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Section (A)

Q2) A rectangular beam must carry a service line load

Width (b) = 10"

Height (h) = 20"

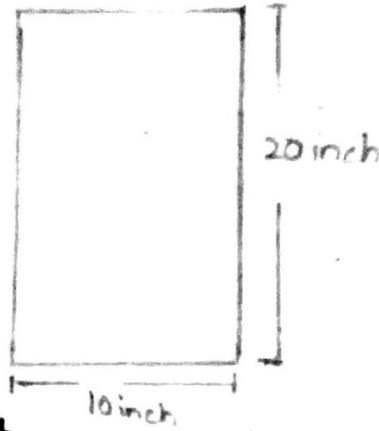
$f_c = 4000$  Psi

$f_y = 60000$  Psi

Span = 18'

Live Load = 2.47 kips/ft

Dead Load = 1.05 kip/ft



Step 1:-

Effective cover ( $d'$ ) = 2.5"

Effective depth ( $d$ ) = 20 - 2.5  
= 17.5"

$\rho_{max} = ?$  (Reinforcement Ratio)

$$\rho_{max} = 0.85 \times \beta \times \frac{f'_c}{f_y} \times \left( \frac{\epsilon_u}{\epsilon_u + \epsilon_y} \right)$$

$$\rho_{max} = 0.85 + 0.85 \times \frac{4}{60} \times \frac{0.003}{0.003 + 0.005}$$

$$\therefore 4000 \text{ Psi} = 4 \text{ ksi}$$

$$\therefore 60000 \text{ Psi} = 60 \text{ ksi}$$

Step 2:- Area of Steel:-

$$\rho_{max} = \frac{A_{steel}}{B \times d}$$

Arranging eq for Area we get

$$A_{steel} = \rho_{max} \times B \times d$$

$$A_{steel} = 0.0181 \times 10 \times 16$$

$$A_{steel} = 2.896 \text{ in}^2$$

$$A_{steel} = 2.896 \text{ in}^2 \text{ or } 2.90 \text{ in}^2$$

**(MOMENTS)**

**Step No 3:-**  $Mu_2 = \phi \times A_{steel} \times f_y \times (d - \frac{a}{2}) \rightarrow \text{eq (i)}$

$a = ? \Rightarrow a = \frac{A_{steel} \times f_y}{0.85 \times f'_c \times b} = \frac{2.90 \times 60}{0.85 \times 4 \times 10}$

$a = 5.11 \text{ inch or } a = 5.11''$

Now put values of  $a$  in eq (i)

$Mu_2 = \cancel{0.90} \times 2.90 \times 60 \times (16 - \frac{5.11}{2})$

$Mu_2 = 2340 \text{ in-kip}$

**Due to given loads:-**

Beam own weight or Self weight  
As we know that  $Mu = \frac{wL^2}{8}$  and  $w = ?$

$w$  is total factored load  $\bar{w}$  and is given as  
factored load =  $(1.2 \times 1.05) + (1.6 \times 2.47) \therefore (1.2 \& 1.6 \text{ are for live and dead loads})$   
 $= 5.21 \text{ kips/ft}$

Now,  $Mu = \frac{wL^2}{8} \Rightarrow \frac{5.21 \times 18^2}{8}$

$Mu = 211 \text{ ft-kips or } 2530 \text{ in-kips}$

Double Reinforcement will be required as  
 $Mu > Mu_2$

**Step 4:-**

$Mu_1 = \frac{Mu - Mu_2}{\phi} \Rightarrow \frac{2530 - 2340}{0.90} = 471.1 \text{ in-kip}$

**Steel Area in Compression zone:-**

$Mu_1 = \phi \times A_{steel}' \times f_y \times (d - d')$

$A_{st}' = \frac{Mu_1}{\phi \times f_y \times (d - d')}$

$A_{st}' = \frac{\cancel{471} 471}{0.90 \times 60 \times (16 - 2.5)} = 0.64 \text{ in}^2$

