

Day: MTWTF S

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Final term Paper  
(Summer)

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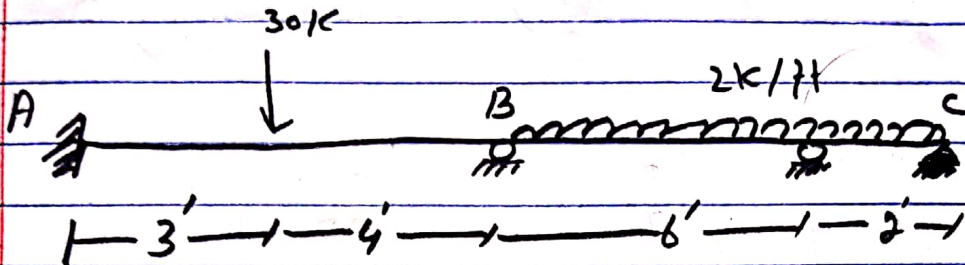
ID = 7768

Subject # Structure 2

Submitted to Engr- Adeed  
Khan

Date = 25 Sept 2020

Q No 01



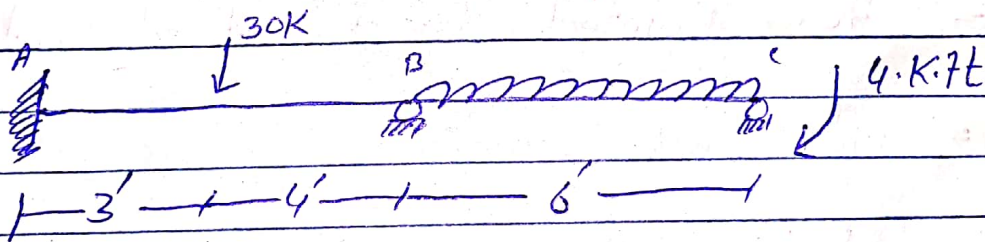
Sol

Step # 1

Determining Kinematic Indeterminacy

$$K-I = 5^{\circ}$$

So we have to reduce the extended portion



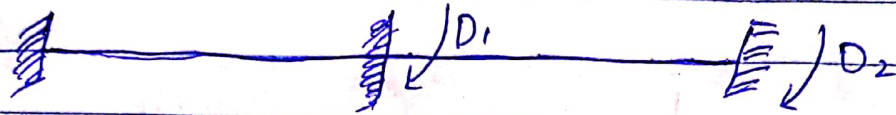
$$\Rightarrow \frac{2(8)}{1} \Rightarrow 4k \cdot ft$$

Now

$$K-I = 2^{\circ}$$

Step # 2

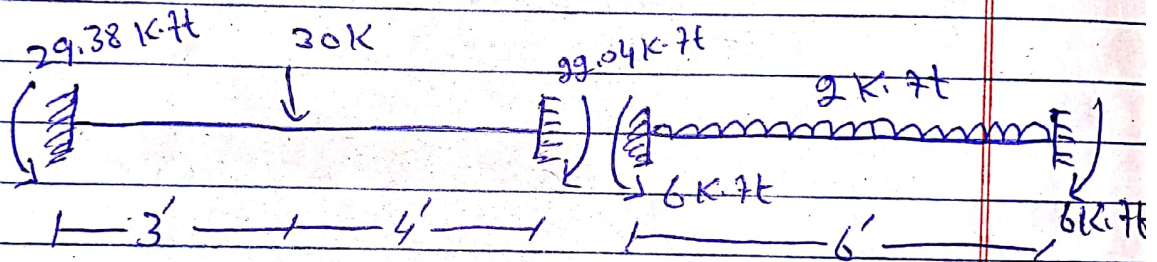
Determine unknown Joint Displacement



$$\begin{bmatrix} D_1 \\ D_2 \end{bmatrix} = \begin{bmatrix} ? \\ ? \end{bmatrix} \quad \begin{bmatrix} AD_1 \\ AD_2 \end{bmatrix} = \begin{bmatrix} 0 \\ 4 \end{bmatrix}$$

### Step # 3

Compute [ADL] matrix



⇒ For Pointed load (not at mid)

⇒ For left end:

$$\Rightarrow \frac{Pab^2}{L^2} = \frac{(30)(3)(4)^2}{7^2} = 29.38 \text{ K.ft}$$

