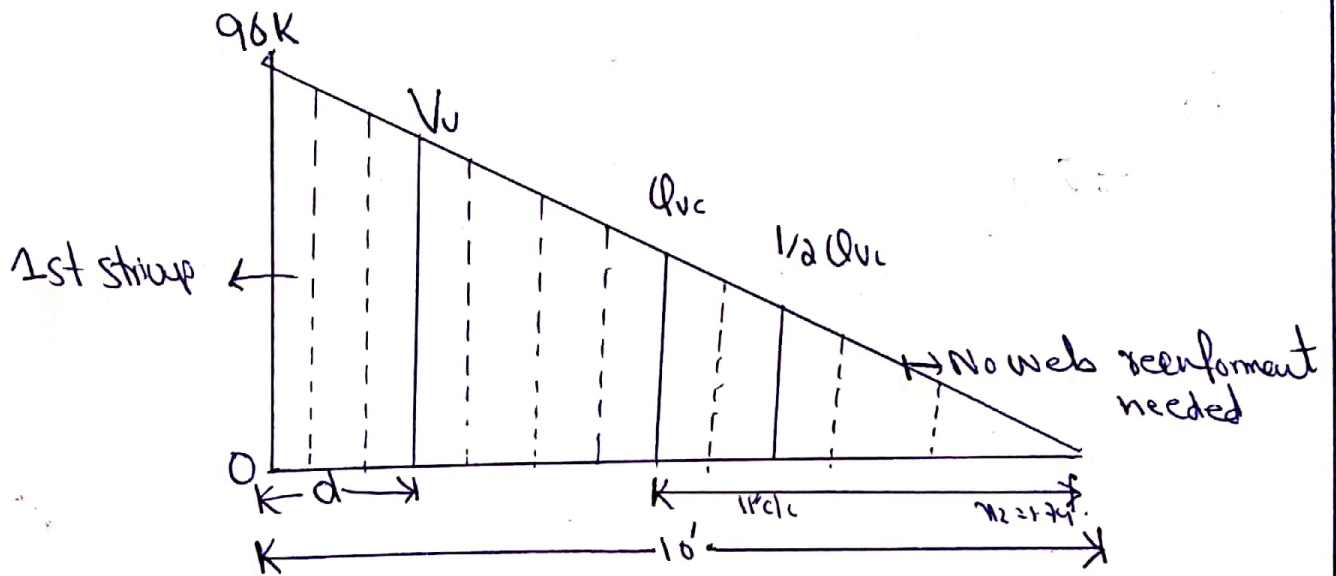
$$P = 13$$

$$S = \frac{\phi \times A_u \times f_y \times d}{V_u - \phi V_c} = \frac{0.75 \times 0.22 \times 60 \times 22}{78.43 - 33.40}$$

$$= 48.4'' \approx 5'' \text{ c/c}$$

Step #09

Find Sketch



$$P = 14$$

Ans
3

Step #1

Find gross area of Concrete

$$A_g = b \times b \quad (\text{Since It is Square tie Column})$$

$$A_g = 12 \times 12 = 144 \text{ in}^2 \quad (\text{Actual})$$

Step #2

Find the area of steel

$$\text{Since } A_s = 5\% \text{ of } A_g$$

$$A_s = 0.05 \times 144$$

$$\boxed{A_s = 7.2 \text{ in}^2}$$

Step #3

Ultimate load Carrying Capacity

$$P_u = \phi \times 0.80 \times [0.85 \times f'_c \times (A_g - A_s) + A_s \times f_y]$$

$$= 0.65 \times 0.80 [0.85 \times 4 [144 - 7.2] + 7.2 \times 60]$$

$$\boxed{P_u = 466.50 \text{ K}}$$

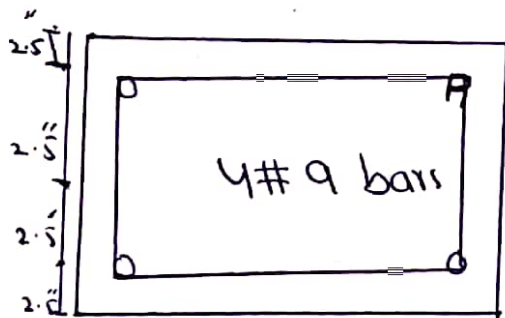
$$P = 15$$

Step #04

Sketch & design of Tie (clc distance)

From the below value we choose the least value of all thus.