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The total area of reinforcement is

$$A_s = 2.90 + A_{st'} \Rightarrow 2.90 + 0.64 = 3.54 \text{ m}^2$$

$$A_s = 3.54 \text{ in}^2$$

**Step 4.5**:- (No of bars for Compression & Tensile zone)

We use # 8 bars  $\therefore$  (dia = 1" Area = 0.785 in<sup>2</sup> for No 8 bar)

$$\text{No. of Bars} = \frac{A_{st}}{\text{Area of 1 bar}} \Rightarrow \frac{3.54}{0.785} = 4.50$$

No of Bars for tensile zone will be 5 of # 8.  
for Compression zone:-

$$\text{No of bars} = \frac{A_{st'}}{\text{Area of 1 bar}}$$

We use bar # 6 (dia = 0.75" Area = 0.44 in<sup>2</sup>)

$$\text{No of bars} = \frac{0.64}{0.44} = 1.49 \approx 2$$

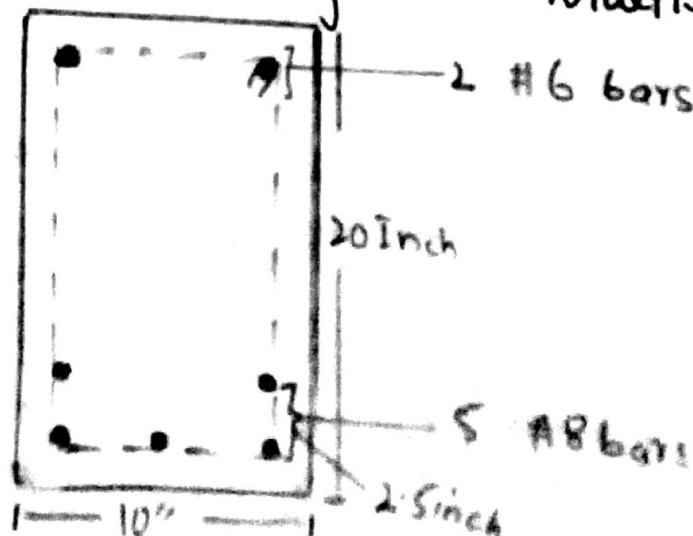
So two No of # 6 bars will be used for Compression

**Beam Minimum Width:-**

$$W_{\min} = 2(1.5) + 2\left(\frac{3}{8}\right) + 5\left(\frac{8}{8}\right) + 4\left(\frac{8}{8}\right)$$

$$W_{\min} = 12.8 \quad \therefore 12.8 > 10$$

So it will be lay in Multilayer  
Main bar will be lay in Multilayer.





Step 8:- Design Moment :-

$$M_d = \phi \times (A_{st} \times f_y \times (d - d') + (A_{st} - A_{st}') \times f_y \times d - \frac{a}{2})$$

$$a = \frac{(A_{st} - A_{st}') \times f_y}{0.85 \times f'_c \times b} \Rightarrow \frac{(0.785 \times 5) - (2 \times 0.44) \times 60}{0.85 \times 4 \times 10}$$

$$a = \frac{3.925 - 0.88(60)}{34}, a = \frac{182.7}{34}, a = 5.373''$$

$$M_d = 0.90 \times [2 \times 0.44 \times 60 \times (16 - 2.25) + (5 \times 0.785 - 1 \times 0.44) \times 60 \times (16 - \frac{5.73}{2})]$$

$$M_d = 0.90(52.8 \times 13.75) + (3.925 - 0.44) \times 60 \times (13.13)$$

$$M_d = 653.4 + 3.485 \times 787.8$$

$$M_d = 653.4 + 2745.483$$

$$M_d = 2798.4 \text{ in-kips}$$

$M_d > M_u$  hence it is okay

Q2 Describe bond stress and Development length?

(c) BOND STRESS:-

It is defined as the resistive stress against the pulling out of steel bar from concrete mass, developed per unit surface area of a reinforcing bar.