⇒ For Right end:

$$\Rightarrow \frac{Pa^2b}{L^2} = \frac{(30)(3)^2(4)}{(7)^2} = 22.04 \text{ K.ft}$$

⇒ for UDL:

$$\frac{wL^2}{19} \Rightarrow \frac{(2)(6)^2}{12} = 6 \text{ K}\cdot\text{ft}$$

$$ADL_1 = +22.04 - 6 = 16.04 \text{ K}\cdot\text{ft}$$

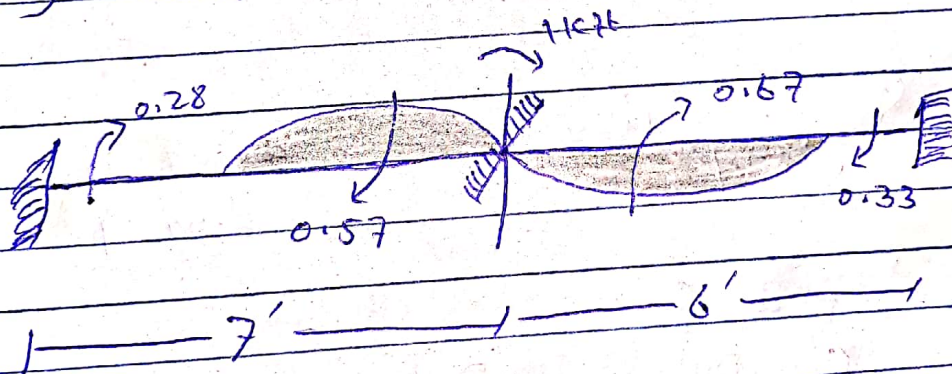
$$ADL_2 = 6 \text{ K}\cdot\text{ft}$$

### Step # 4

compute [S] matrix

$$S = \begin{bmatrix} S_{11} & S_{12} \\ S_{21} & S_{22} \end{bmatrix}$$

a)  $D_1 = 1K$        $D_2 = 0$



$$\Rightarrow \frac{4EI}{7} = 0.57 \quad , \quad \frac{2EI}{6} = 0.33$$

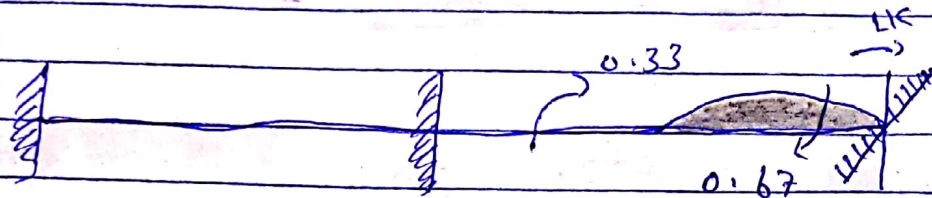
$$\Rightarrow \frac{4EI}{6} = 0.67 \quad , \quad \frac{2EI}{7} = 0.28$$

$$S_{11} = 0.57 + 0.67$$

$$S_{11} = 1.24 \text{ EA}$$

$$S_{21} = 0.33 \text{ EA}$$

(b)  $D_1 = 0$        $D_2 = 1K$



$$\frac{4EI}{6} = 0.67$$

$$\frac{2EI}{6} = 0.33$$

$$S_{12} = 0.33$$

$$S_{22} = 0.67$$

$$S = \begin{bmatrix} 1.24 & 0.33 \\ 0.33 & 0.67 \end{bmatrix}$$

Step # 5

compute  $[D]$  matrix

$$\begin{bmatrix} D_1 \\ D_2 \end{bmatrix} = \begin{bmatrix} S_{11} & S_{12} \\ S_{21} & S_{22} \end{bmatrix}^{-1} \times \begin{bmatrix} AL_1 \\ AL_2 \end{bmatrix} - \begin{bmatrix} PL_1 \\ PL_2 \end{bmatrix}$$

$$= \frac{1}{\begin{vmatrix} 1.24 & 0.33 \\ -0.33 & 0.67 \end{vmatrix}} \times \text{Adj } A \times \begin{bmatrix} 0 \\ 4 \end{bmatrix} - \begin{bmatrix} 16.04 \\ 6 \end{bmatrix}$$

