

STRUCTURE ANALYSIS 2

MID TERM



Submitted by:

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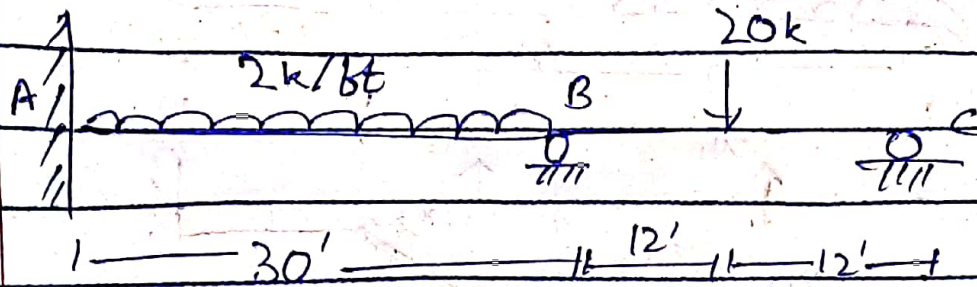
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Submitted to:

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Question # 01



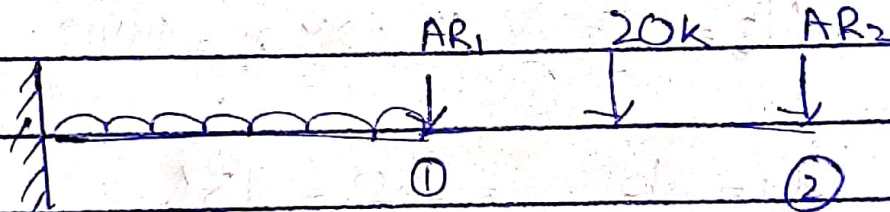
$EI = \text{constant}$

Sol

Structural indeterminacy = 2°

Step # 01

Select Redundant Actions

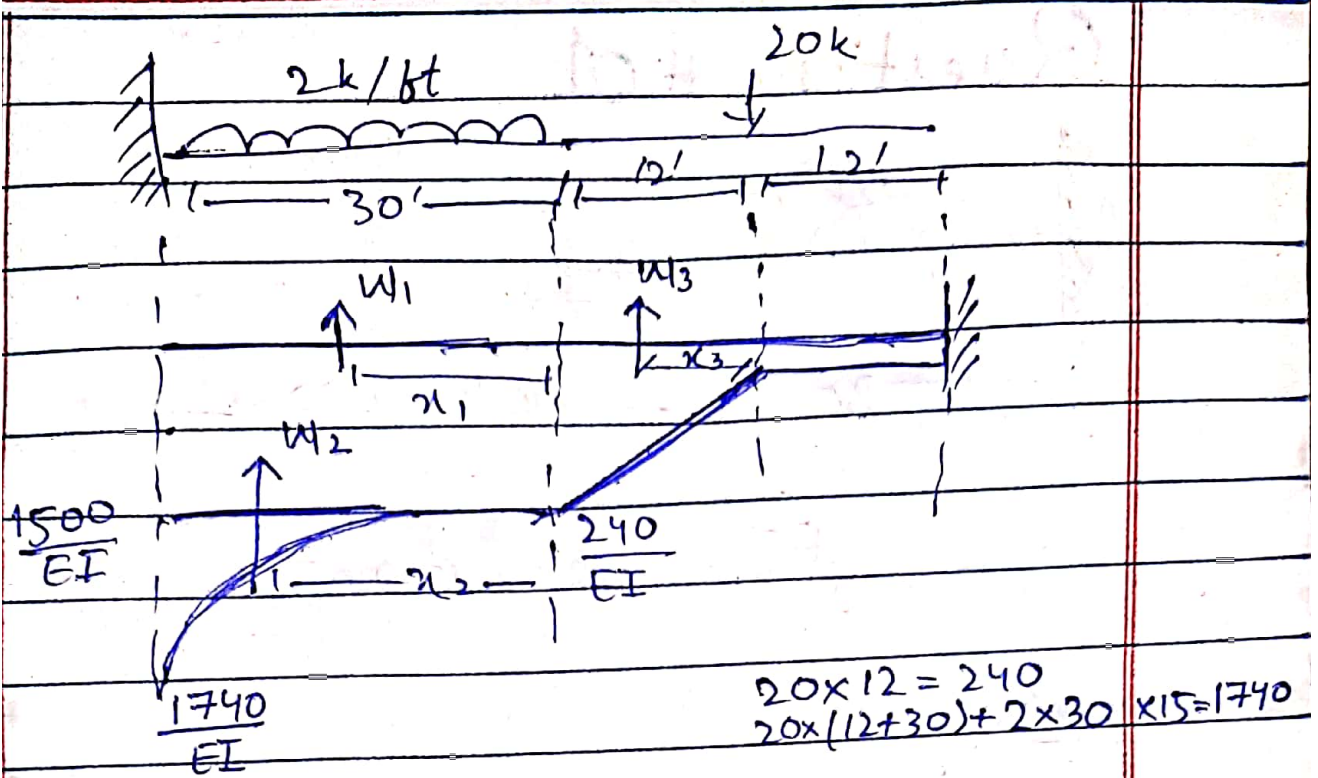


$$\begin{bmatrix} DRS_1 \\ DRS_2 \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \end{bmatrix} + \begin{bmatrix} AR_1 \\ AR_2 \end{bmatrix} - \begin{bmatrix} ? \\ ? \end{bmatrix}$$

$$[DRS] = [DRL] + [F] \times [AR]$$

Step # 02

Compute the values of [DRL]



$$W_1 = 1500 \times 30 = 45000$$

$$W_2 = \frac{1}{3} \times 30 \times 240 = 2400$$

$$W_3 = \frac{1}{2} \times 12 \times 240 = 1440$$

$$x_1 = \frac{b}{2} = \frac{30}{2} = 15'$$

$$x_2 = \frac{3}{n+2} \times L = \frac{3}{2+2} \times 30 = 22.5'$$

$$x_3 = \frac{2}{3} \times L = \frac{2}{3} \times 12 = 8'$$

Now Finding DRL

$$\begin{aligned}
 DRL_1 &= W_1(x_1) + W_2(x_2) \\
 &= 45000(15) + (2400)(22.5)
 \end{aligned}$$

$$DRL_1 = 675000 + 54000$$

$$DRL_1 = 729000/ET$$

$$\begin{aligned} DRL_2 &= W_1(x_1+24) + W_2(x_2+24) \\ &\quad + W_3(x_3+12) \\ &= 45000(15+24) + 2400(22.5+24) \\ &\quad + 1440(8+12) \\ &= 1755000 + 111600 + 28800 \end{aligned}$$

