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Program :- B.Sc Civil Engineering

Assignment :- Plain and Reinforced Concrete Design-I

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Q No 1

7839 (1)

Explain in detail types of stirrups with figure and also explain ACI codes for shear design.

Ans - Stirrup :- stirrups are closed-loop bars tied at regular interval in beam reinforcement to hold the bars in position.

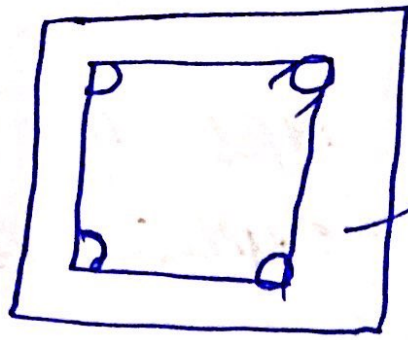
Types of Stirrups :-

i) Single Legged Stirrup :-

Legged stirrup have rarely being used because they are mostly used when binding only two rods. The single



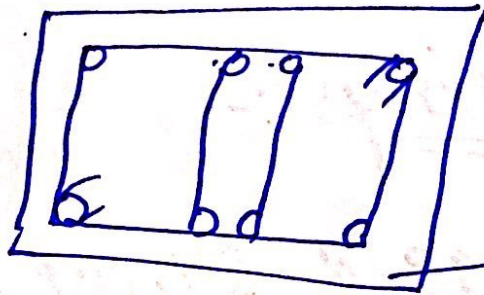
2) Two Legged Stirrup :- It is most commonly and widely used stirrup. Minimum 4 bars are required for providing this stirrup.



2 Legged Stirrup

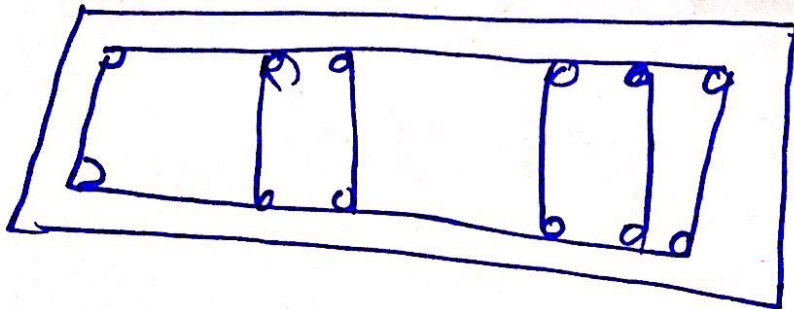
3) Four Legged Stirrup:-

These stirrups are used in case of web reinforcement



4 Legged Stirrup.

4) Six Legged Stirrup:-



ACI Codes for Shear Design of a Beam:-

Following are the formulas used for the According to ACI-318 used for the

# Shear design of a beam.

## 1) Critical Section:-

Critical section occur at  $45^\circ$  and it is distance ( $d$ ) from the face of support which is equal to effective depth.

## 2) Shear Strength Capacity of Concrete is:-

$$V_c = 2 \times \sqrt{f'_c} \times b_w \times d$$

## 3) Minimum Web Reinforcement:-

if  $V_u \leq \phi V_c$ , then theoretically no web reinforcement is required. However ACI Code require provision of atleast a minimum area of web reinforcement equal to

$$\phi = 0.75 \rightarrow \text{For shear design}$$

( $\because V_u = \text{Total factored shear applied to a given section}$ )

## For minimum Reinforcement Area:-

$$A_{u\text{min}} = 0.75 \times \frac{\sqrt{f'_c} \times b_w \times s}{f_u}$$

or 
$$\frac{S_o \times b_w \times S}{f_y}$$

By interchanging the above formula we can obtain the formula for minimum spacing

$$S_{max} = \frac{A_u \times f_y}{0.75 \times \sqrt{f'_c} \times b_w} \quad \text{or} \quad \frac{A_u \times f_y}{S_o \times b_w}$$

4 - No-web reinforcement is required to

$$\underline{V_u < \frac{1}{2} \phi V_c}$$

→ Between critical section " $V_u$ " and " $\phi V_c$ ", spacing b/w web reinforcement can be find by

$$S = \frac{\phi \times A_u \times f_y \times d}{V_u - \phi V_c}$$

5) if  $\underline{V_c \leq 4 \times \sqrt{f'_c} \times b_w \times d}$ , then max

spacing for stirrups will be the of the following

- 1 =  $24''$
- 2 =  $d/2$

3  $S_{max} = \frac{A_u \times f_y}{0.75 \sqrt{f'_c} \times b_w}$

(4)  $S_{max} = \frac{A_u \times f_y}{S_o \times b_w}$

## Q No 2

A simply supported rectangular beam 14" wide having an effective depth of 22" to carry a lateral load of 6.5 k/ft on a 18' simple span. It is reinforced with 7 in<sup>2</sup> of tensile steel area of  $f'_c = 4 \text{ ksi}$  and  $f_y = 60 \text{ ksi}$ .  
The design the beam for shear.