- i) $16 \times \text{dia of long bar} = 16 \times 9/8$
- ii) $48 \times \text{dia of Tie bar} = \underline{48} \times 3/8$
- iii) least Column dimensions = $12''$
So c/c distance b/w ties = $12''$



Since it is a tied square column so there is no spiral stirrup used. The stirrups used is of rectangular shape due to the specification of the structure. Thus we will use tie stirrups instead.

P=16

Step #1

Total weight $h = 24''$

Step #2

$$\begin{aligned} \text{Total weight} &= \text{wt of soil} + \text{wt of Rc} \\ &= 3 \times 120 + 2 \times 150 \\ &= 660 \text{ Psf} = 0.660 \text{ ksf} \end{aligned}$$

Step #3

Effective bearing Capacity

$$\begin{aligned} q_e &= q_a - w \\ q_e &= 2.50 - 0.660 \\ q_e &= 1.84 \text{ ksf} \end{aligned}$$

Step #4

Required Area of foundation

$$P = 17$$

$$A_{req} = \frac{\text{Service load}}{q_e} = \frac{100 + 120}{1.84} = 119.57 \text{ ft}^2$$

Step #5

Since foundation is square

$$A_{req} = b \times b = 119.57 \Rightarrow 12'$$

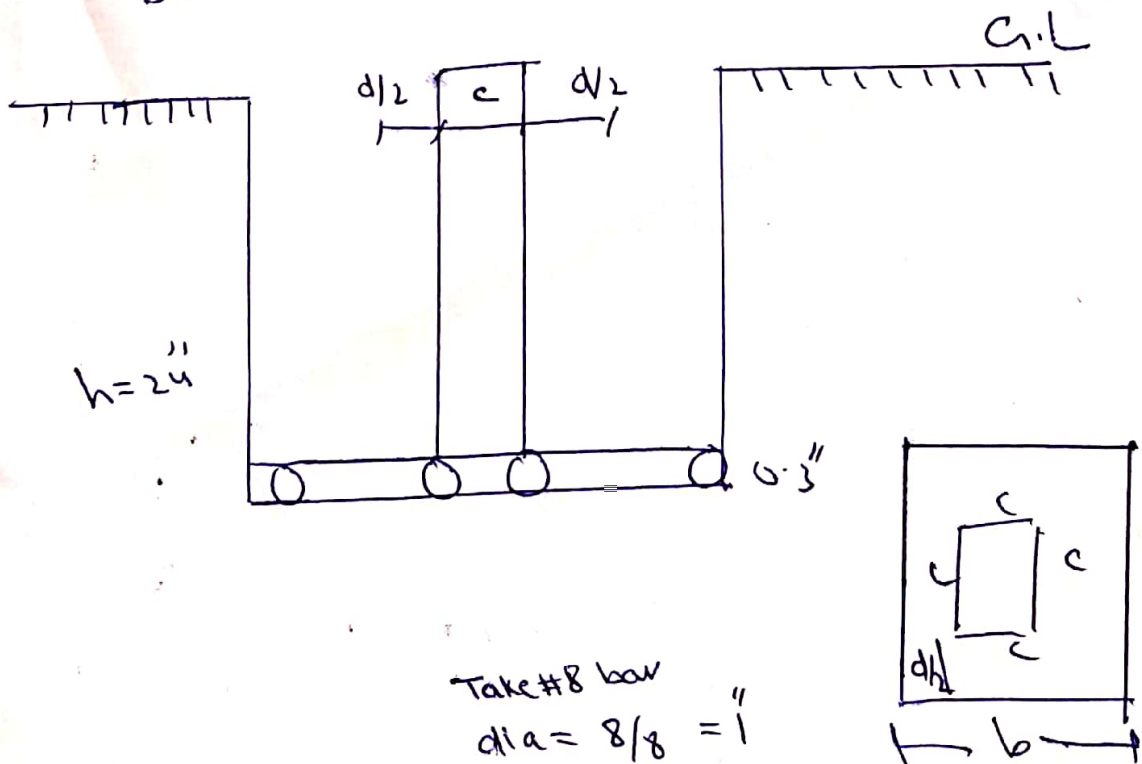
Step #6

Upward bearing capacity of soil

$$q_{up} = \frac{\text{Factored load}}{(B)^2} = \frac{1.2 \times 100 + 1.6 \times 120}{(12)^2}$$