$$DRL_2 = 1895400/ET$$

So,

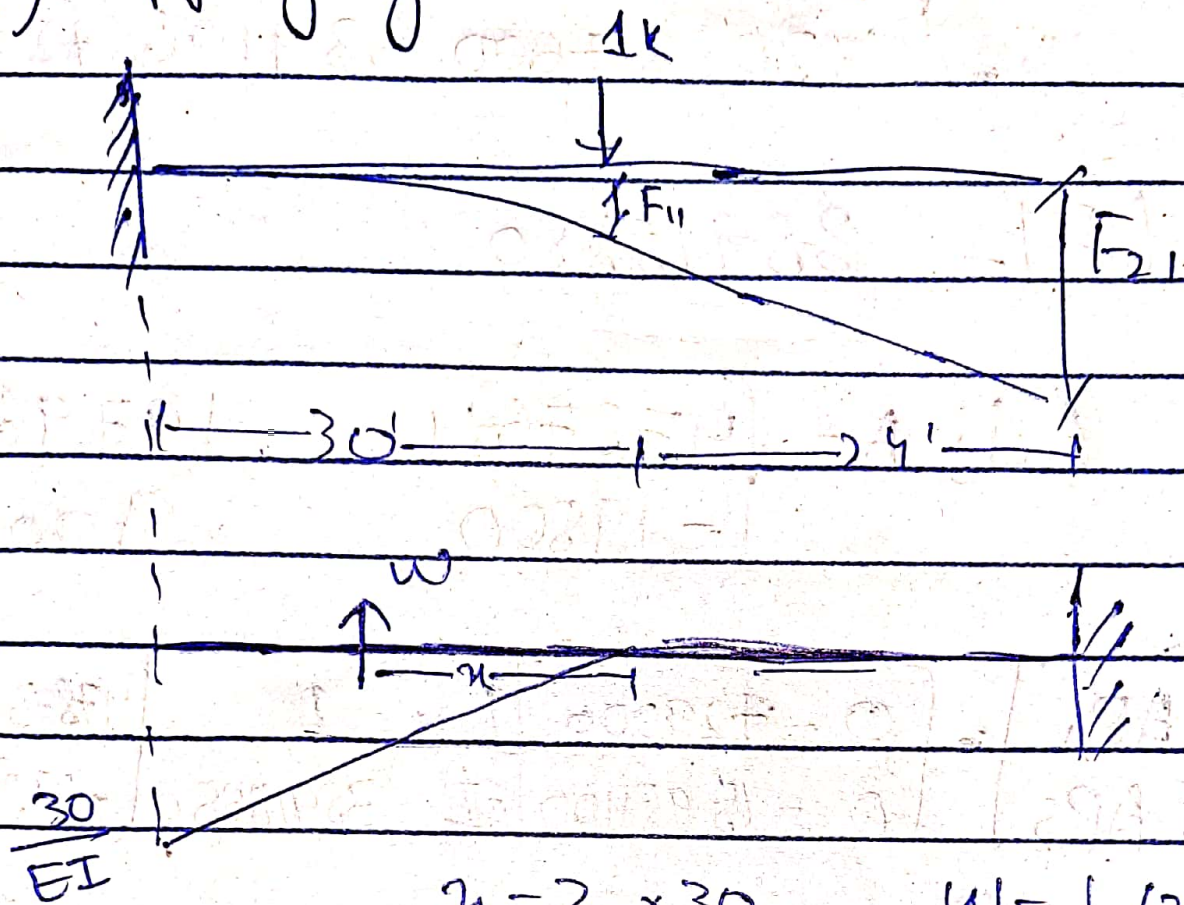
$$DRI = \frac{1}{ET} \begin{bmatrix} 729000 \\ 1895400 \end{bmatrix}$$

Step# 03

Flexibility Matrix

$$[F]_{2 \times 2} = \begin{bmatrix} F_{11} & F_{12} \\ F_{21} & F_{22} \end{bmatrix}$$

