

Probability and Statistics:

Q No 1.

Ans:

Class interior	Freq	class Boundaries	cf <	cf >
0-4	25	0-4.5	25	2092
5-9	45	4.5-9.5	70	2067
10-14	81	9.5-14.5	151	2022
15-19	143	14.5-19.5	294	1941
20-24	280	19.5-24.5	574	1798
25-29	349	24.5-29.5	923	1518
30-34	374	29.5-34.5	1297	1169
35-39	395	34.5-39.5	1692	775
40-44	400	39.5-44.5	2092	400

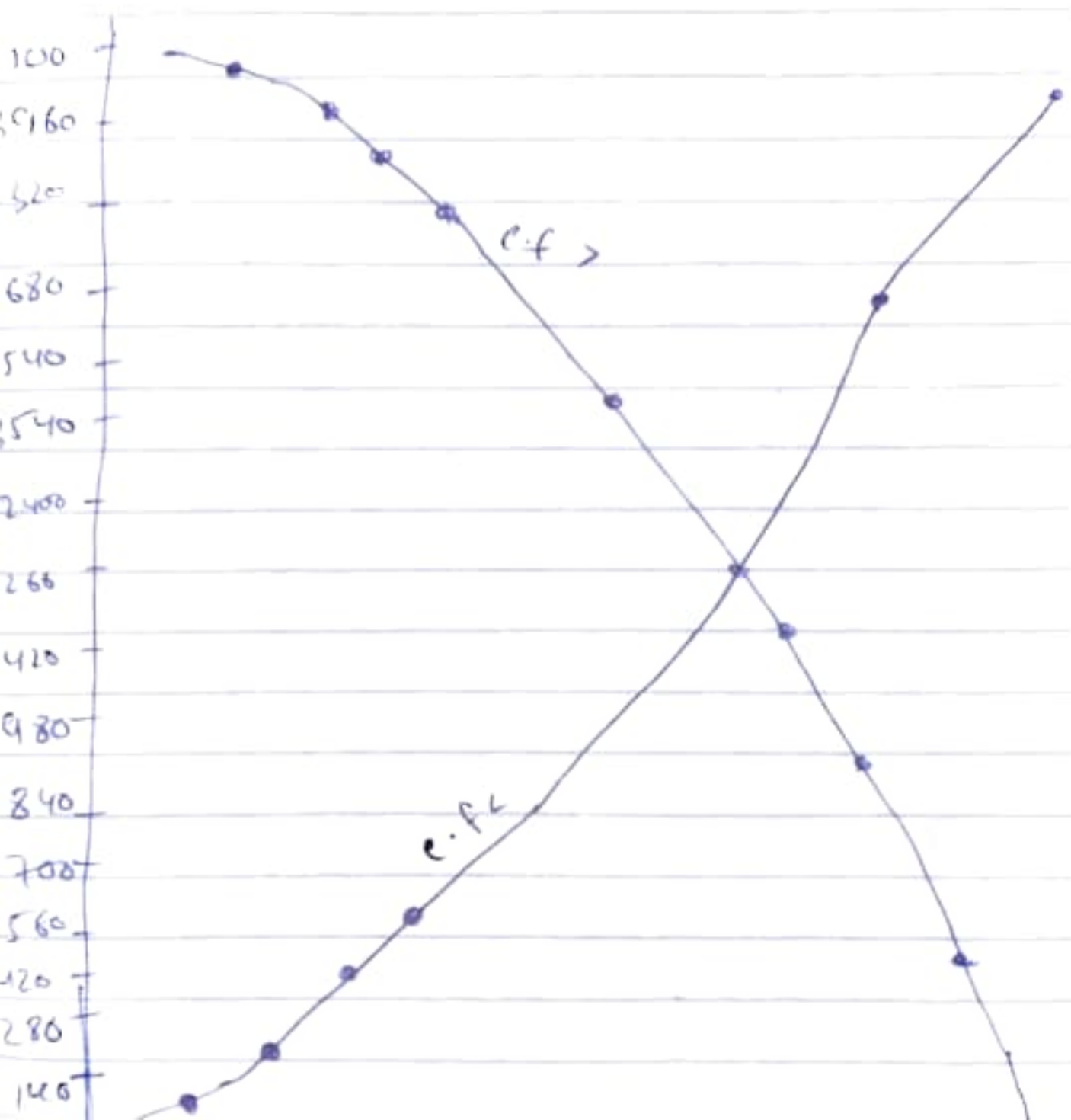
e.B = Δ = Lcl of 2nd class - Ucl of 1st class