Given :-

Breadth of web of beam ( $b_w$ ) = 14"

Effective depth ( $d$ ) = 22"

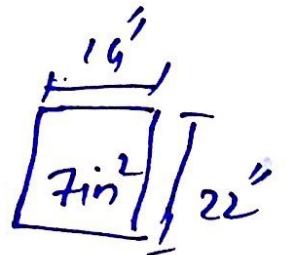
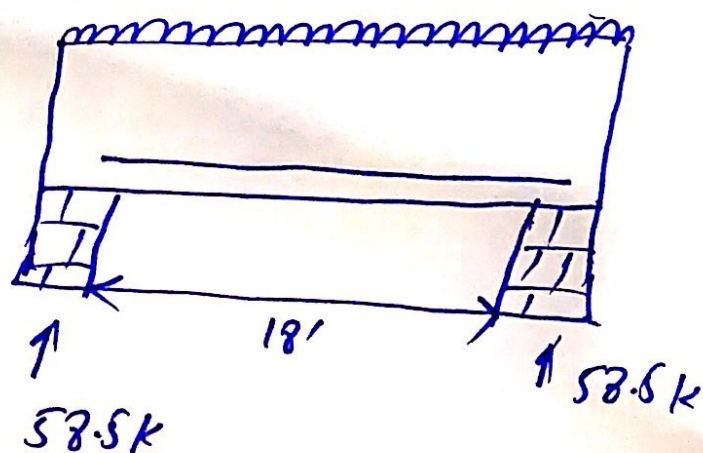
Given load = 6.5 k/ft

Steel area = 7 in<sup>2</sup>

$f'_c$  = 4 ksi

$f_y$  = 60 ksi

Sol :-



$v_s > 4 \times \sqrt{f'_c} \times bw \times d$

↓  
max spacing will be halved

→ if  $v_s > 8 \times \sqrt{f'_c} \times bw \times d$

↓  
Then either increase cross-section dimensions or increase  $f'_c$ .



Step # 01 :-

Reaction on Support :-

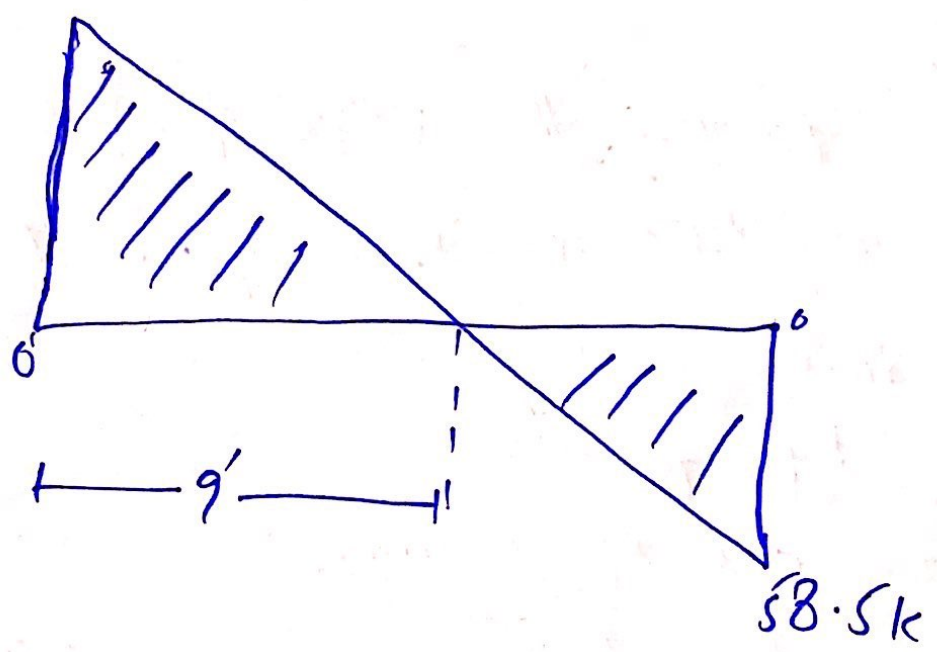
Finding the reaction due to applied Load.

Total load =  $\frac{6.5 \times 18}{2} = 58.5 \text{ kips}$

Step # 2 :-

(Shear Force Diagram)

The required shear diagram will be



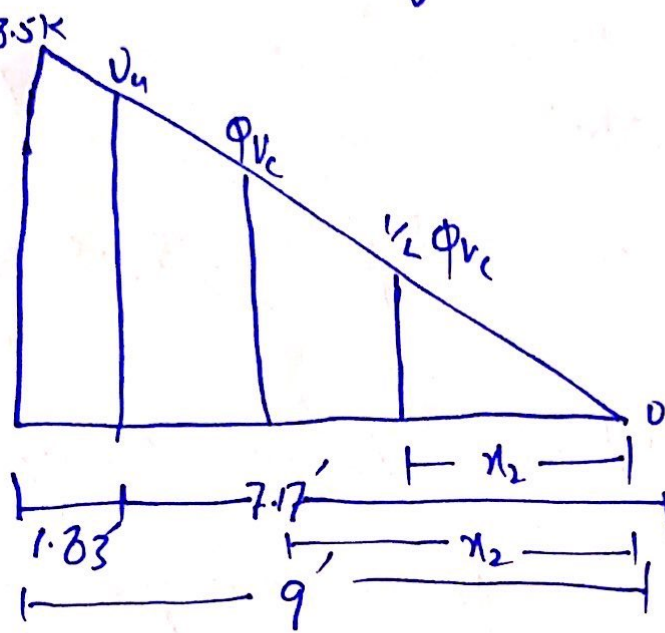
Step # 3 :-

Finding the value of critical shear  $V_a$  and its location  $M_s$ ,

we know that critical shear is located at distance "d" from face of support  $(d) = 2' = 1.83'$



⇒ So we will find the value of critical shear at distance (d) by use of similar triangle. #139 (8)



Step # 4! - Finding the value of  $\phi V_c$  and  $\frac{1}{2} \phi V_c$  and also its distance from zero shear to right side.