a) Applying unit load on AR,



$$n = \frac{2 \times 30}{3}$$

$$W = \frac{1}{2} \left(\frac{30}{EI} \times 30 \right)$$

$$x = 20'$$

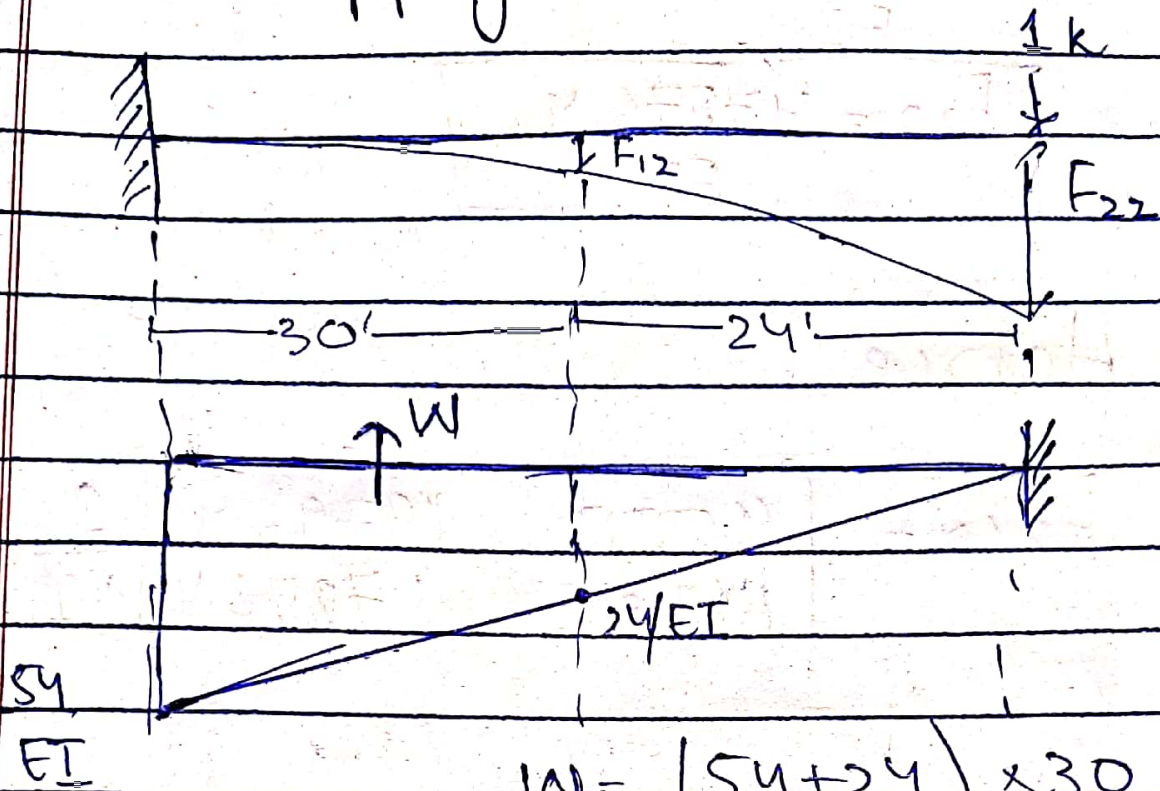
$$W = \frac{450}{EI}$$

So,

$$F_{11} = \frac{450 (20)}{EI} = \frac{9000}{EI}$$

$$F_{21} = \frac{450 (20+24)}{EI} = \frac{19800}{EI}$$

b) Now apply unit load on AR₂



$$W = \left(\frac{54 + 24}{2EI} \right) \times 30$$

$$= 1170/EI$$

Now the distance

$$x = \frac{L}{3} \left[\frac{b + 2(a)}{a + b} \right]$$

$$= \frac{30}{3} \left[\frac{24 + 2(54)}{54 + 24} \right] = 16.92'$$

$$\rightarrow F_{12} = \frac{1170 \times 16.92}{EI}$$

$$F_{12} = \frac{19796.4}{EI}$$

$$F_{22} = \frac{1170 \times (16.92 + 24)}{EI}$$

$$F_{22} = \frac{47876.4}{EI}$$

Hence

$$F_{2 \times 2} = \begin{bmatrix} 9000 & 19796.4 \\ 19800 & 47876.4 \end{bmatrix} \frac{1}{EI}$$

Step # 04

Compute the values of AR

$$[DRS] = [DRL] + [F] \times [AR]$$

$$[AR] = [DRS - DRL] \times [F]^{-1}$$

$$[F]^{-1} = \frac{1}{|F|} \text{Adj } F$$

$$= \frac{1}{\begin{vmatrix} 9000 & 19796.4 \\ 19800 & 47876.4 \end{vmatrix}} \times \text{Adj} \begin{bmatrix} 9000 & 19796.4 \\ 19800 & 47876.4 \end{bmatrix}$$

$$|F| = (9000 \times 47876.4 - 19796.4 \times 19800) \\ = (430887600 - 391968720)$$

$$|F| = 38918880$$

$$\text{Adj } A = \begin{bmatrix} 47876.4 & -19796.4 \\ -19800 & 9000 \end{bmatrix}$$

$$\begin{bmatrix} AR_1 \\ AR_2 \end{bmatrix} = \begin{bmatrix} 0 & -729000 \\ 0 & -1895400 \end{bmatrix} \frac{1}{EI} \times \frac{1}{38918880} \begin{bmatrix} 47876.4 & -19796.4 \\ -19800 & 9000 \end{bmatrix}$$

$$= \begin{bmatrix} -729000 \\ -1895400 \end{bmatrix} \frac{1}{EI} \times \begin{bmatrix} 47876.4 & -19796.4 \\ -19800 & 9000 \end{bmatrix} \\ 38918880$$

$$\begin{bmatrix} AR_1 \\ AR_2 \end{bmatrix} = \begin{bmatrix} 66.193 \\ -67.505 \end{bmatrix}$$

