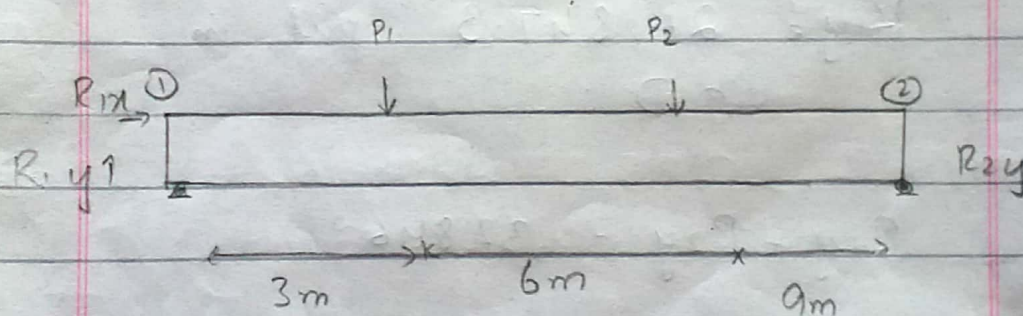


- ⇒ Name: AriZ-ullah
- ⇒ Id : 16073
- ⇒ Section: A
- ⇒ Paper: Eng: Mechanics - Final Paper:
- ⇒ Teacher: Sir - Majid Naem (sb)
- ⇒ Submitted: Sir - Majid Naem (sb)

α α ≡ ≡ ≡ ≡ ≡ α α

Answer # 01 ::

α  $\xrightarrow{\hspace{2cm}}$  α



$$\begin{aligned}
 P_1 &= 200 + \text{stu I.D} \\
 &= 200 + 16073 \\
 &= 16273
 \end{aligned}$$

$$\begin{aligned}
 P_2 &= 500 + \text{stu ID} \\
 &= 500 + 16073 \\
 &= 16573
 \end{aligned}$$

Sol:  $R_{1x} = 0$

$$\sum F_x = 0$$

Now

$$R_{1y} + R_{2y} - P_1 - P_2 = 0$$

$$\sum F_y = 0$$

$$R_{1y} + R_{2y} - 16273 - 16573 = 0$$

$$R_{1y} + R_{2y} - 32846 = 0$$
$$\boxed{R_{1y} + R_{2y} = 32846} \quad - \textcircled{1}$$

$$R_{1y} = \frac{[(16573 \times 9) + (16273 \times 15)]}{18} \quad \because \sum m_i = 0$$