$$[S] = (1.24 \times 0.67) - (0.33 \times 0.33)$$

$$= 0.8308 - 0.1089$$

$$[S] = 0.7219$$

$$\text{Adj } A = \begin{bmatrix} 0.67 & -0.33 \\ -0.33 & 1.24 \end{bmatrix}$$

Now

$$\begin{bmatrix} AD_1 - ADL_1 \\ AD_2 - ADL_2 \end{bmatrix} = \begin{bmatrix} 0 - 16.04 \\ 4 - 6 \end{bmatrix} = \begin{bmatrix} -16.04 \\ -2 \end{bmatrix} EI$$

$$\begin{bmatrix} D_1 \\ D_2 \end{bmatrix} = \frac{\begin{bmatrix} 0.67 & -0.33 \\ -0.33 & 1.24 \end{bmatrix} \times \begin{bmatrix} -16.04 \\ -2 \end{bmatrix}}{0.7219} \frac{1}{EI}$$

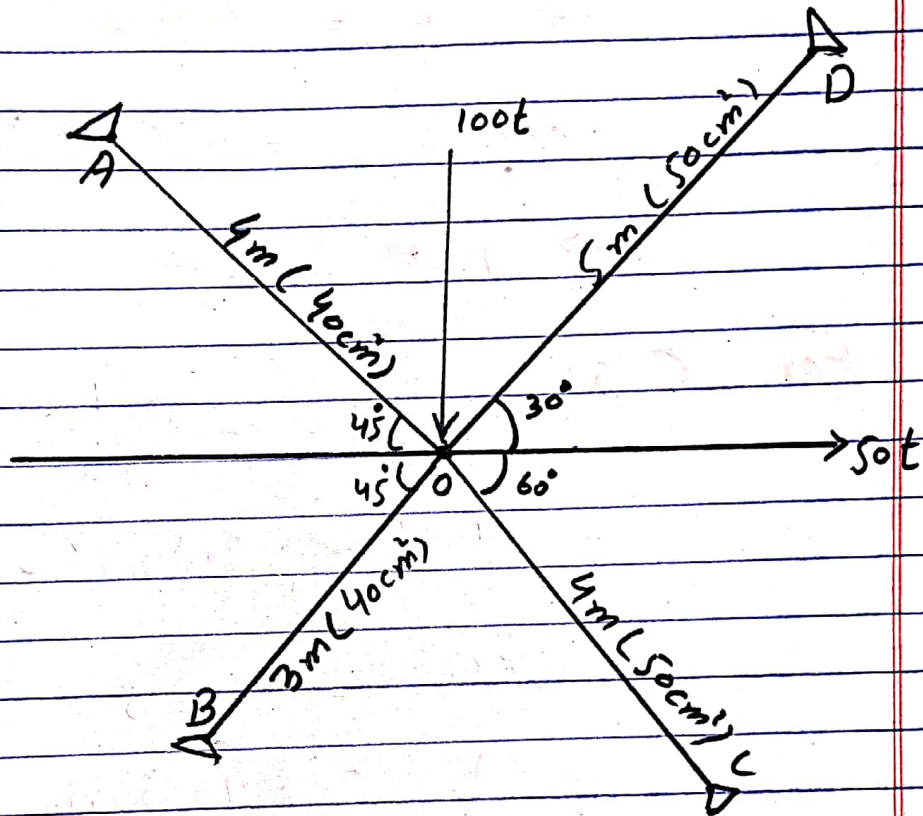
$$\begin{bmatrix} D_1 \\ D_2 \end{bmatrix} = \begin{bmatrix} -13.97 \\ 3.8902 \end{bmatrix} \times EI$$