By formula

$$\begin{aligned} \Rightarrow \phi V_c &= \phi \times 2 \times \sqrt{f'_c} \times b_w \times d \\ &= 0.75 \times 2 \times \sqrt{4000} \times 14 \times 22 = 29219 \text{ lbs} \\ &= 29.211 \text{ kips} \end{aligned}$$

⇒ location of  $\phi V_c$  by similar triangle

$$\frac{58.5}{9} = \frac{\phi V_c}{x_1} \Rightarrow \frac{58.5}{9} = \frac{29.21}{x_1}$$

$$\Rightarrow x_1 = 4.49'$$

→ Similarity

$$\frac{1}{2} \phi v_c = \phi v_c / 2 \Rightarrow 29.21 / 2 = 14.6 \text{ kips.}$$

→ Location of  $\frac{1}{2} \phi v_c$  will be

$$\frac{58.5}{9} = \frac{14.60}{x_2} \rightarrow \boxed{x_2 = 2.24}$$

Step # 5:

Find the value of  $\phi v_s$

By formula.  $v_u = \phi v_s + \phi v_c$

$$\begin{aligned} \rightarrow \phi v_s &= v_u - \phi v_c \\ &= 46.61 - 29.21 \end{aligned}$$

$$\boxed{= \phi v_s = 17.4 \text{ kips.}}$$

Step # 6

Check on section adequacy

By formula

$$= \phi \times \beta \times \sqrt{f'_c} \times b \times w \times d$$

$$\begin{aligned} &= 0.75 \times \beta \times \sqrt{4000} \times 14 \times 22 = 116877 \text{ lbs} \\ &= 116.87 \text{ kips.} \end{aligned}$$

$$\text{As } \phi \times \beta \times \sqrt{f'_c} \times b \times w \times d > \phi v_s$$

So section is Adequate.

Step # 7:- check on maximum spacing for stirrup:-  
By formula

$$= \phi \times 4 \times \sqrt{f'_c} \times b_w \times d$$

$$= 0.75 \times 4 \times \sqrt{4000} \times 14 \times 22 = 58438 \text{ lbs}$$

$$= 58.43 \text{ kips}$$

As  $\phi \times 4 \times \sqrt{f'_c} \times b_w \times d > \phi V_s$

So maximum will be selected from the following 4 conditions.

1)  $S_{max} = 24''$

2)  $d/2 = 22/2 = 11''$

3)  $S_{max} = \frac{A_v \times f_y}{0.75 \times \sqrt{f'_c} \times b_w}$

$$S_{max} = \frac{0.22 \times 60000}{0.75 \times \sqrt{4000} \times 14} = 19.87''$$

4) -  $S_{max} = \frac{A_v \times f_y}{S_o \times b_w} = \frac{0.22 \times 60000}{S_o \times 14} = 18.75''$

From 4 above conditions, least value of spacing for #3 2 legged stirrup will be selected as

∴  $S_{max} = 11''$

Check on maximum spacing for stirrups

(11)

By formula

$$= \phi \times 4 \times \sqrt{f'_c} \times b_w \times d$$

$$= 0.75 \times 4 \times \sqrt{4000} \times 14 \times 22 = 58438 \text{ lbs}$$
$$= 58.43 \text{ kips}$$

$$\text{As } \phi \times 4 \times \sqrt{f'_c} \times b_w \times d > \phi V_s$$

so maximum will be selected from the following 4 conditions.

1) -  $s_{\max} = 24''$

2) -  $d/2 = 22/2 = 11''$

3) -  $s_{\max} = \frac{A_u \times f_y}{0.75 \times \sqrt{f'_c} \times b_w}$

$$= \frac{0.22 \times 60000}{0.75 \times \sqrt{4000} \times 14} = 19.87''$$

4) -  $s_{\max} = \frac{A_u \times f_y}{S_o \times b_w} = \frac{0.22 \times 60000}{S_o \times 14} = 18.25''$

From above 4 conditions, Least value of spacing for #3,  $s_{\max} = 11''$

Step # 8:- Stirrups spacing from/at critical section will be.

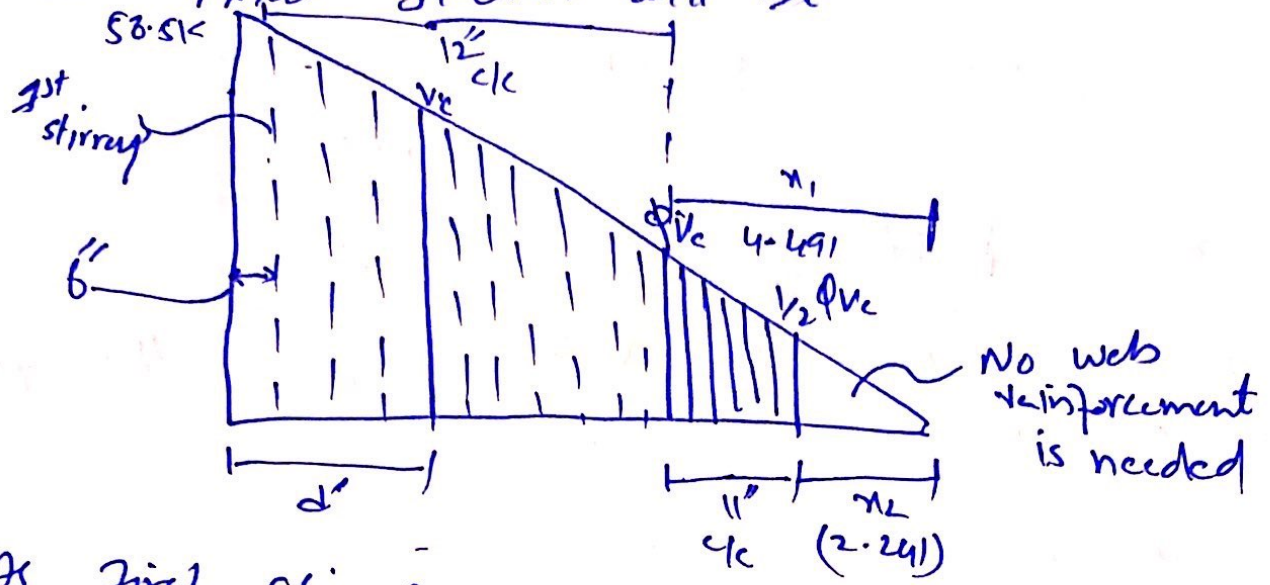
$$s = \frac{\phi \times A_u \times f_y \times d}{V_u - \phi V_c} = \frac{0.75 \times 0.22 \times 60 \times 22}{46.61 - 29.21}$$