Question # 02

Force Method

It is also known as flexibility matrix method or compatibility method

In force method the unknown are taken as Force or reaction

In force method number of redundants = D_s

The forces are determined by compatibility equation of displacements

Displacement Method

It is also called as equilibrium method or stiffness matrix method

In displacement method the unknown are take as joint displacements (θ, Δ)

In displacement method number of redundants = D_k

In this method the displacements are determined by equilibrium equation of forces.

Force
Method

Displacement
Method

In this method type of indeterminacy is static

In this method type of indeterminacy is kinematic

This method is suitable when $D_s < D_k$

This method is suitable when $D_s > D_k$

Suitable Method For Structure Analysis Of Matrix Approach

• For analysis of structure of matrix approach both the force method or displacement method can be used depends upon situation

→ When the degree of static indeterminacy ^(D_s) is less than the degree of kinematic indeterminacy (D_k) i.e. $D_s < D_k$, then it is suggested to use force method

→ When the degree of static indeterminacy (D_s) is more than kinematic indeterminacy (D_k) i.e. $D_k < D_s$ then it is suggested to use displacement method of analysis.

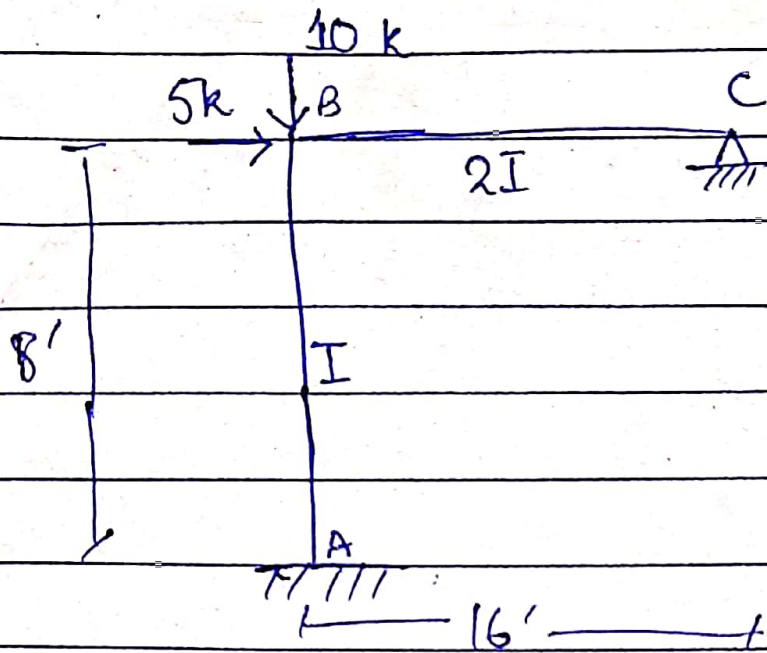
→ The main advantage of displacement method is ~~it~~ it is primary method used in matrix analysis.

→ Also displacement method is conducive to computer programming, once the analytical model of the structure has been defined no further engineering

decisions are required in the stiffness method in order to carry out the analysis.

Hence displacement method is suitable for structure analysis of matrix approach.

Question # 03



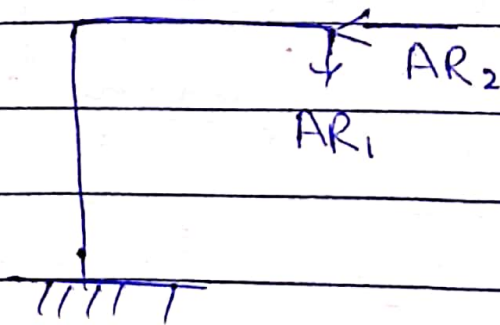
$E = \text{constant}$

Sol

Total statical indeterminacy
 $R - 3 = 5 - 3 = 2^\circ$

Step # 01

Identifying Redundant actions



$$\begin{bmatrix} AR_1 \\ AR_2 \end{bmatrix} = \begin{bmatrix} ? \\ ? \end{bmatrix}$$

$$\begin{bmatrix} DRS_1 \\ DRS_2 \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \end{bmatrix}$$