Step #7 Punching Shear

$$b_o = 4 \times (c + d)$$



Take #8 bar
 $d_{la} = 8/8 = 1''$

3st P=18

$$d = h - c.c - \text{dia of bar} - \frac{1}{2} d_b$$

$$= 24 - 3 - 1 - \frac{1}{2}(1) = 19.5$$

$$b_o = 4 \times (16 + 19.5) = 142''$$

Step#08

$$V_{u2} = q_{up} \times \left[B^2 - (c+d)^2 \right]$$

$$= 2.58 \times \left[11^2 - \left(\frac{16 + 19.5}{12} \right)^2 \right]$$

$$V_{u2} = 289.60 \text{ K}$$

Step#9

$$\phi V_{cp} = \phi \times 4 \times \sqrt{f_c'} \times b \times d$$

$$= 0.75 \times 4 \times \sqrt{4000} \times 142 \times 19.5$$

$$\phi V_{cp} = 525.38$$

Step#10

Beam shear one way shear check

$$p = 19$$

$$V_{U1} = q_{up} \times B \times \left[B/2 - \frac{c}{2} - d \right]$$

$$V_{U1} = 2.58 \times 11 \times \left[\frac{11}{2} - \frac{16}{2} - 19.5 \right]$$

$$V_{U1} = 90.95 \text{ k}$$

Step #11

Self Shear Capacity

$$\phi_{vc} = \phi \times 2 \times \sqrt{f_c} \times b \times d$$

$$= 0.75 \times 2 \times \sqrt{4000} \times [11 \times 2 - 16]$$

$$= 110.04 \text{ k} > V_{U1} \Rightarrow \text{O.K.}$$

$$p = 20$$

Step #12 Ultimate moment

$$M_u = \frac{q_{up} \times B}{8} \times (B - c)^2 = \frac{2.58 \times 11}{8} \times \left(\frac{11 - 16}{12}\right)^2$$

$$M_u = 331.49 \text{ k} \approx 3977.93 \text{ k'}$$

Step #13

Area of steel for main bar
by trial & Repeat method

Trial #01

$$\text{let } a = 0.2 \times h = 0.2 \times 24 = 4.8''$$

$$A_s = \frac{M_u}{d \times f_y \left(d - \frac{a}{2}\right)} = \frac{3977.93}{0.85 \times 60 \times 11 - \frac{4.8}{2}} = 1.53''$$

Trial #02

$$A_s = \frac{3977.93}{0.90 \times 60 \times \left(11 - \frac{1.53}{2}\right)} = 7.197 \text{ in}^2$$

Trial #03

$$a = \frac{7.197 \times 60}{0.85 \times 3 \times 11 \times 12} = 1.28''$$

$$P = 21$$

$$A_s = \frac{3977.93}{0.90 \times 60 \left(11 - \frac{1.28}{2}\right)} = \boxed{7.1 \text{ in}^2}$$

So that area = 7.1 in^2

Step#14

check the min reinforcement by following
03 method

$$\begin{aligned} \text{a) } A_{s_{\min}} &= 0.0018 \times B \times h = 0.0018 \times (11 \times 12) \times 24 \\ &= 5.70 \text{ in}^2 \end{aligned}$$

$$\begin{aligned} \text{b) } A_{s_{\min}} &= \frac{200}{f_y} \times B \times d = \frac{200}{60000} (11 \times 12) \times 19.5 \\ &= 8.58 \text{ in}^2 \end{aligned}$$

$$\begin{aligned} \text{c) } A_{s_{\min}} &= \frac{3 \times \sqrt{f_c'}}{f_y} \times B \times d = \frac{3 \times \sqrt{3000} \times (11 \times 12) \times 19.5}{60000} \\ &= 7.05 \text{ in}^2 \end{aligned}$$

From above value greater value
will be selected

$$\text{thus } A_{s_{\min}} = 8.58 \text{ in}^2$$

$$p = 22$$

Step #15 Using #8 bar

$$A_b = 0.785 \text{ in}^2$$

$$\text{No of bar} = \frac{A_s}{A_b} = \frac{8.58}{0.785} = 10.92 = 11$$

11 bar in each direction