

Final Term Exam Summer Semester 2020

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Subject: Steel structures

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Q1:- Select the Lightest W shape of A-36 Steel . . .

-- Use AISC / LRFD Method.

Lightest W-shape column
A36 steel

$$DL = 60k \quad LL = 110k$$

Pin supported at top and bottom

$$K_x L_x = 36ft \quad K_y L_y = 18ft$$

AISC / LRFD Method.

Solution: Required Capacity = $(1.2 \times 60) + (1.6 \times 110)$
 $= 248k$

Enter design strength table of manual with
 $K L = 18ft$ and $P = 248k$.

Some possible sections are:

| | | | |
|----------------------|---|----------|------------------|
| W ₁₄ x 61 | - | P = 364k | $r_x/r_y = 2.44$ |
| W ₁₂ x 53 | | P = 320k | $r_x/r_y = 2.11$ |
| W ₁₀ x 49 | | P = 301k | $r_x/r_y = 1.71$ |
| W ₈ x 58 | | P = 300k | $r_x/r_y = 1.74$ |

Now

$$\frac{K_x L_x}{K_y L_y} = \frac{36}{18} = 2$$

Try W₁₂ x 53 $r_x/r_y = 2.11$

$$\frac{r_x}{r_y} > \frac{K_x L_x}{K_y L_y}$$

$$r_x = 5.23 \quad r_y = 2.48 \quad A = 15.6 \text{ in}^2$$

$$\frac{K_x L_x}{r_x} = \frac{36 \times 12}{5.23} = 82.6$$

①

$$k_y \frac{F_y}{r_y} = \frac{18 \times 12}{2.48} = 87.09.$$

$$\frac{KL}{r} = 87.09.$$

$$\begin{aligned} \lambda_c &= \frac{KL}{r\pi} \sqrt{\frac{F_y}{e}} \\ &= \frac{87.09}{\pi} \sqrt{\frac{36}{29,000}} \\ &= 0.97 < 1.5 \end{aligned}$$

$$\begin{aligned} F_{cr} &= 0.658^{\lambda_c^2} \times F_y \\ &= 0.658^{(0.97)^2} \times 36 \end{aligned}$$

$$F_{cr} = 24.28$$

$$\begin{aligned} P_n &= A_g F_{cr} \\ &= 15.6 \times 24.28 \end{aligned}$$

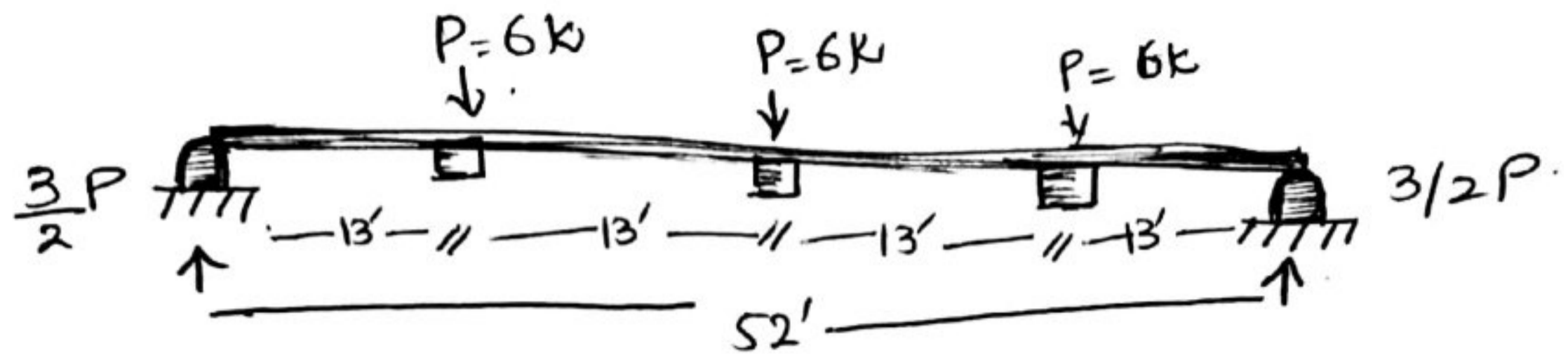
$$P_n = 378.78 \text{ k.}$$

$$\begin{aligned} \phi P_n &= 0.85 \times 378.78 \\ &= 321.96 > 248 \text{ k.} \\ &\text{OK.} \end{aligned}$$

So, use

W12 x 53

Q2: Determine the Lightest W section to support concentrated loads Use AISC / ASD Method.