$$s = 12.5'' \hookrightarrow 12''$$

$S_0 = 12' \text{ etc}$

Step # 9 :-

Final sketch will be



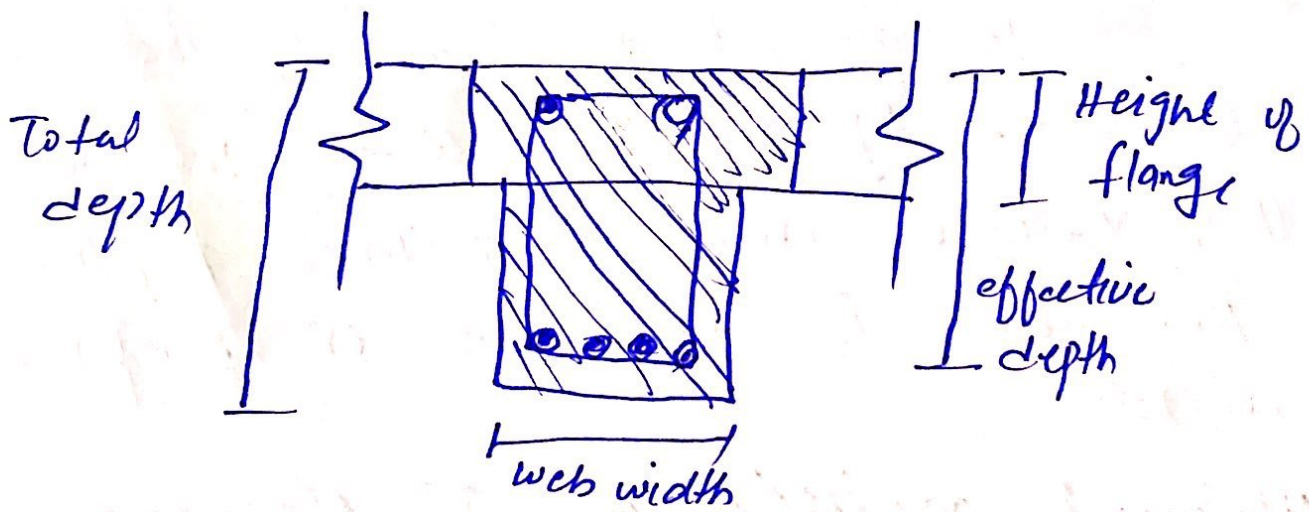
As first stirrup of face of support;  
 $S/2 = 12/2 = 6'$



Define both the T-Beam and L-Beam with the help of diagram. Also explain the Flexural analysis of T-Beam.

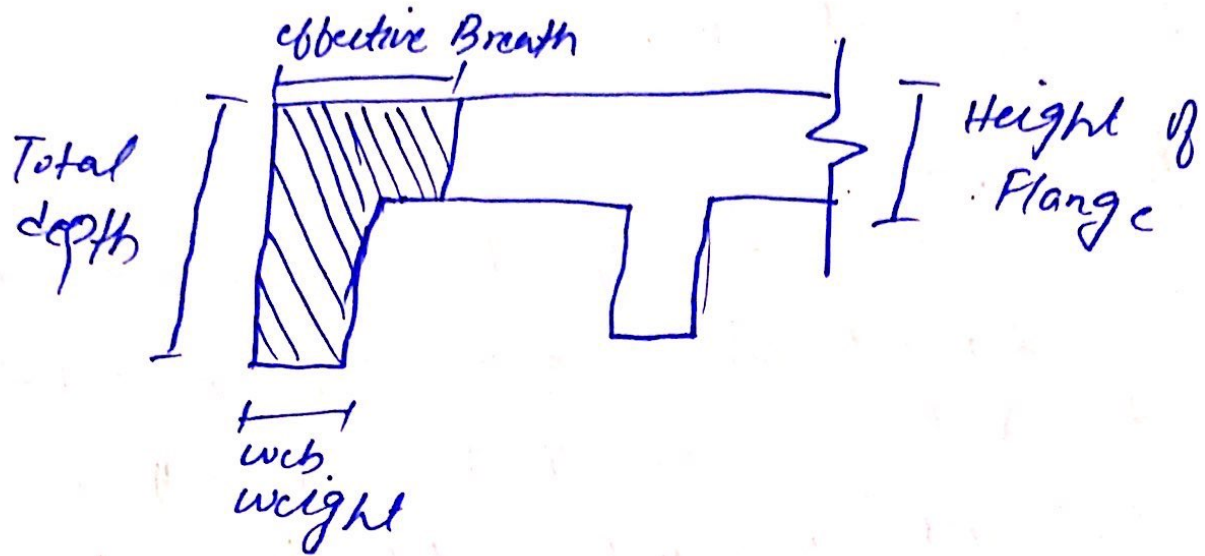
### T-Beam :-

⇒ In most of the reinforcement concrete structure, concrete slabs, are cast monolithically with the slabs, so in this case that the beam act as in intermediate beam are called T-Beam



- ⇒ The upper most area of the beam attached to the slab is called Flange
- The bottom rectangular portion of the beam is called web of the beam.