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Q No 02



$$E = 2000 \text{ t/cm}^2$$

Sol

For A

$$\sin 45^\circ = \frac{P}{h} = \frac{P}{4}$$

$$\Rightarrow P = 2.828 \text{ m}$$

$$\cos 45^\circ = \frac{b}{4}$$

$$\Rightarrow b = 2.828 \text{ m}$$

$$\underline{\text{For B}} \quad \therefore \sin 45^\circ = \frac{p}{3}$$

$$\Rightarrow p = 2.12 \text{ m}$$

$$\cos 45^\circ = \frac{b}{h} \Rightarrow \frac{b}{3}$$

$$\Rightarrow b = 2.12 \text{ m}$$

$$\text{For C} \quad \therefore \sin 30^\circ = \frac{p}{h} = \frac{p}{5}$$

$$\Rightarrow p = 2.5 \text{ m}$$

$$\cos 30^\circ = \frac{b}{5}$$

$$\Rightarrow b = 4.33 \text{ m}$$

Now

$$EA(A) = 2000 \times 40 = 80,000 \text{ t}$$

$$EA(B) = 2000 \times 40 = 80,000 \text{ t}$$

$$EA(C) = 2000 \times 50 = 100,000 \text{ t}$$

$$EA(D) = 2000 \times 50 = 100,000 \text{ t}$$

Step # of

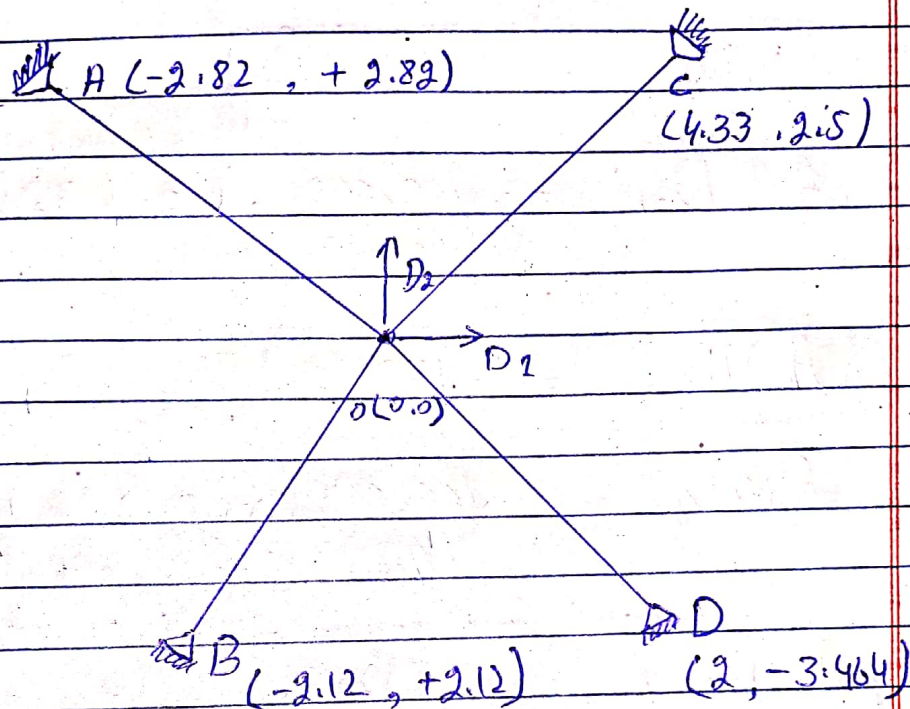
$$\begin{aligned} K \cdot I &= 2j - 8 \\ &= 2(5) - 8 \end{aligned}$$

$$K \cdot I = 2^\circ$$



Step # 02

Select unknown  
joint displacement



$$\begin{bmatrix} D_1 \\ D_2 \end{bmatrix} = \begin{bmatrix} ? \\ ? \end{bmatrix}, \quad \begin{bmatrix} AD_1 \\ AD_2 \end{bmatrix} = \begin{bmatrix} 50 \\ -100 \end{bmatrix}$$

Step # 03

$$[AMD]_{4 \times 2} \in [S]_{2 \times 2}$$

$$i) D_1 = 1 \quad D_2 = 0$$

$$AMD = \frac{EA}{L^2} (x_k - x_j)$$

$$AMD_{11} = \frac{80,000}{(400)^2} \times (0 + 2.82)$$

$$= \boxed{141}$$

$$AMD_{21} = \frac{80,000}{(300)^2} \times (0 + 212)$$

$$AMD_{21} = 188.44$$

$$AMD_{31} = \frac{100,000}{(500)^2} \times (0 - 433)$$

$$AMD_{31} = -173.2$$

$$AMD_{41} = \frac{100,000}{(400)^2} \times (0 - 200)$$

$$AMD_{41} = -125$$

$$\text{Now } S_{11} = \sum_x \frac{EA}{L^3} (x_k - x_j)^2$$

$$S_{11} = \frac{80,000}{400^3} (282)^2 + \frac{80,000}{(300)^3} (212)^2$$

$$+ \frac{100,000}{(500)^3} \times (-433)^2 + \frac{100,000}{(400)^3} \times (-200)^2$$