Step # 2

Compute value of [DRL]

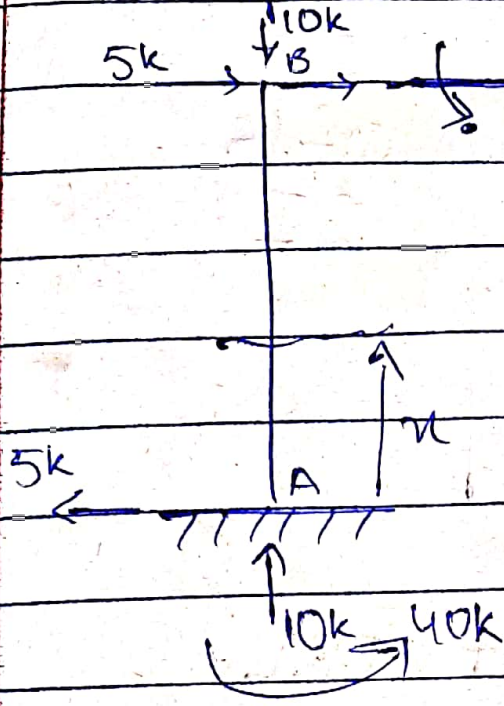


Fig AMIL value
(M values)

Step # 03

[F] or [AMR]

a)

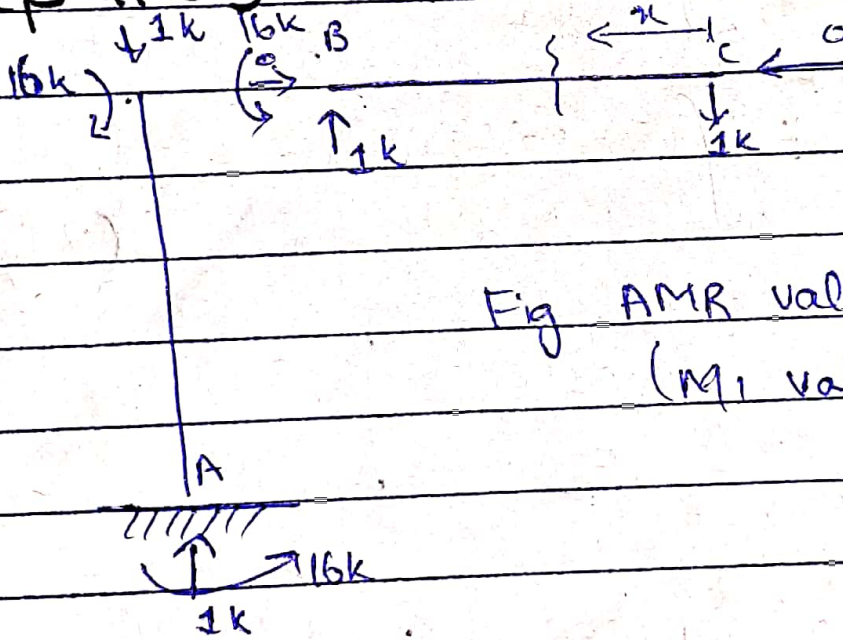


Fig AMR value
(M₁ values)

b)