L-Beam: -  $\rightarrow$  L-Beam is structure that is in contact with the slabs and present at the corner of the floor is called L-Beam.



- $\Rightarrow$  L-Beam are also called Edge Beam.
- $\Rightarrow$  It also provide at the corner of the slabs.
- $\Rightarrow$  L-Beam are typical floor beam. Because of their reduced overall structure depth, The beam are in prestressed or reinforced concrete.

### Flexural analysis of I-Beam:-

- 1- For finding the ultimate factored moment we are the following formula:-

$$M_u = \frac{w_u \times L^2}{8}$$

2) - Effective width for T-Beam is Calculate as:-

- 1) -  $b(h_f) + b_w$
- 2) - c/c distance
- 3) - span/4
- 4) -  $\frac{L T_s}{2} + b_w$

3) Checking whether Rectangular or T-Beam

Analysis:-

- i) - if  $a > h_f \rightarrow$  special analysis is required
- ii) - if  $a < h_f \rightarrow$  Rectangular Beam analysis is required

4) - For Find Area of steel, we have to use:-

$$A_{st} = \frac{M_y}{\phi \times f_y \times (d - a/2)}$$

where

$$a = \frac{A_{st} \times f_y}{0.85 \times f'_c \times b_w}$$

5) - For checking minimum width for Bars accommodation:-

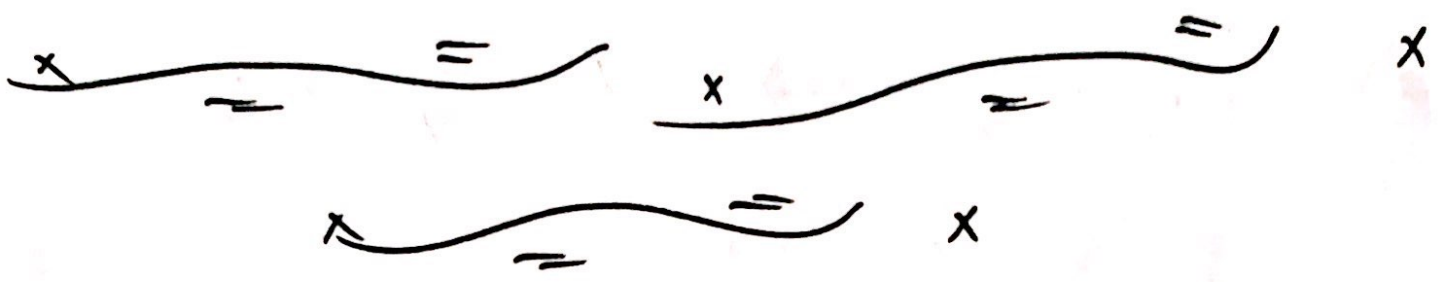
$$\text{No. of bars} = \frac{\text{Area of steel}}{\text{Area of Single Bar}}$$



①- Design moment is given by :-

$$M_d = \phi \times f_y \times A_{st} \times (d - a/2) \rightarrow \text{if } a < h_f.$$

$$M_d = \phi \times [A_s \times f_y \times (d - h_f/2) + (A_s - A_{st}) \times f_y \times (d - a/2)] \rightarrow \text{if } a > h_f$$



Q No 4

What is the difference between Case-I And Case-II in the design of T-Beam.

Case-I:-

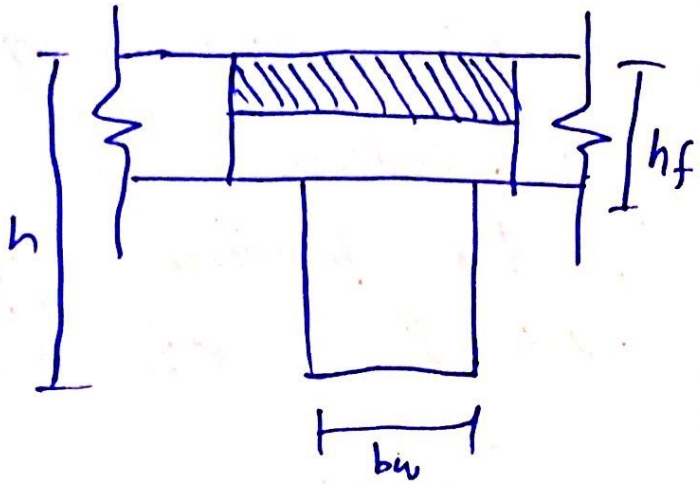
From the figure

$a < h_f$

So in this case,

Rectangular Beam analysis is required so, The Design moment formula will be

$$M_d = \phi \times f_y \times A_{sT} \times (d - a/2)$$



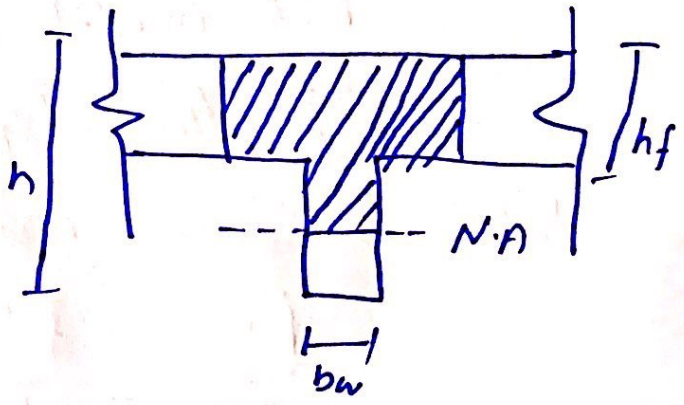
Case-II:-

From the figure

$a > h_f$

So in this special beam analysis i.e, T-Beam analysis is required so, The required design moment will be

$$M_d = \phi \times \left[ A_s \times f_y \times (d - \frac{h_f}{2}) + (A_s - A_{sT}) \times f_y \times (d - a/2) \right]$$