$$S_{11} = 99.405 + 133.107 + 149.991$$

$$+ 82.5$$

$$S_{11} = 445.063$$

$$S_{12} = S_{21} = \sum_{i=1}^m \frac{\epsilon A}{L^3} \times (X_k - X_j)(Y_k - Y_j)$$

$$S_{12} = \frac{80,000}{(400)^3} \times (282)(-282) + \frac{80,000}{(300)^3} (212)(212)$$

$$+ \frac{100,000}{(500)^3} \times (-250)(-250) + \frac{100,000}{(400)^3} (-200)(346)$$

$$S_{12} = S_{21} = 12,237$$

$$(ii) D_1 = 0 \quad D_1 = 1K'$$

$$AMD = \frac{\epsilon A}{L^2} (Y_k - Y_j)$$

$$AMD_{12} = \frac{80,000}{400^2} (-282) = -141$$

$$AMD_{22} = \frac{80,000}{300^2} (212) = 188.44$$

$$AMD_{33} = \frac{100,000}{500^2} (-250) = -100$$

$$AMD_{42} = \frac{100,000}{400^2} (346) = 216.25$$

$$\text{Now } S_{22} = \sum_{i=1}^m \frac{EA}{L^3} (Y_k - Y_j)^2$$

$$S_{22} = \frac{80,000}{400^3} (-282)^2 + \frac{80,000}{300^3} (212)^2$$

$$+ \frac{100,000}{500^3} (-250)^2 + \frac{100,000}{400^3} (346)^2$$

$$S_{22} = 469.628$$

Step # 04

$$[D] = [S]^{-1} \times [AD]$$

$$\begin{bmatrix} D_1 \\ D_2 \end{bmatrix} = \begin{bmatrix} 445.083 & 12.237 \\ 12.237 & 469.628 \end{bmatrix}^{-1} \times \begin{bmatrix} 50 \\ -100 \end{bmatrix}$$

$$\begin{bmatrix} D_1 \\ D_2 \end{bmatrix} = \begin{bmatrix} 0.1183 \\ -0.216 \end{bmatrix}$$

Step # 5

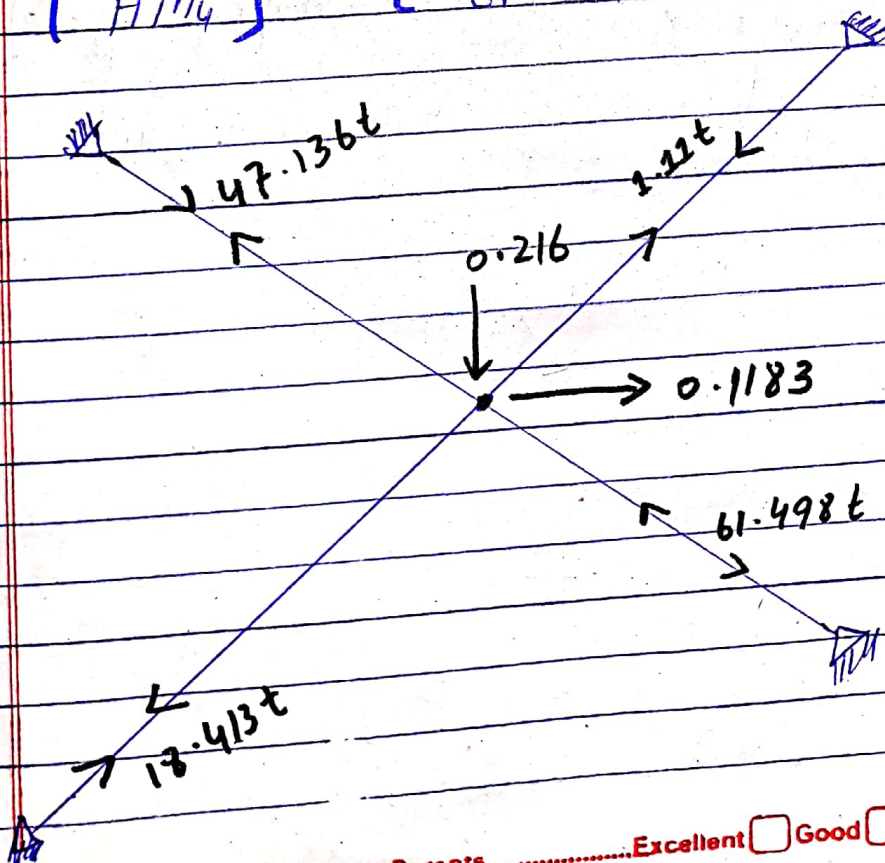
[AM]

$$\begin{bmatrix} AM_1 \\ AM_2 \\ AM_3 \\ AM_4 \end{bmatrix} = \begin{bmatrix} 141 & -141 \\ 188.44 & 188.44 \\ -173.2 & -100 \\ -125 & 216.25 \end{bmatrix} \times \begin{bmatrix} 0.1183 \\ -0.216 \end{bmatrix}$$

