

Given that

Factor of Safety = 2

$$E = 10.3 \times 10^6 \text{ psi}$$

$$\text{length} = 6 \text{ ft}$$

$$b = 3/4 \text{ inch}, \quad h = 2 \text{ inch}$$

Condition

→ one end hinged & one end fixed

Required:

$$\frac{\pi^2 ET}{L_e^2}$$

$$\frac{\pi^2 EA r^2}{L_e^2} \quad \therefore I = Ar^2$$

Now  $\delta = \sqrt{\frac{I}{A}}$

$$\delta = \sqrt{\frac{hb^3}{12bh}}$$

$$= \sqrt{\frac{b^2}{12}}$$

$$\Rightarrow \frac{b}{2\sqrt{3}}$$

$$\Rightarrow \frac{3/4}{2\sqrt{3}}$$

$$\delta = 0.216 \text{ in}$$

To find crippling load,

$$P_{cr} = \frac{\pi^2 EA}{(L_{eff})^2}$$

$$= \frac{(314)^2 (10.3 \times 10^6) (1.5 \text{ in}^2)}{(0.7 L)^2}$$

$$= \frac{(9.8596) \times 15.45 \times 10^6}{\left(\frac{0.7 \times 72}{0.216}\right)^2}$$

$$= \frac{152.33}{54444.4}$$

$$P_{cr} = 2.7979 \times 10^3 \text{ PSI}$$

$$P_{cr} = 2.7979 \text{ KSI}$$

for  $P_{safe}$

$$P_{safe} = \frac{P_{cr}}{\text{Factor of Safety}}$$

$$P_{safe} = \frac{2.7979}{2}$$

$$= 1.3988 \text{ KSI}$$

Q No 2:

Given data

$$L = 310 \text{ mm} \times 45 \text{ mm}$$

$$E = 200 \times 10^9 \text{ Pa}$$

$$GP = 240 \times 10^6 \text{ Pa}$$

$$C = 12 \text{ m}$$

Factor of Safety = 2.5

Required:

$$L_{\text{mm}} = ?$$

$$P_{\text{safe}} = ?$$

Solution:

As we know that

$$GP = \frac{F L^2}{(L_e/r)^2}$$

$$\frac{L_e}{r} = \sqrt{\frac{4 L^2}{E}}$$

$$\frac{L_e}{r} = \sqrt{\frac{(3.14)^2 \times (200 \times 10^3)}{240 \times 10^3}}$$

$$\boxed{\frac{L_e}{r} = 90.64}$$

Now

$$r = \sqrt{\frac{b^2}{12}}$$

$$r = \sqrt{\frac{(45)^2}{12}} \rightarrow r = 12.99 \text{ m}$$

Part B =

$$P_{cr} = \frac{\pi^2 EA r^2}{L^2}$$

$$P_{cr} = \frac{(3.14)^2 (200 \times 10^9) (1950) (12.99)^2}{(12 \times 1000)^2}$$

$$P_{cr} = 37.2343 \text{ kN}$$

For  $P_{safe}$

$\frac{P_{cr}}{\text{Factor of Safety}}$

$$P_{safe} = \frac{37.2343 \text{ kN}}{2.5}$$

$$P_s = 12.8937 \text{ kN}$$