A floor system consists of 3.5" concrete slab supported by 16' simple span spaced at 9' c/c the beam having a width of 18" and effective depth of 18" and total height is 23". Calculate the necessary flexural reinforcement if the factored applied moment is 5800 kip-inch. Use  $f'_c = 3 \text{ ksi}$  and  $f_y = 60 \text{ ksi}$ .

Given :-

Height of flange = 3.5"

c/c distance = 16'

Length/span of the beam = 16'

web width ( $b_w$ ) = 18"

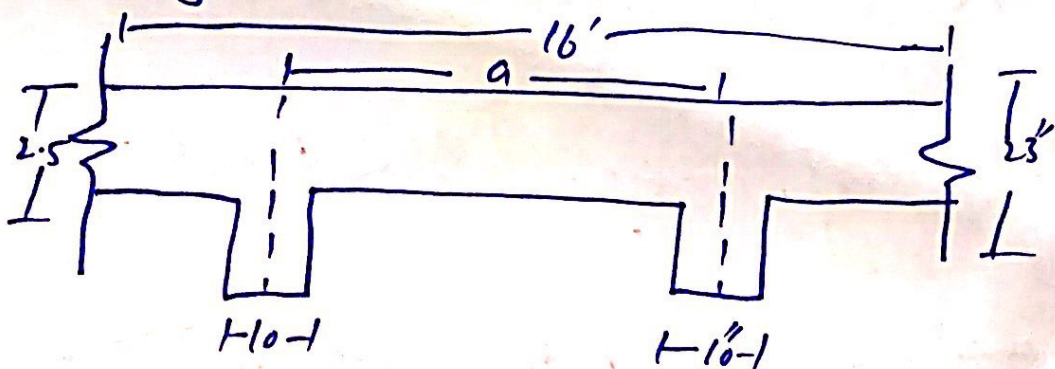
effective depth = 18"

Total factored moment ( $M_u$ ) = 5800 kip-inch

$f'_c = 3 \text{ ksi}$

$f_y = 60 \text{ ksi}$

Sol :-



Step # 1:- Calculate the effective width for T-Beam

1 -  $16(h_f) + b_w = 16(3.5) + 10 = 66''$

2 - c/c distance =  $9 \times 12 = 108''$

3 - Span/4 =  $\frac{16}{4} \times 12 = 48''$

Selecting the least value of  $b_e$  as,

$b_e = 48''$

Step # 2:- Check whether Rectangular or T-Beam Analysis is required.

Trial # 01:- Let  $a = h_f = 3.5''$

$A_{ST} = \frac{M_u}{\phi \times f_y \times (d - a/2)} = \frac{5800}{0.90 \times 60 \times (18 - 3.5/2)} = 6.61 \text{ in}^2$

Trial # 02:-  $a = \frac{A_{ST} \times f_y}{0.85 \times f'_c \times b_e}$

$a = \frac{6.61 \times 60}{0.85 \times 3 \times 48} = 3.2''$

$A_{ST} = 6.55 \text{ in}^2 \Rightarrow 2.2'' < 3.5''$

So Rectangular Beam Design is Required.

Trial # 3:-  $a = 3.2''$

$A_{ST} = \frac{5800}{0.90 \times 60 \times (18 - \frac{3.2}{2})} = 6.55 \text{ in}^2$

So Area of steel is  $6.55 \text{ in}^2$

Step # 03! - check  $S_{max}$  and  $S_{min}$

$$\Rightarrow S_{max} = 0.85 \times B \times \frac{f'_c}{f_y} \left( \frac{\epsilon_y}{\epsilon_u + \epsilon_t} \right)$$

$$= 0.85 \times 0.85 + \frac{3}{60} \left( \frac{0.003}{0.0003 + 0.0005} \right) = 0.013$$

$$\Rightarrow S_{min} = \frac{200}{f_y} = \frac{200}{60000} = 0.003$$

$$\Rightarrow S = \frac{A_{st}}{b \times d} = \frac{6.55}{10 \times 18} = 0.036$$

$$S_{min} < S < S_{max}$$

$$0.003 < 0.036 < 0.013$$

$\Rightarrow$  First we have to find the area of steel against  $S_{max}$

$$S_{max} = \frac{A_{st}}{b \times d} \Rightarrow A_{st} = S_{max} \times (b \times d)$$

$$A_{st} = 0.013 \times (10 \times 18)$$

$$A_{st} = 2.34 \text{ in}^2$$

Step # 4! - Finding the value of  $M_{uz}$

By formula

$$M_{uz} = \phi \times A_{st} \times f_y \times (d - a/2)$$

First finding the value of "a"

$$\Rightarrow a = \frac{A_{st} \times f_y}{0.85 \times f'_c \times b} = \frac{2.43 \times 60}{0.85 \times 3 \times 10}$$

$$e = 5.72''$$

7839 (21)

$$\Rightarrow M_{u2} = 0.90 \times 2.43 \times 60 \times (18 - 5.72/2)$$

$$M_{u2} = 1936.67 \text{ kip-inch}$$

$$\text{As } M_{u2} < M_u$$

So we have to design the beam in such way that it can resist more bending moment than the applied external moment.