$$R_{1y} = (149,157 + 244,095) / 18$$

$$R_{1y} = 393,252 / 18$$

$$R_{1y} = 21,847.3, \text{ put in eq } \textcircled{1}$$

$$R_{1y} + R_{2y} = 32846$$

$$R_{1y} = -R_{2y} + 32846$$

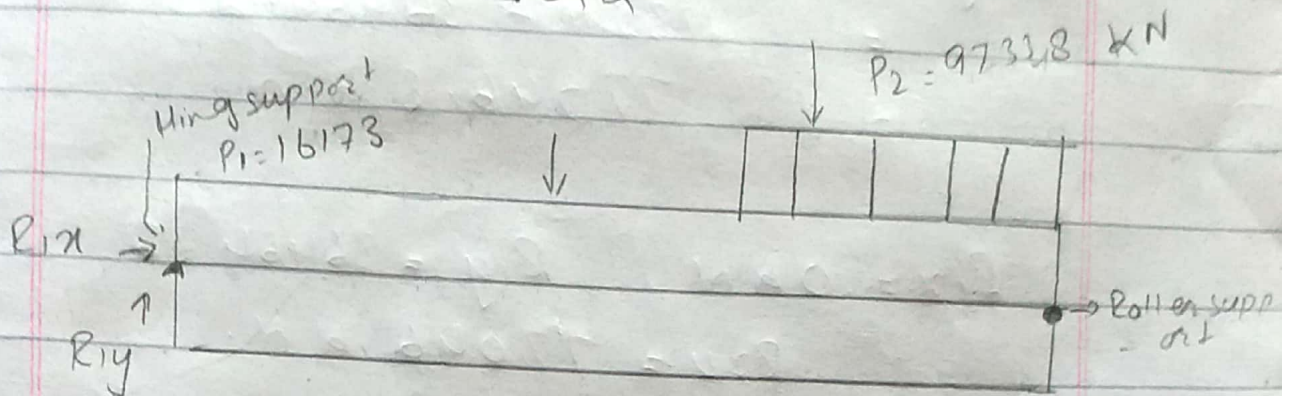
$$R_{1y} = 32846 - 21847.3$$

$$R_{2y} = 10,998.7$$

$$\left\{ \begin{array}{l} R_{1x} = 0, \quad R_{1y} = 21847.3 \\ \quad \quad \quad R_{2y} = 10998.7 \end{array} \right\}$$

$\alpha$  —————  $\alpha$

Answer: 02:-  
αα = αα



$$P_1 = 100 + \text{student ID}$$

$$= 100 + 16073 = 16173$$

$$\text{UDL} = 150 + \text{student ID}$$

$$= 150 + 16073 = 16223$$

$$\text{UDL Resultant} = (16223 \text{ kN/m} \times 6 \text{ m}) = 97338 \text{ kN}$$

$$R_{1x} = 0 \quad \sum F_x = 0$$

$$R_{1y} + R_{2y} - P_1 - P_2 = 0$$

$$R_{1y} + R_{2y} - 16173 - 97338 = 0$$

$$R_{1y} + R_{2y} = +113,511$$

$$R_{1y} = (97338 \times 3) + (16173 \times 9) / 12$$

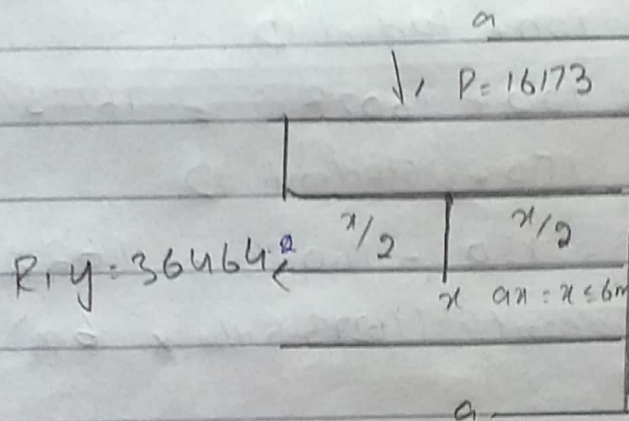
$$= \frac{292014 + 145557}{12}$$

$$= \frac{437571}{12}$$

$$= 36464.2 \text{ kN}$$

$$\begin{aligned}
 R_{2y} &= 113511 - R_{1y} \\
 &= 113511 - 36464 \cdot 2 \\
 &= 77046.8 \text{ kN}
 \end{aligned}$$

$$\begin{aligned}
 R_{1x} &= 0 \text{ kN}, & R_{1y} &= 36464 \cdot 2 \\
 R_{2y} &= 77046 \text{ kN}
 \end{aligned}$$