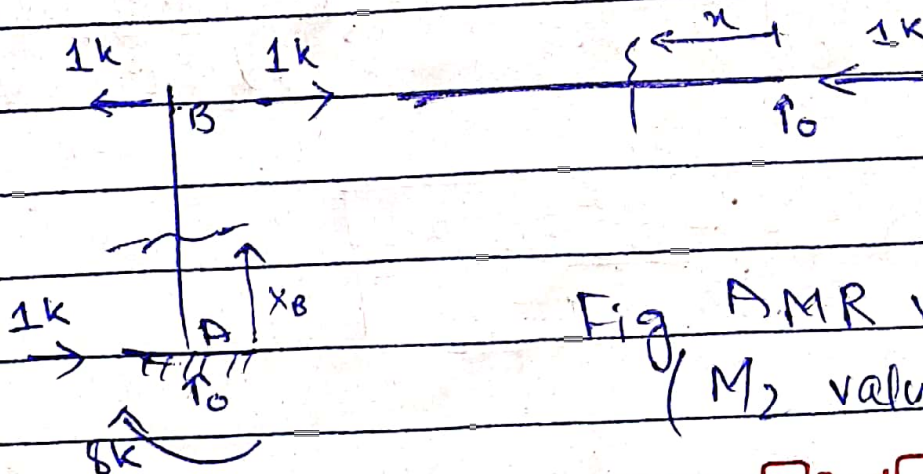


Fig AMR value
(M₂ value)

Member	AB	BC
Origin	A	C
Limits	0-8	0-16
I	I	2I
M	$5x-40$	0
m_1	-16	-x
m_2	$8-x$	0

→ Finding values of DRL

$$DRL_1 = \int_0^8 \frac{M_{AB} \cdot m_1(AB)}{EI} dx + \int_0^{16} \frac{M_{BC} \cdot m_2(BC)}{EI} dx$$

$$= \int_0^8 \frac{(5x-40)(-16)}{EI} dx + \int_0^{16} \frac{0 \cdot x}{E(2I)} dx$$

$$DRL_1 = \frac{2560}{EI}$$

$$DRL_2 = \int_0^8 \frac{(5x-40)(8-x)}{EI} dx + \int_0^{16} \frac{0 \cdot 0}{E(2I)} dx$$

$$DRL_2 = \frac{-853.33}{EI}$$

→ Compute Flexibility Matrix

$$F_{2 \times 2} \xrightarrow{2^0} = \begin{bmatrix} F_{11} & F_{12} \\ F_{21} & F_{22} \end{bmatrix}$$

$$\begin{aligned} \rightarrow F_{11} &= \int_0^8 \frac{m_1^2(AB)}{EI} dx + \int_0^{16} \frac{m_1^2(BC)}{EI} dx \\ &= \int_0^8 \frac{(-16)^2}{EI} dx + \int_0^{16} \frac{x^2}{E(2I)} dx \end{aligned}$$

$$F_{11} = \frac{2730.67}{EI}$$

$$\rightarrow F_{12} = F_{21} = \int_0^8 m_1(AB) \cdot m_2(AB) dx + \int_0^{16} m_1(BC) \cdot m_2(BC) dx$$

$$= \int_0^8 \frac{(-16)(8-x)}{EI} dx + \int_0^{16} \frac{(x)(0)}{E(2I)} dx$$

$$F_{12} = F_{21} = \frac{-512}{EI}$$

$$\begin{aligned} \rightarrow F_{22} &= \int_0^8 \frac{(m_2)^2_{AB}}{EI} dx + \int_0^{16} \frac{(m_2)^2_{BC}}{E(2I)} dx \\ &= \int_0^8 \frac{(8-x)^2}{EI} dx + \int_0^{16} \frac{0^2}{E(2I)} dx \end{aligned}$$

$$F_{22} = 170.67$$

As we know

$$[DRS] = [DRL] + [AR] \times [F]$$

$$[AR] = \frac{[DRS] - [DRL]}{[F]}$$

$$[AR] = [F]^{-1} \times [DRS - DRL]$$

$$= EI \begin{bmatrix} 2730.67 & -512 \\ -512 & 170.67 \end{bmatrix}^{-1} \times \begin{bmatrix} 0 & -2560 \\ 0 & 853.33 \end{bmatrix} \times \frac{1}{EI}$$

$$\begin{bmatrix} AR_1 \\ AR_2 \end{bmatrix} = \begin{bmatrix} -0.00005 \\ 4.97 \end{bmatrix}$$

$$\begin{bmatrix} AR_1 \\ AR_2 \end{bmatrix} = \begin{bmatrix} 0 \\ 5 \end{bmatrix}$$