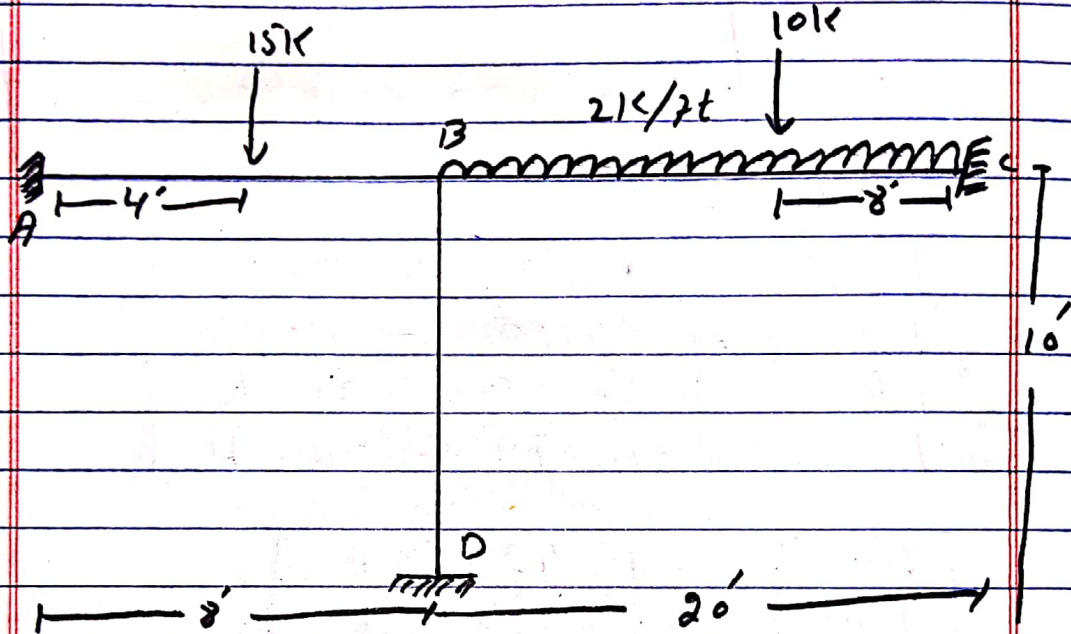
$$= \begin{bmatrix} 141 \times 0.1183 + (-141) \times (-0.216) \\ 188.44 \times 0.1183 + 188.44 \times (-0.216) \\ -173.2 \times 0.1183 + (-100) \times (-0.216) \\ -125 \times 0.1183 + 216.25 \times (-0.216) \end{bmatrix}$$

$$\begin{bmatrix} AM_1 \\ AM_2 \\ AM_3 \\ AM_4 \end{bmatrix} = \begin{bmatrix} 16.68 & + & 30.46 \\ 22.29 & - & 40.70 \\ -20.49 & + & 21.16 \\ -14.79 & - & 46.71 \end{bmatrix}$$

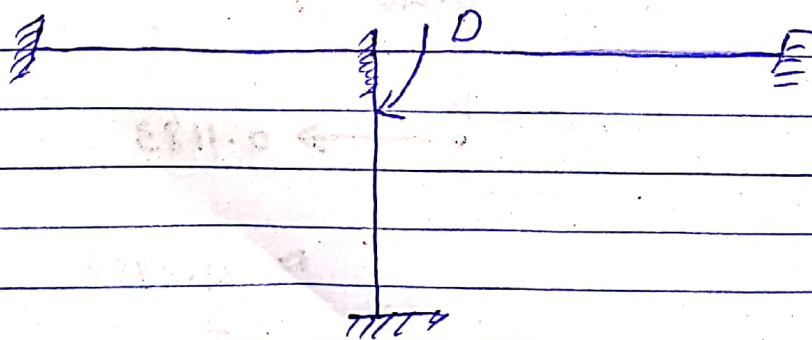
$$\begin{bmatrix} AM_1 \\ AM_2 \\ AM_3 \\ AM_4 \end{bmatrix} = \begin{bmatrix} 47.136t \\ -18.413t \\ 1.11t \\ -61.498t \end{bmatrix}$$