$$\text{Summation } F_y = 0$$

$$-v_a a - P + 36464 \cdot 2 \text{ kN}$$

$$v_a a = 36464 \cdot 2 - 16173 \text{ eqn 1}$$

To find the location of shear force let eqn equal to zero

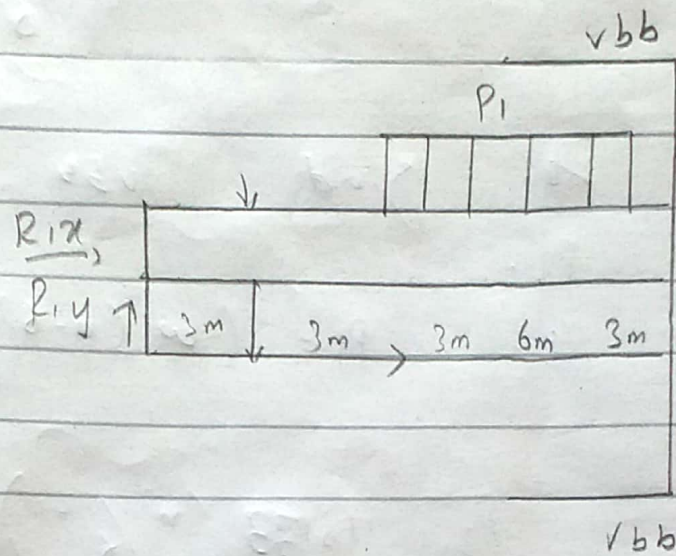
$$0 = 36464 \cdot 2 - 16173 x$$

$$x = \frac{36464 \cdot 2}{16173}$$

$$x = 2.25 \text{ m}$$

at  $x = 2.25$  the shear

will be zero.



From law of similar triangle

$$\frac{16173}{6m} = \frac{w \cdot kn/m}{(n-6)m}$$

$$6w \cdot kn = 16173n(n-6)$$

$$6w \cdot kn = 16173n^2 - 97038$$

$$w_0 = \frac{16173n^2 - 16173}{6}$$

$$\omega_0 = 16173 \left( \frac{n^4}{8} - 1 \right)$$

to find  $v_b$  find  
 $P_3$ .

$$P_3 = \left( \omega_0 (n-6) \right) / 2$$

$$P_3 = 16173 \left( \frac{n^4}{8} - 1 \right) (n-6) / 2$$

$$= 16173 \left( \frac{n^5}{8} - n^3 - n + 6 \right) / 2$$

$$P_3 = \frac{16173}{2} \left( \frac{n^5}{8} - n^3 - n + 6 \right)$$

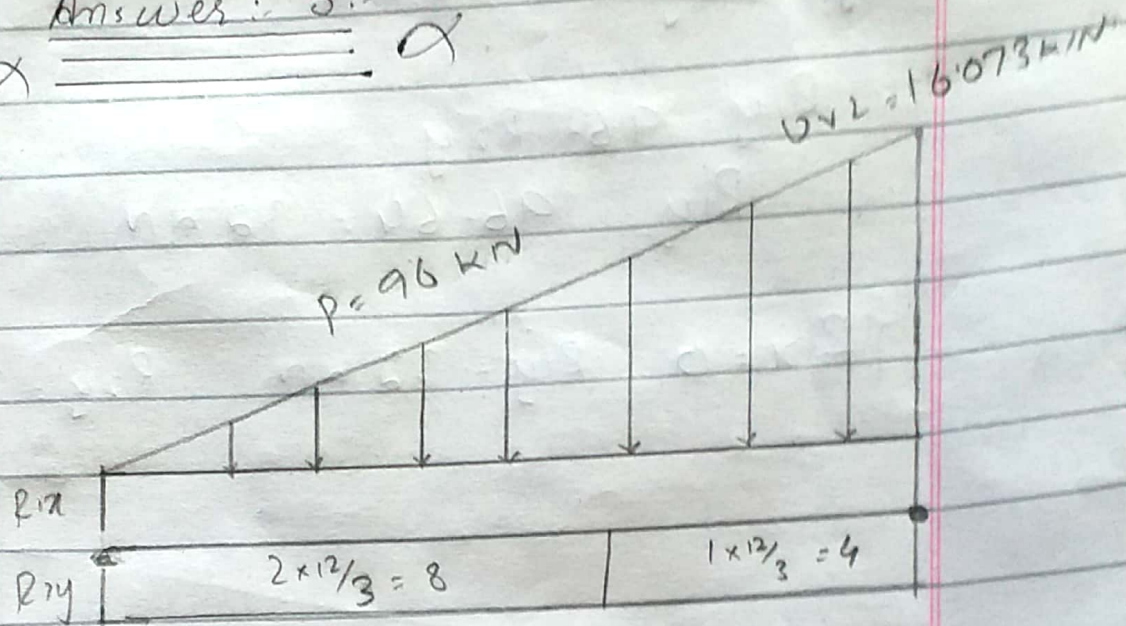
$$P_3 = 8086.5 \left( \frac{n^5}{8} - n^3 - n + 6 \right)$$