$$e.B = 5 - 4$$

$$e.B = 1$$

$$e.B = \Delta/2 = 1/2$$

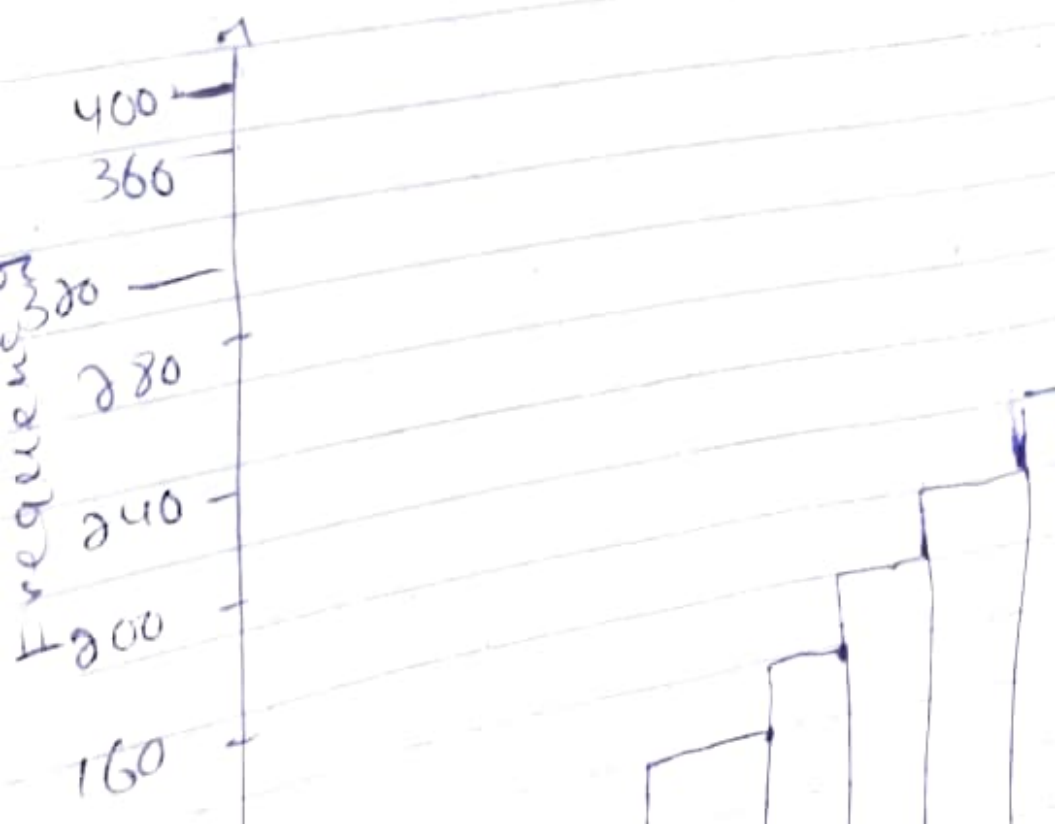
$$e.B = 0.5$$



NO 1:

Ans (b)

Class Interval	freq
0-4	25
5-9	45
10-14	81
15-19	143
20-24	280
25-29	349
30-34	374
35-39	395
40-44	400



No.:

Group Distribution Table:

Step 1

Count the number of observations

$N = 30$

Step 2

Largest value; $x_n = 431$

Smallest value $x_0 = 363$

Step 3

Range; $R = x_n - x_0$

$$= 431 - 363$$

$$= 68$$

Step 4

$$k = 1 + 3.33 \log N$$

$$k = 1 + 3.33 \log (30)$$

$$k = 1 + 3.33 (1.477)$$

$$k = 5.92$$

$$k = 6 \text{ (rounding off)}$$

Step 5

$$h = R/k$$

$$h = 68/6$$

$$h = 11.33$$

$$h = 12 \text{ (by rounding)}$$

(5)

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Classes	Frequency
363 - 374	4
375 - 386	4
387 - 398	8
399 - 410	7
411 - 422	4
423 - 434	3

By Tally column.