The bond stress balances the force present in the bar. In case of no bond, the steel bar will be pulled out of concrete.

Development length:-

It can be defined as the amount of bar length needed to be embedded or projected into the column to establish the desired bond strength between the concrete and steel and is given by

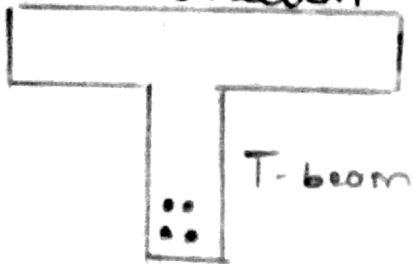
$$L_d = \frac{\phi \sigma_s}{4 \tau_{bd}}$$

Q2 In which condition double reinforced beam used?

- (ii) We used double reinforced beam due to the following reasons:-
- => When the cross section of beam is fixed
  - => When moment to be carried by the beam is more than the balanced beam
  - => In case of continuous beam
  - => When there is torsion on the beam

Q2:- Differentiate between T-beam & Rectangular beam?

Both beam have T-shape but their analysis is quite different from one another. In case of T beam slab and beam are connected with one another and act as one member. In case of rectangular beam slab has been placed on beam and there is no connection between slab and beam.



T-beam



Rectangular Beam

Q2 write a short note on the effect of strength--?

When we design flexural strength, the strength reduction factor decreases from tension-controlled section to compression controlled section to decrease ductility and increase safety. So to determine the reduction factor for flexural strength of reinforced concrete beam according to ACI code. In the ~~reliability~~ reliability-based design the reliable prediction of the flexural strength of reinforced concrete members is assured by the use of reduction factors corresponding to different target reliability index.

## Q2: Briefly describe design Method?

- Design Method are particularly based on condal provisions of a country so they vary from places to places. There are three methods of design that is Working Stress, Ultimate Load Method, Limit state. These design are used for reinforced concrete as well as for steel design.
- Out of these three limit state method is much more preferred because of
- i) Area of cross section required is less than working stress design.
  - ii) It considers uncertainty in load as well as design strength of materials and takes factors of safety for both.
  - iii) State of serviceability is checked for design.

## Q3:-

### Data:-

Slab thickness = 6"

Span = 32'

C/C distance = 10'

Web width = 14"

Effective depth =  $28'' - 3'' = 25''$

Total depth (h) = 28"

D.L = 50 lb/ft<sup>2</sup>

S.S = 225 lb/ft<sup>2</sup>

$f_y = 60000 \text{ Psi} = 60 \text{ kips}$

$f'_c = 4000 \text{ Psi} = 4 \text{ kips}$



**(Solution:-)****Step 1:-**

$$M_u = \frac{M_v \times L^2}{8}$$

Beam self weight per ft

$$W_t = b \times t \times \gamma_c = \frac{14}{12} \times \frac{18}{12} \times 150 \quad (\because 1'' = \frac{1}{12}')$$

$$W_t = 408.33 \text{ lb/ft}$$

Factored Load:-

$$= 1.2(50 + 408.33) + 1.6(225) \quad (\because 1.2 \text{ \& } 1.6 \text{ are constant})$$

$$= 0.909 \text{ kip/ft} \quad (\text{lb} \rightarrow \text{kip}) \quad \text{and factor of live \& dead loads}$$

( $\div$  by 1000)

Moment:-

$$\frac{W L^2}{8} = \frac{0.909 \times 32^2}{8} \times 12 = 1396.23 \text{ kip-inch}$$

Effective breadth.

$$16(h_f) + b_w = 16(6) + 14 = 110''$$

$$\text{C/C distance} = 10(12) = 120''$$

$$\text{Span/4} = 32/4 = 8' \times 12 = 96'' \Rightarrow b_e = 96''$$

(Rectangular or T-beam):-

Trial # 1:-

$$a = h_f = 6''$$

$$A_{st} = \frac{M_u}{\phi \times f_y \times (d - a/2)}$$

$$A_{steel} = \frac{1396.23}{0.90 \times 60 \times (25 - 6/2)}$$

$$A_{steel} = 1.17 \text{ in}^2$$

Trial 2:-

$$a = \frac{A_{st} \times f_y}{0.85 \times f_c \times b} = \frac{1.17 \times 60}{0.85 \times 4 \times 96}$$

$$a = 0.2''$$

and  $0.2 < 6$ 

so it is rectangular beam.