Q No 03



Sol Step # 1 : Determine Kinematic Indeterminacy  
Step # 02  $K.I = 1$   
 Determine unknown joint Displacement.



$$[D] = [P]$$

$$[AD] = [0]$$



For Left End:

$$\frac{Pab^2}{L^2} \Rightarrow \frac{(10)(12)(8)^2}{(20)^2} = 19.2 \text{ K}\cdot\text{ft}$$

For Right End:

$$\frac{Pa^2b}{L^2} \Rightarrow \frac{(10)(12)(8)^2}{(20)^2} \Rightarrow 28.8 \text{ K}\cdot\text{ft}$$

So Total moment at left end:

$$19.2 + 66.67 = 85.87 \text{ K}\cdot\text{ft}$$

Similarly at right End:

$$28.8 + 66.67 = 95.47 \text{ K}\cdot\text{ft}$$

$$\text{So } [ADL] = -85.87 + 15 = -70.87 \text{ K}\cdot\text{ft}$$

Step #4

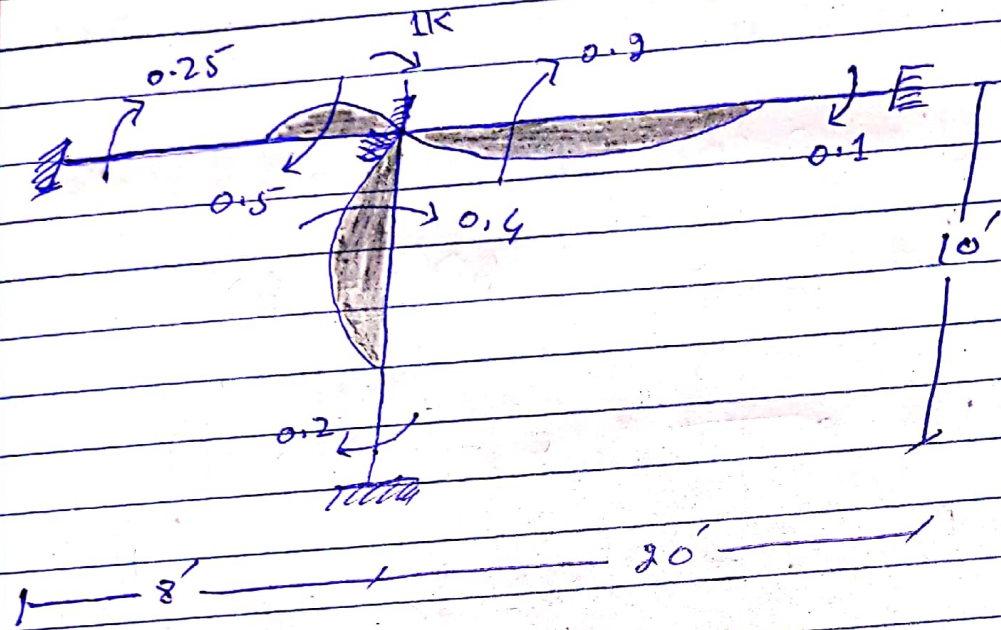
Determine  $[S]$  matrix

$$[S] = [S_{ij}]$$

Now

$$D = 1 \text{ K}$$





$$\Rightarrow \frac{4EI}{8} = 0.5, \quad \frac{2EI}{8} = 0.25$$

$$\Rightarrow \frac{4EI}{20} = 0.9, \quad \frac{2EI}{20} = 0.1$$

$$\Rightarrow \frac{4EI}{10} = 0.4, \quad \frac{2EI}{10} = 0.2$$

$$[S] = (0.5 + 0.4 + 0.2) EI$$

$$= 1.1 EI$$

$$[S] = 1.1 EI$$

## Step #5

Compute  $[D]$  matrix

$$[D] = [S]^{-1} \times [AD] - [ADL]$$

$$[D] = \frac{1}{1.1} \times [0] - [-70.87]$$

$$[D] = \frac{70.87}{1.1}$$

$$[D] = [64.42] \frac{1}{EI}$$