→ Lightest W-section.

→ D.L. = 1.5 k L.L. = 4.5 k.

(At each quarter point)

→ Total length = 52'

→ Live load deflection = $\frac{1}{360}$ of span.

→ $F_y = 36 \text{ ksi}$

AISC / ASD Method.

Solution:

Design load = $4.5 + 1.5 = 6 \text{ k}$.

$P = 6 \text{ k}$.

$$\Delta = \frac{5}{48} \frac{ML^2}{EI} \quad \text{--- (1)}$$

Δ by this equation is multiplied by the factor from table 5.4.

$$M = \left(\frac{3}{2} \times 6 \times 26 \right) - (6 \times 13) = 156 \text{ k-ft}$$

$$\text{eqn (1)} \Rightarrow I = \frac{5}{48} \times \frac{ML^2}{E\Delta} \times 0.95$$

$$I = \frac{5}{48} \frac{(156 \times 12) (52 \times 12)^2}{29,000 \left(\frac{52}{360} \times 12 \right)}$$

$$I = 1510.51 \text{ in}^4 \times 0.95 \quad \boxed{I = 1434.98 \text{ in}^4}$$

Try W24x62 : $I_x = 1550 \text{ in}^4$
 $bf = 7.04 \text{ in}, \frac{d}{A_f} = 5.72$

$$L_c = \frac{76 bf}{\sqrt{f_y}} \Rightarrow \frac{76 \times (7.04)}{\sqrt{36}} = 89'' = 7.41'$$

$$L_c = \frac{20,000}{f_y \frac{d}{A_f}} \Rightarrow \frac{20,000}{36 \times 5.72} = 97.12'' = 8.09'$$

$$L > L_c$$

from table S-2.
 $C_b = 1.13$

$$\sqrt{\frac{102,000 C_b}{F_y}} = \sqrt{\frac{102,000 \times 1.13}{36}} = 57$$

$$\sqrt{\frac{510,000 C_b}{F_y}} = \sqrt{\frac{510,000 \times 1.13}{36}} = 127$$

$$\frac{L}{r_T} = \frac{13 \times 12}{1.71} = 91.22$$

Condition : $\sqrt{\frac{102,000 C_b}{F_y}} \leq \frac{L}{r_T} < \sqrt{\frac{510,000 C_b}{F_y}}$

So:- $F_b = \left[\frac{2}{3} - \frac{F_y \left(\frac{L}{r_T} \right)^2}{1530 \times 10^3 \times C_b} \right] F_y$
 $= \left[\frac{2}{3} - \frac{36 (91.22)^2}{1530 \times 10^3 \times 1.13} \right] 36$

$$F_b = 17.76 \text{ ksi allowable}$$

The beam self weight = $\frac{62 \text{ lb}}{\text{ft}} = 0.062 \text{ k/ft}$

$$M = \frac{wL^2}{8} = \frac{1}{8} (0.062) (52)^2$$

$$M = 20.95 \text{ k}\cdot\text{ft}$$

$$\text{Total } M = 156 + 20.95$$

$$M = 176.95$$

$$S_x = 131$$

$$f_b = \frac{M}{S_x} \Rightarrow \frac{176.95 \times 12}{131} = 16.2 \text{ ksi}$$

$$f_b < F_b$$

OK

Use W24 x 62

Q3: Determine an A-36 double-angle tension...

... Use ASD Method.

Sol: Given D.L = 50k

L.L = 150k

BoHs Dia = $\frac{3}{4}$ "

Length = 18ft

Connection Type = Bearing

ASD Method.