at  $n = 6m$

at  $n = 12$ , eq ①

$$v_b = 138.$$

⇒ Answer: 3:  $\alpha$



$$OVL = \text{Student} / 1000 = \frac{16073}{1000} = 16.073$$

$$OVL \text{ Resultant} = \left( \frac{16 \text{ kN/m} \times 12}{2} \right)$$

$$= 96 \text{ kN}$$

This load will act  $1/3$  of length from the maximum side

$$R_{1x} = 0 \quad - \quad \Sigma \mathcal{M} = 0 \quad \Sigma \mathcal{F}_x = 0$$

$$R_{1y} + R_{2y} - 96 \text{ kN} = 0 \quad - \quad \Sigma \mathcal{F}_y = 0$$

$$(R_{2y} \times 12) - (96 \times 8) = 0 \quad \Sigma \mathcal{M} = 0$$

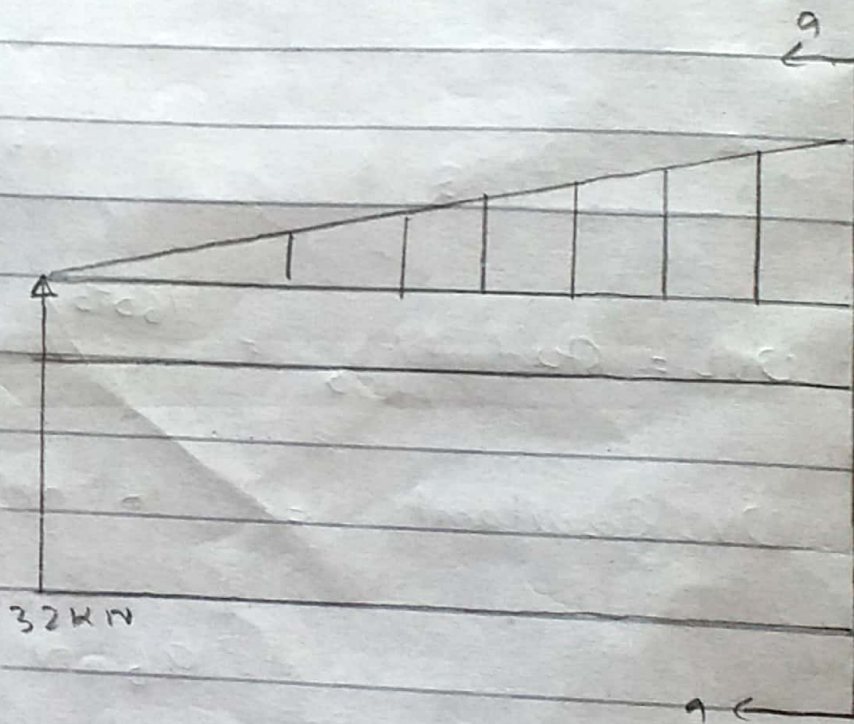
$$R_{2y} = \frac{96 \times 8}{12} = 64 \text{ kN}$$

$$R_{1y} + R_{2y} = 96 \text{ kN}$$

$$R_{1y} = 96 - R_{2y}$$

$$R_{1y} = 96 - 64 = 32 \text{ kN}$$

$$\left\{ R_{1x} = 0 \quad R_{1y} = 32 \text{ kN} \quad R_{2y} = 96 \text{ kN} \right\}$$



from law of similar  
triangle

$$\frac{16 \text{ kN/m}}{12 \text{ m}} = \frac{w \cdot \text{kN/m}}{x \cdot \text{m}}$$

