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ID of section : 7925 (A)

Assignment# 03

Structural analysis

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4th semester

BE civil

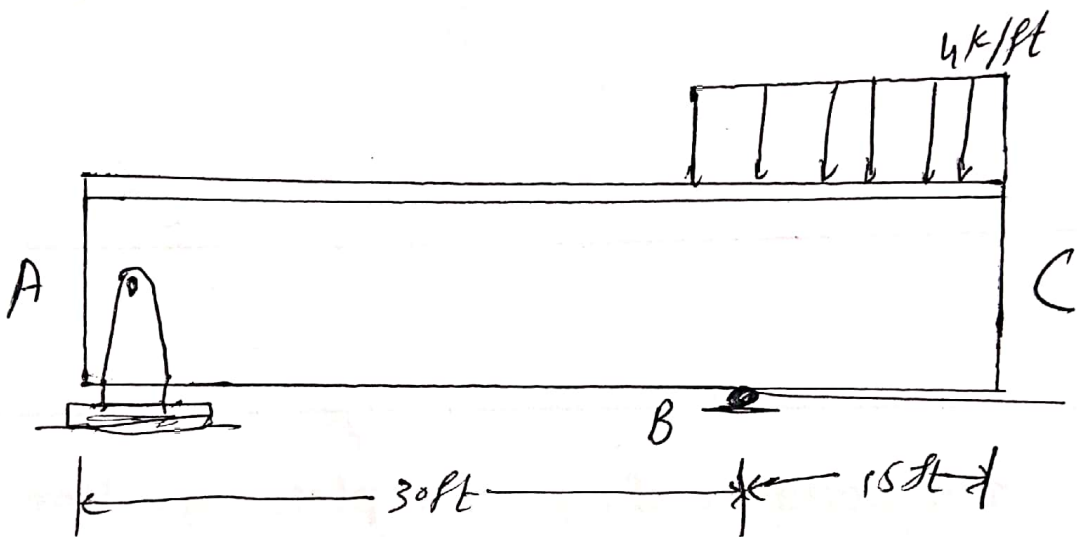
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Assignment # 3rd

Conjugate Beam Method

Q#1) Determine the slope and displacement at C,  $EI$  is constant.

Use the moment Area theorem



Solution  $\therefore \sum M_A = 0$

$$-V_B \times 30 + (4 \times 15) \times 3.75 = 0$$

$$V_B = 75 \text{ k}$$

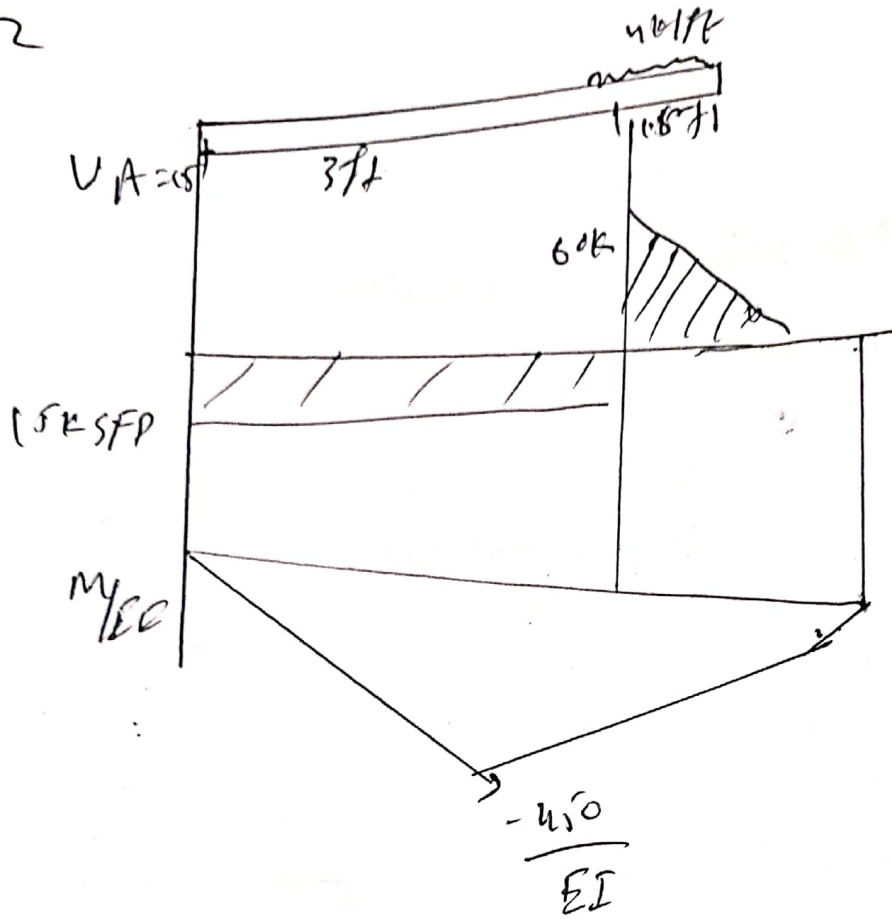
$$V_B = 75 \text{ k}$$

$$\sum M_B = 0$$

$$V_A \times 30 + (4 \times 15) \times 7.5 = 0$$

$$V_A = -15 \text{ k}$$

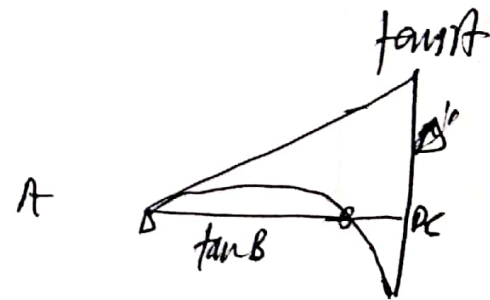
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Thus  $M/EI$  consist of triangle and