Required : Design A36 steel double angle
tension member

Solution:

$$\begin{aligned}\text{Total load} &= D.L + L.L \\ &= 50 + 150 \\ &= 200 \text{ k or } 100 \text{ k/Angle.}\end{aligned}$$

→ For yielding at the gross area allowable stresses are

$$0.6 F_y = 0.6 \times 36 = 22 \text{ ksi}$$

→ For Fracture at the net area allowable stresses are

$$0.5 F_u = 0.5 \times 58 = 29 \text{ ksi}$$

Since, the connection is bolted so,

$$A_g \neq A_n$$

$$\text{Now } A_e = 0.85 A_n$$

$$\text{For yielding } A_g \times 22 = 100$$

$$A_g = \frac{100}{22}$$

$$A_g = 4.54 \text{ in}^2$$

For Fracture.

$$29 \times A_e = 100$$

$$A_e = 3.44 \text{ in}^2$$

$$A_n = \frac{A_e}{0.85} \Rightarrow \frac{3.44}{0.85} \Rightarrow A_n = \boxed{4.04 \text{ in}^2}$$

Assume 15% deduction in gross area for holes

$$\text{So, } A_g = \frac{A_n}{0.85} \Rightarrow A_g = \frac{4.04}{0.85}$$

(6)

$$A_g = 4.76 \text{ in}^2$$

For $L_4 \times 4 \times 5/8$ $A_g = 4.61 \approx 4.76$ OK.

$r_x = 1.20$ $r_y = 1.20$ with $3/8$ in gusset plate

$$\frac{L}{r_{\min}} = \frac{18 \times 12}{1.20} = 180 \leq 300 \text{ K}$$

OK.

Bolts Design.

using A325 bolts with threads included in shear plane as $\text{dia} = 3/4$ ".

$$\text{Area} = \frac{\pi}{4} (d)^2 \Rightarrow \frac{\pi}{4} (0.75)^2$$

$$A = 0.44 \text{ in}^2$$

Allowable bolts shear = 21 ksi.

Since, bolts are in double shear so allowable shear per bolt = $2 \times 21 \times 0.44 = 18.5 \text{ K}$

Allowable bolt bearing stress = $1.2 F_u = 1.2 \times 58 = 69.6 \text{ ksi}$

Allowable bearing on two $5/8$ " thick angle

$$\text{long legs} = 69.6 \times 2 \times 5/8 \times 0.75 = 65.25 > 18.5$$

So, Shear governs.

$$\text{Number of bolts} = \frac{200}{18.5} = 10.81$$

use 10 bolts.

Design of gusset plate:

$$\text{Bearing stress} = \frac{1.2 F_u}{1.2 \times 58} = 69.6 \text{ ksi}$$

(7)

c. Allowable bearing = $69.6 \times 10 \times 0.75 \times t$
 $= 200$

$t = 0.38 \text{ in}$

use $\frac{3}{4}$ " G.P.

Checking various limit states

yielding = $0.6 F_y A_g$
 $= (0.6) F_y A_g$
 $= 0.6 \times 36 \times (8 \times 0.75)$
 $= 129.6 \text{ k} < 200 \text{ k}$

Not OK

Try $L \times 4 \times \frac{1}{2}$ $A_g = 5.25$

$r_x = 2.25$ $r_y = 1.11$ with $\frac{3}{8}$ " G.P.

$\frac{1}{r_{min}} = \frac{18 \times 12}{1.11}$ $194.59 \leq 300 \text{ k}$
 OK.

Allowable bearing on two $\frac{1}{2}$ " thick angle
 long leg = $69.6 \times \frac{1}{2} \times 2 \times 0.75$
 $52.2 > 18.5$

so shear governs.

Checking various limit states

yielding = $0.6 F_y A_g$
 $= 0.6 \times 36 \times (14 \times 0.75)$
 $= 226.8 > 200 \text{ k}$
 OK.

Fracture = $0.5 \times F_u \times A_e$
 $= 0.5 \times 58 \times 0.85 \left[14 - \left(\frac{3}{4}\right) \times 2 \right]^{3/4}$
 $= 231 \text{ k} > 200 \text{ k}$
 OK.

check for tearing failure

$$L_e = \frac{2P}{F_{ut}}$$

$$1.25 = \frac{2P}{58 \times 0.5}$$

$$(1.25)(58 \times 0.5) = 2P$$

$$P = 18.125 \text{ k.}$$

$$L = \frac{2P}{F_{ut}} \times \frac{d_b}{2}$$

$$2 = \frac{2P}{58 \times 0.5} + \frac{3/4}{2}$$

$$2(58 \times 0.5) = 2P = 0.375$$

$$116.1 - 0.375 = 2P$$

$$115.72 = 2P$$

$$P = 57.86 \text{ k.}$$

Capacity since 10 bolts and five bolts per row

$$2 \times 18.125 + 8 \times 57.86$$

$$499.13 \text{ k} > 200 \text{ OK}$$