$$A_{st} = \frac{1396.23}{0.90 \times 60 \times \left(25 - \frac{0.2}{2}\right)} = 1.05 \text{ in}^2$$

Step 23:-  $\rho_{max}$  and  $\rho_{min}$ 

$$\rho_{max} = 0.85 \times 0.85 \times \frac{4}{60} \left( \frac{0.003}{0.003 + 0.005} \right)$$

$$\rho_{max} = 0.018$$

$$\rho_{min} = \frac{200}{f_y} = \frac{2000}{60,000} = 0.003$$

$$\rho = \frac{A_{steel}}{b \times d} = \frac{1.05}{14 \times 25} = 0.0029$$

$$\rho_{min} < \rho < \rho_{max} \quad \therefore 0.003 < 0.0029 < 0.018$$

$$\text{So, } \rho = \frac{A_{st}}{b \times d}, \quad A_{st} = \rho_{min} \times b \times d \Rightarrow A_{st} = 0.003 \times 14 \times 25$$

$$A_{st} = 1.05 \text{ in}^2$$

Selection of Bars :-

Let use # 6 bar then ( $\text{Area} = 0.78$ ) ( $\text{Area} = 0.44 \text{ in}^2$ )  
( $\text{dia} = 0.44$ ) ( $\text{dia} = 0.75$ )

$$\text{No of bars} = \frac{1.05}{0.44} = 2.386 \approx 3 \text{ bars \# 6}$$

Minimum Width:-

$$b_{min} = 2(1.5) + 2\left(\frac{3}{8}\right) + 2(0.75) + 1(0.75)$$

$$b_{min} = 3 + 0.75 + 1.5 + 0.75$$

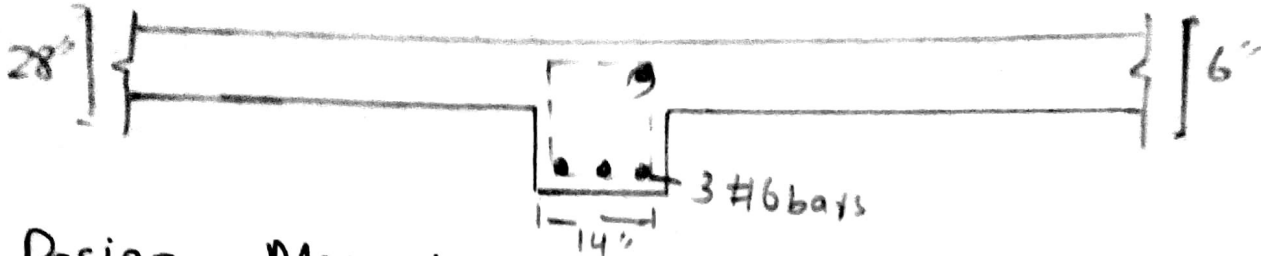
$$b_{min} = 6''$$

 $6'' < 14''$  so it is in one layer



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Design Moment:-

$$M_d = \phi \times f_y \times A_{st} \times (d - \frac{a}{2})$$

Area of steel = Area of 1 bar  $\times$  No of bars

$$A_{st} = 0.44 \times 3 \Rightarrow 1.32 \text{ in}^2$$

$$a = \frac{1.32 \times 60}{0.85 \times 4 \times 96} \Rightarrow \frac{79.2}{326.4} = 0.242''$$

$$M_d = 0.90 \times 60 \times 1.32 \times (25 - \frac{0.24}{2}) = 2092.3 \text{ kip-inch}$$

$$As \quad 2092.3 > 1396.23$$

so the Design is ok.