

Name: Hamad - Ali

ID: 16086

Subject: Applied Calculus.

Submitted to: Madam Shumaila.

## Application of derivatives in Engineering

important application in mathematics

- Rate of Change of Quantity.
- Increasing and decreasing functions.
- Tangent and normal to a Curve
- Minimum and maximum values.
- Newton Methods
- Linear Approximations.

### \* Rate of change of a Quantity

General and most important application of Derivatives. for Example

Check the rate of change of the volume with respect to its decreasing sides.



Form of derivatives used.

Page 2

$dy/dx$ .

$Dy$  represents rate of change of volume of cube.

$Dx$  represents change of sides of cube.

### \* Increasing and Decreasing Function.

To find that given function is increasing or decreasing or constant, say in graph, we use derivatives. If it is a function which is continuous in  $[p, q]$  and differentiable in the open interval than  $[p, q]$  then.

### Maxima and Minima.

To calculate the highest and lowest point of the curve in a graph or to know its function is used.

•  $x=a$ , if  $f(x) \leq f(a)$  for every  $x$  in the domain, then  $f(x)$  has an absolute. Point  $a$  is the point of the maximum value of  $f$ .

• when  $x=a$ , if  $f(x) \leq f(a)$  for every  $x$  in some open interval  $(p, q)$  than  $f(x)$  has a relative a relative maximum value.



- when  $x = a$ , if  $f(x) \geq f(a)$  for every  $x$  in domain. absolute minimum value
- when  $x = a$ , if  $f(x) \geq f(a)$  for every  $x$  in open interval.  
 $f(x)$  has a relative minimum value.

Approximation or finding Approximate value.

To a ~~find~~ find a very small change or variation of Quality, we can use derivatives to give the approximate value is represented by delta  $\Delta$ .

Suppose change in the values of  $x$ ,  $dx = \Delta x$

then  $dy/dx = \Delta y/\Delta x$

Since the change in  $x$ ,  $dx \approx \Delta x$  therefore  $dy \approx \Delta y$ .

Point of inflection

For continuous function  $f(x)$ , if  $f'(x_0) = 0$  or  $f''(x_0)$  does not exist at point where  $f'(x_0)$  exists and if  $f''(x)$  changes sign when passing through  $x = x_0$  then  $x_0$  is called the point of inflection.



## Application of Integration

- Area b/w Curves
- Volume
- work
- Kinetic energy: improper integral
- Arc length
- Distance, velocity, acceleration
- Average volume of Function
- Centre of mass
- probability
- Surface area.

### \* Area between Curves

We have seen how integration can be used to find area between a curve and  $x$ -axis with very little change we can find some areas b/w curves indeed the area b/w curve and the  $x$ -axis maybe interpreted as the area b/w the curve and a second "curve" with equation  $y=0$ . In the simplest of cases, the idea is quite easy to understand.

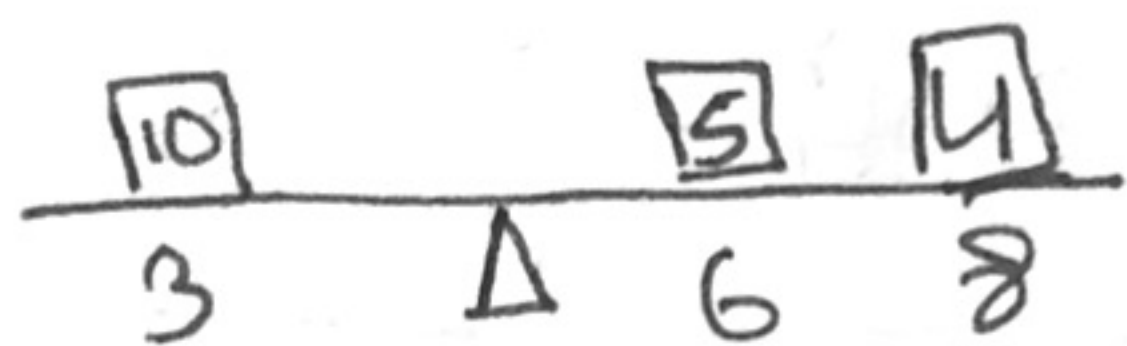
### \* Centre of Mass

Suppose a beam is 10 meters long and that there are three weights on the beam: a 10 kilogram weight 3 meters from the left end, a 5 kilogram weight 6 meters from the left end and a 5 kilogram weight 6 meters.



Pages

From the left end and a 4 kilograms weight 8 meters from the left end where should a fulcrum be placed so that the beam balances? Let's assign scale to the beam from 0 at the left end to 10 at the right, so that we can denote locations on the beam simply as coordinates the weights are at  $x=3$ ,  $x=6$  and  $x=8$ , as



Suppose to begin with with that fulcrum is placed at.

### \* Arc Length

Here is another geometric application of the integral. Find a length of a ~~portion~~ portion of a curve. As usual we need to think about how we might approximate the length and turn the approximation into integrals we already know how to compute one simple arc length, that of a line segment, if the endpoints are  $P_0(x_0, y_0)$  and  $P_1(x_1, y_1)$  then the length of the segment



is the distance b/w the

Points  $\sqrt{(x_1 - x_0)^2 + (y_1 - y_0)^2}$  From the

Pythagorean theorem as illustrated.