$$w = \left[ \frac{16 \text{ kN}}{12} \right] \text{ kN/m}$$



Summation  $F_y = 0$

$$- V_{aa} - P_1 + 32 \text{ kN}$$

$$- V_{aa} - \frac{16n^2}{24} + 32$$

$$V_{aa} = \frac{32 - 16n^2}{24} \quad \text{--- Eq ①}$$

$$\text{at } x = 0 \quad \text{Eq ①} = 32.$$

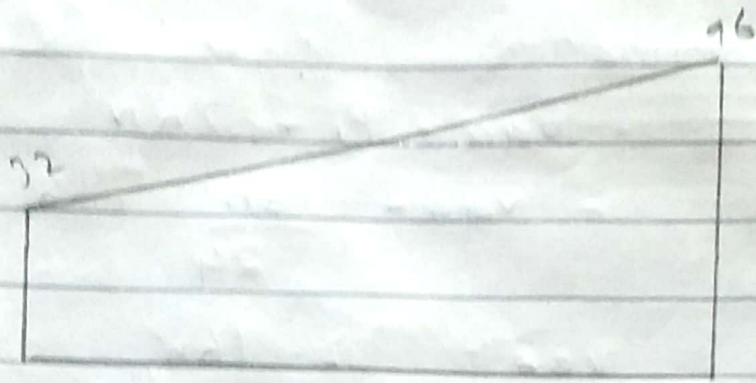
$$\text{At } x = 12 \quad \text{Eq ①} = 96.$$

the point at which  
shear force are negative

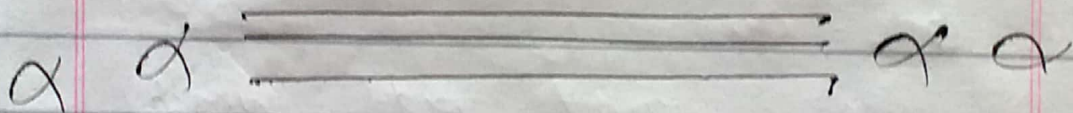
$$0 = \frac{16n^2}{24} + 32 = \frac{16n^2}{24} = 32.$$

$$\sqrt{n^2} = \sqrt{\frac{32 \times 24}{16}} \quad n = \sqrt{48}$$

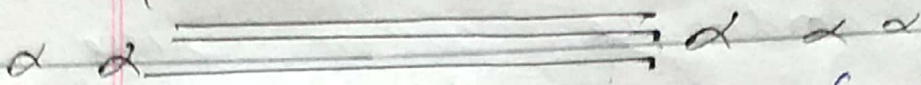
$$n = 6.92$$



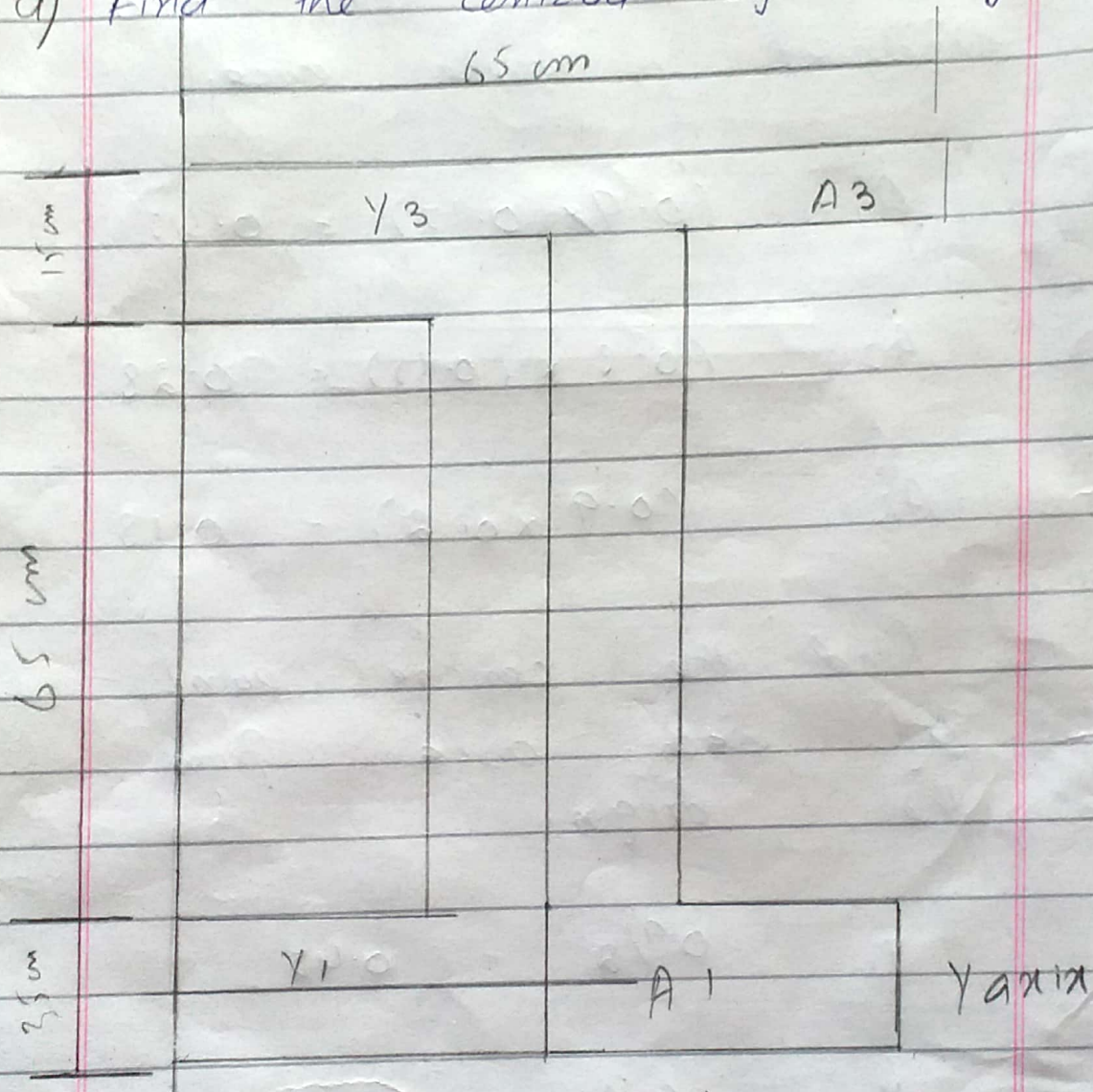
Hence the shear force  
is positive.