Step # 5 :-

Finding difference of moment, And Area of steel :-

$$M_{u1} = M_u - M_{u2}$$
$$= 5800 - 1936.67$$

$$M_{u1} = 381.33 \text{ kip-inch}$$

By Formula

$$A_{st} = \frac{M_u}{\phi \times f_y \times (d - d')} = \frac{3813.33}{0.90 \times 60 \times (18 - 2.5)}$$

$$A_{st} = 4.56 \text{ in}^2$$

Step # 6 :-

Finding total steel area :-

$$A_s = A_{st} = A'_{st}$$

$$= 2.43 + 4.56 = 6.99 \text{ in}^2$$

Step #7:- Selection of Bars:-

In tension zone:-

let we use #8 bar

$$\text{dia} = (3/8) = 1'' \quad \therefore \text{Area} = \frac{\pi}{4} (1)^2 = 0.785 \text{ in}^2$$

By formula

$$\text{No. of Bars} = \frac{\text{Area of Steel}}{\text{Area of single bar}} = \frac{6.99}{0.785} = 8.9 \approx 9$$

So 9 #8 bars.

In Compression zone:-

let we use #7 bars

$$\text{dia} = (7/8)'' \quad \therefore \text{Area} = \frac{\pi}{4} (7/8)^2 = 0.601 \text{ in}^2$$

By formula

$$\text{No. of Bars} = \frac{\text{Area of Steel}}{\text{Area of single Bar}} = \frac{4.56}{0.601} = 7.5 \approx 8$$

So 8 #7 bars

Step #8:-

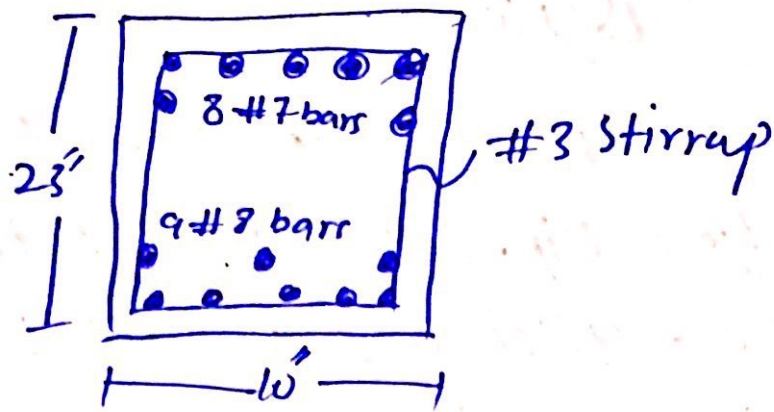
minimum width for accommodation Bars:-

$$b_{\text{min}} = (2 \times 1.5) + (2 \times 3/8) + 9(3/8) + 8(3/8)$$

$$= 20.75''$$

$$\text{As } 20.75'' > 10''$$

So the bars will be placed in multiple layers.



$$\text{Effective depth} = 23 - 1.5 + \frac{3}{8} + \frac{3}{8} + \frac{1}{2} \left( \frac{3}{8} \right) = 19.6''$$

$$\text{Effective cover} = 1.5 + \frac{3}{8} + \frac{7}{8} + \frac{1}{2} \left( \frac{7}{8} \right) = 3.18''$$

Step # 9 :- Find the design moment.

$$m_d = \phi \left[ A_s \times f_y \times (d - d') + (A_s - A_{st}) \times f_y \times \left( d - \frac{a}{2} \right) \right]$$

$$\text{First } a = \frac{(A_s - A_{st}) \times f_y}{0.75 \times f'_c \times b} = \frac{9 \times 0.75 - 8 \times 0.601 \times 60}{0.75 \times 3 \times 10} = 5.31''$$

$$\Rightarrow m_d = 0.90 \left[ 8 \times 0.601 \times 60 \times (19.6 - 3.18) + (9 \times 0.75 - 8 \times 0.601) \times 60 \times \left( 19.6 - \frac{5.31}{2} \right) \right]$$

$$\Rightarrow m_d = \boxed{6328.38}$$

As  $6328.38 > 5800 \rightarrow$  So design is OK!





7839 (27)

Q No 6

A beam is required to develop and ultimate moment of 6000 kip-inches limited to 14x26 inch size, use  $f'_c = 4 \text{ ksi}$  and  $f_y = 60 \text{ ksi}$ . Determine flexural reinforcement assume two rows of tensile reinforcement and effective depth of beam is 22 inches.

Sol:-

Given data:-

$$\text{Breadth} = 14''$$

$$\text{Height} = 26''$$

$$\text{Concrete Compression Strength } (f'_c) = 4 \text{ ksi}$$

$$\text{Steel tensile strength } (f_y) = 60 \text{ ksi}$$

$$\text{ultimate factored moment } (M_u) = 6000 \text{ kip-inches}$$

$$\text{Effective depth of beam} = 22''$$

$$\text{Assume effective cover } (d') = 2.5''$$

Step # 1:- (Reinforcement Ratio)

By Formula

$$\rho_{\max} = 0.85 \times \beta \times \frac{f'_c}{f_y} \times \left( \frac{\epsilon_u}{\epsilon_u + \epsilon_y} \right)$$

$$= 0.85 \times 0.85 \times \frac{4}{60} \times \left( \frac{0.003}{0.003 + 0.005} \right)$$

$$\boxed{I_{max} = 0.0180}$$

Step #2 :- (Area of Steel)

we know that

$$I_{max} = \frac{A_{st}}{b \times d} \Rightarrow A_{st} = I_{max} \times (b \times d)$$

$$\Rightarrow A_{st} = 0.0180 \times (14 \times 22) = \boxed{5.54 \text{ in}^2}$$