~~Parabola~~ <sup>Parabola</sup> segment

→ For Displacement



$$\frac{tC}{A} = DC + D'$$

$$DC = \frac{tC}{A} - D' \rightarrow \textcircled{1}$$

$$D' \leftarrow \frac{D'}{45} = \frac{tB/A}{30}$$

P-3

$$D' = \frac{3}{3} tB/A$$

ean (1)

$$DL = \frac{tC}{A} - \frac{3}{2} tB/A$$

tC/a:

$$tC/A = \left[ \frac{-450}{EI} \times 30 \times \frac{1}{2} \right] \times \left[ 15 + \frac{1}{3} + 30 \right] + \left[ \frac{3}{4} \times 15 \right]$$

$$\times \left[ \frac{1}{3} \times \frac{450}{EI} \times 15 \right]$$

$$\frac{tC}{a} = \frac{108750}{EI} - \frac{25312.5}{EI}$$

$$\frac{tC}{a} = -19406.5/EI$$

$$\text{For } tB/a = \left[ \frac{-450}{EI} \times \frac{30}{2} \right] \times \left[ \frac{1}{3} \times 30 \right]$$

$$tB/a = -67500/EI$$

$$P-4) \quad DC = \frac{-19406.5}{2} - \left( \frac{67500}{EI} \right) \times \frac{3}{2}$$

$$DC = \frac{-295312.5}{EI} \text{ kPa}^3$$

For Slope at B

$$\theta_B = \frac{DC}{15}$$

$$\theta_B = \left( \frac{295312}{EI} \right) // 15$$

$$\theta_B = \frac{19687.5}{EI} \text{ kPa}^3$$

Slope of the force at

point EC is nearly equal

to zero



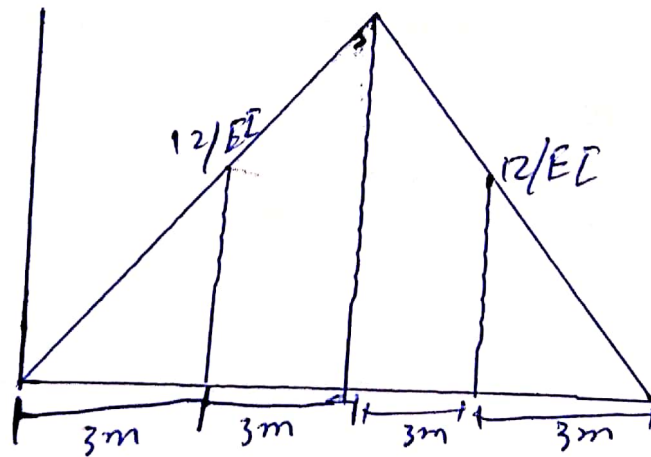
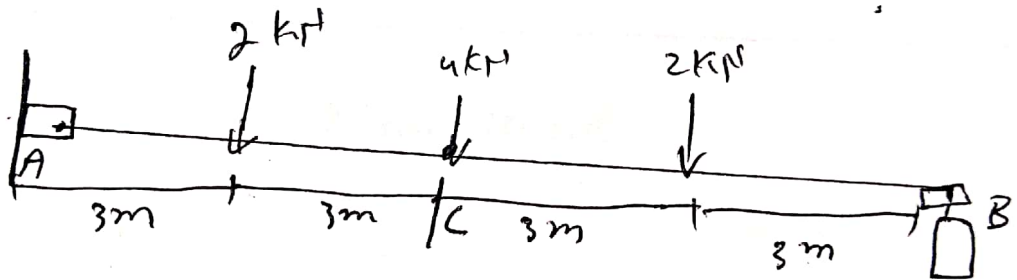
## Assignment #3

Q#2 :

Determine the slope at A and displacement at C of the beam in the figure moment area theorem Take  $E = 200 \text{ GPa}$

$$I_x = (6 \times 10^6) \text{ mm}^4$$

Solution :



$$\theta_{A/C} = \frac{1}{2} \left( \frac{12}{EI} \right) (3) + \left( \frac{12}{EI} \right) (3) + \frac{1}{2} \left( \frac{6}{EI} \right) (3)$$



$$\theta_{A/C} = \left(\frac{18}{EI}\right) + \left(\frac{36}{EI}\right) + \left(\frac{9}{EI}\right)$$

$$\theta_{A/C} = \frac{63}{EI} \Rightarrow \frac{63}{(200 \times 10^6)(6 \times 10^8)(1000)^2}$$

$$\theta_{A/C} = 0.0525 \text{ rad}$$

$$\theta_A = 0.0525 \text{ radian}$$

~~$$\theta_{A/C} = \left[\frac{1}{2} \left(\frac{18}{EI}\right) (3)\right]$$~~

$$\theta_{A/C} = \left[\frac{1}{2} \left(\frac{12}{EI}\right) (3)\right] \left[\frac{2}{3}(3)\right] + \left[\left(\frac{12}{EI}\right) (3)\right]$$

$$\left(3 + \frac{1}{2}(3)\right) + \left[\frac{1}{2} \left(\frac{6}{EI}\right) (3)\right] \left(3 + \frac{2}{3}(3)\right)$$

$$= 0.202 \text{ m}$$

So

$$DC = \theta_{A/C} = 0.202 \text{ m}$$

$$= 202 \text{ mm}$$

Ans