⇒ {Answers :- 04}



a) Find the centroid of the given?



35 cm

25 cm

First we have to established the coordinate system. Divide the composite area into different simple area.

$$A_1 = (0.9 \times 0.35) = 0.315$$

$$A_2 = (0.8 \times 0.35) = 0.28$$

$$A_3 = (0.9 \times 0.2) = 0.18$$

Find the centre point of each area from the origin.

$$y_1 = 0.9/2 = 0.45$$

$$y_2 = 0.9/2 = 0.45$$

$$y_3 = 0.9/3 = 0.45$$

$$z_1 = 0.35/2 = 0.175$$

$$z_2 = 0.35 + (0.65/2) = 0.675$$

$$23 = 0.35 + 0.65 + (0.15/0) = 1.075$$

$$Y_c = \frac{A_1 y_1 + A_2 y_2 + A_3 y_3}{A_1 + A_2 + A_3}$$

$$Y_c = \frac{(0.315 \times 0.45) + (0.28 \times 0.45) + (0.18 \times 0.45)}{0.315 + 0.28 + 0.18}$$

$$Y_c = \frac{0.14175 + 0.126 + 0.081}{0.775}$$

$$Y_c = 0.34875 / 0.775$$

$$Y_c = 0.45 \text{ m}$$

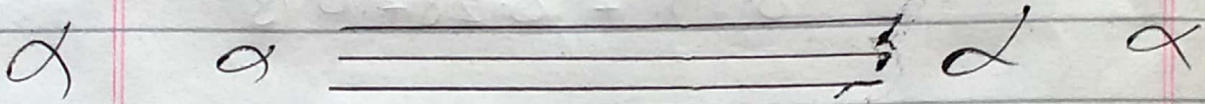
$$Z_c = \frac{A_1 z_1 + A_2 z_2 + A_3 z_3}{A_1 + A_2 + A_3}$$

$$Z_c = \frac{(0.315 \times 0.175) + (0.28 \times 0.675) + (0.18 \times 1.675)}{0.315 + 0.28 + 0.18}$$

$$Z_c = 0.055125 + 0.189 + 0.1935$$

$$0.775$$

$$Z_c = 0.56m$$



⇒ Answer: 0.5:

⇒ Work:

The application of a force through certain distance is known as work.