Step #3 :- (Design Moment)

By using formula

$$m_u = \phi \times A_{st} \times f_y \times (d - a/2)$$

$$\Rightarrow a = \frac{A_{st} \times f_y}{0.85 \times f'_c \times b} = \frac{5.54 \times 60}{0.85 \times 4 \times 14} = \boxed{6.98''}$$

$$\text{So, } m_u = 0.90 \times 5.54 \times 60 \times \left(22 - \frac{6.98}{2}\right)$$

$$= 5537.4 \text{ kip-inch}$$

$$\text{As, } 5537.4 < 6000$$

So we have to design a section as doubly

Reinforcement :-

Step # 4      Difference In Moments:-

$$m_{u1} = M_u - m_{u2}$$

$$= 6000 - 5537.4$$

$$m_{u1} = 462.6 \text{ kip-inches}$$

Step # 5:-      Area of Steel

$$m_{u1} = \phi \times A'st \times f_y \times (d-d')$$

So Area of steel in compression zone will be,

$$\rightarrow A'st = \frac{m_{u1}}{\phi \times f_y \times (d-d')} = \frac{462.6}{0.90 \times 60 \times (22 - 2.5)}$$

$$\rightarrow A'st = 0.44 \text{ in}^2$$

Step # 6:-      Total Steel Area:-

$$A_{sF} = A_{st} + A'st$$

$$= 5.54 + 0.44 = 5.98 \text{ in}^2$$

Step # 7:-      Selection and No. of bars used:-

1- Steel in Tension zone:-

we use # 7 bars

$$dia = (7/8)'' = 0.875'' , \text{ Area} = \frac{\pi}{4} (0.875)''^2$$

$$= 0.60 \text{ in}^2$$

So, No. of Bars =  $\frac{A_{st}}{\text{Area of single Bars}}$   
 $= \frac{5.98}{0.601} = 9.9 \approx 10 \text{ bars}$

So 10 #7 bars

(2) - Steel in Compression zone! -

we use #5 bar,

dia =  $(5/8)'' = 0.625''$ , Area =  $\frac{\pi}{4} (0.625)''^2$   
 $= 0.306 \text{ in}^2$

So No. of bar =  $\frac{A'_{st}}{\text{Area of single bars}}$   
 $= \frac{0.44}{0.306} = 1.43 \approx 2 \text{ bars}$

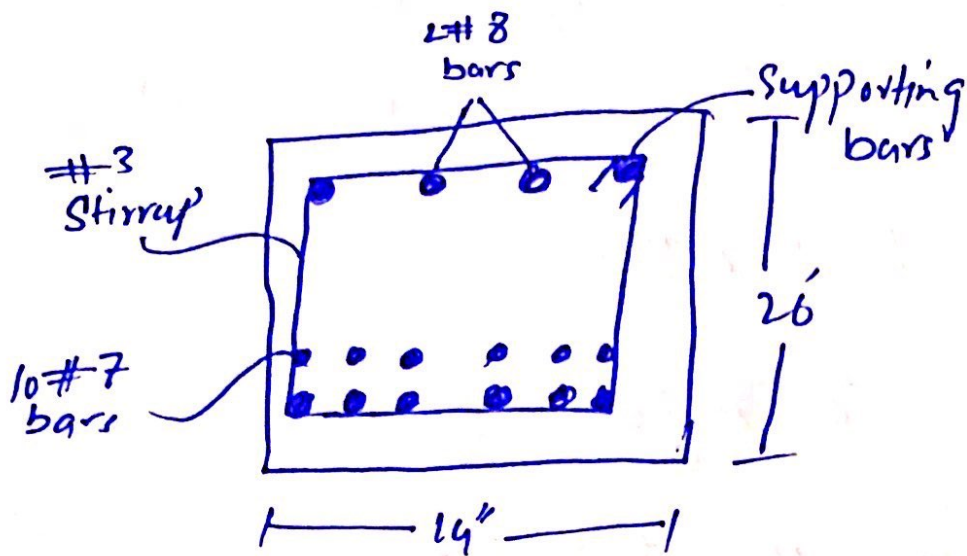
So 2 #5 bars

Step #8! - Minimum Width of Beam! -

$b_{min} = 2(1.5) + 2(3/8) + 10(7/8) + 9(7/8)$

$b_{min} = 20.37 > 14''$

So not good in one layer



$$\text{Now} \Rightarrow \text{effective depth} = 26 - 1.5 - 3/8 - 7/8 - 1/2(7/8) \\ = 22.82''$$

$$\Rightarrow \text{effective cover} = 1.5 + 3/8 + 1/2(5/8) = 2.18''$$

Step #9 :-

$$M_d = \phi \left[ A_s' f_y (d - d') + (A_{st} - A_s') f_y (d - a/2) \right]$$

$$a = \frac{(A_{st} - A_s') f_y}{0.85 f_c' b}$$

$$= \frac{(10 \times 0.601 - 2 \times 0.306) \times 60}{0.85 \times 4 \times 14} = 6.80''$$

$$M_d = 0.90 \left[ (2 \times 0.306) \times 60 \times (22.82 - 2.18) + (10 \times 0.601 - 2 \times 0.306) \right. \\ \left. \times 60 \times (22.82 - 6.80/2) \right]$$

$$M_d = 7047.6 \text{ kip-inches}$$

$$\text{As } 7047.6 > 6000$$

Design is OK!