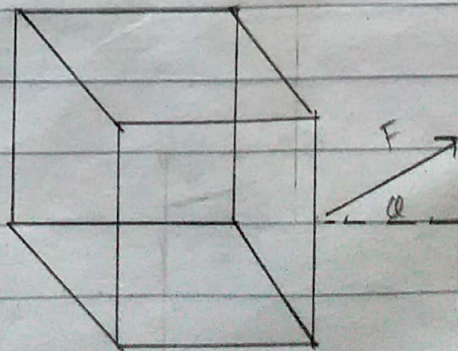
It can be measured in Joules (J).

• Mathematically form:

$$W = F \cdot d$$

⇒ Work done by a force at an angle  $\theta$ :

The same box is now dragged by a rope, which is raised at an angle  $\theta$  to the horizontal.

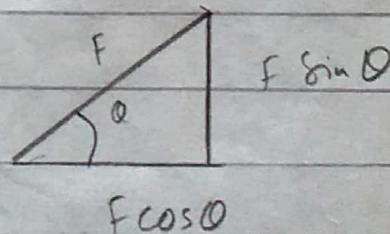


This time, the box moves in a different direction to the direction of the applied force. How does this affect the work done? Can you think any suggestions?

⇒ Calculating work done at an angle  $\theta$ :-

When calculating the work done by a force acting at an angle, it is useful to break the force into components.

The tension in the rope can be broken down into a horizontal and a vertical component.





So to calculate work done by a force at an angle:  
work done = Force in direction of movement  $\times$  distance covered  
 $W = F \cos \theta$ .

$\Rightarrow$  Example :- 01:

A box is pushed across a floor by a constant force of 100 N. What is the work done by the force to move the box 5 m?

Sol:

$$F = 100 \text{ N}$$

$$S = 5 \text{ m}$$

Required

$$W = ?$$

as we know that

$$W = FS$$

$$W = 100 \times 5$$

$$W = 500 \text{ J.}$$

$\Rightarrow$  Example :- 02:

A toy car is pulled along by a piece of

string is at  $30^\circ$  to the horizontal. Calculate the work done in pulling the toy if the tension in the string is  $10\text{N}$  and it is pulled along  $5\text{m}$ .

Sol:  $F = 10\text{N}$   
 $S = 5\text{m}$   
 $\theta = 30^\circ$

Req:

$$W = ?$$

$$W = Fs \cos \theta$$

$$W = 10\text{N} \times 5\text{m} \times \cos 30^\circ$$

$$\{W = 43.3\text{J}\}$$

⇒ Energy:

Energy is the measures of the ability of an object or a system to perform work.

The Unit of Energy is Joule.

It is denoted by  $J$ .

⇒ Types of Energy: These are many types of energy:

- Kinetic energy: Energy of an object due to its speed.
- Gravitational Potential energy: Energy of an object due to position in a gravitational field.
- Elastic Potential Energy: Energy stored when an object is stretched or compressed.
- Chemical energy: Energy stored in a chemical bonds.
- Nuclear Energy: Energy stored in nuclei.

- Heat Energy: Hot things have more energy than their cold counterparts.

⇒ Energy Transfer:

When work is

done, energy is transferred. That energy might be:

- Gravitational Potential energy: When an object changes height within a gravitational field.

- Kinetic energy: when an object changes speed.

- Light energy: when a light bulb is switched on.

- Heat and sound: when a

brakes sharply.

⇒ Conservation of Energy:

Energy can't be created, or destroyed but it can only be changed from one form to another form.

⇒ Power:

Power is the rate at which work is done, or the rate at which energy is transferred.

⇒ Mathematically:

$$P = W/t$$

Power is measured in watts. The work done or energy is transferred is measured in Joules. While the time is measured in seconds. (s).

⇒ Example:

A crane lifts a load of 1500kg to a height of 25m at a steady rate in a time of 2 min. What is the power of the crane.

Sol:

$$P = \frac{W}{t}$$

$$P = \frac{367875}{120}$$

$$P = 3066 \text{ W}$$

$$\therefore W = \text{energy} = \Delta E_p$$

$$\Delta E_p = mgh$$
$$= 1500 \times 9.8 \times 25$$

$$= 367875 \text{ J}$$

The End