Classes	Class Boundaries	Class Mark	(F)	c.f	Tally
363 - 374	361.5 - 374.5	368.5	4	4	
375 - 386	374.5 - 386.5	380.5	4	8	
387 - 398	386.5 - 398.5	392.5	8	16	
399 - 410	398.5 - 410.5	404.5	7	23	
411 - 422	410.5 - 422.5	416.5	4	27	
423 - 434	422.5 - 434.5	428.5	3	30	

Mean

$$\begin{aligned} \bar{x} = & \frac{423 + 369 + 387 + 411 + 393 + 394 + 371 + 377 + 389 + 409 + 392 + 408 + 431 + 407 + 363 + 391 + 405 + 384 + 400 + 381 + 399 + 411 + 428 + 422 + 396 + 372 + 410 + 419 + 386 + 390}{30} \end{aligned}$$

$$\bar{x} = \frac{11914}{30}$$

= 397

Mode:

$$\text{Mode} = l + \frac{f_m - f_1}{(f_m - f_1) + (f_m - f_2)} \times h$$

Here $l = 387$, $f_m = 8$, $f_1 = 4$
 $f_2 = 7$, $h = 12$.

So

$$\text{Mode} = 387 + \frac{8-4}{(8-4)+(8-7)} \times 12$$

$$\text{Mode} = 387 + \frac{4}{4+1} \times 12$$

$$\text{Mode} = 387 + \frac{4}{5} \times 12$$

$$\text{Mode} = 387 + 48$$

$$\text{Mode} = 396.6$$

$$\text{Mode} = 397$$

Quartile

$$Q_1 = \frac{n}{4} = \frac{30}{4}$$

$$Q_1 = 7.5$$

which corresponds to value in class 375-386. Therefore,

$$Q_1 = l + \frac{n}{f} \left(\frac{n}{4} - c \right)$$

$$Q_1 = 375 + \frac{12}{4} (7.5 - 4) \because c = 4$$

$$Q_1 = 375 + 3(3.5)$$

$$Q_1 = 375 + 10.5$$

$$Q_1 = 385.5$$

$$Q_1 = 386$$

Now

$$Q_3 = \frac{34}{4} = \frac{3+30}{4}$$

$$Q_3 = \frac{90}{4} = 22.5$$

which corresponds to value in which class 399-410. Therefore

$$Q_3 = l + \frac{h}{f} \left(\frac{34}{4} - c \right)$$

$$Q_3 = 399 + \frac{12}{7} (22.5 - 16) \because c = 16$$

$$Q_3 = 399 + \frac{12}{7} (6.5)$$

$$Q_3 = 399 + \frac{78}{7}$$

$$Q_3 = 399 + 11$$

$$Q_3 = 410$$

Q 4:-

Ans:-

class	f_i	n	n^2	$f_i n$	$f_i n^2$
64-84	15	74	5476	1110	82140
85-104	18	945	8930.25	1701	160744.5
105-124	27	1145	13110.25	3091.5	353976.75
125-144	10	1345	18090.25	1345	180902.5
145-164	6	1545	2387.25	927	143221.5
165-184	5	1745	30450.25	87.5	152251.25
185-204	13	1945	3790.25	2528.5	491793.25
	$\Sigma = 94$			$\Sigma = 11575.5$	$\Sigma = 1565029.75$

Variance

$$s^2 = \frac{\Sigma f_i n^2}{n} - \left(\frac{\Sigma f_i n}{n} \right)^2$$

$$s^2 = \frac{1565029.75}{94} - \left(\frac{11575.5}{94} \right)^2$$

$$s^2 = 16649.26 - 15164.35$$

$$s^2 = 1484.9$$

$$s^2 = 1485$$

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Standard Deviation

Taking square root of eq (1) we have $\sqrt{s^2} = \sqrt{1485}$

$$s = 38.5$$

Q3

Ans: First Data:-

3, 6, 2, 1, 7, 5

mean = $\frac{3+6+2+1+7+5}{6}$

$$\text{Mean} = \frac{24}{6} = 4$$

x	x^2	
3	9	S. Deviation $\sqrt{\frac{\sum x^2}{N} - \left(\frac{\sum x}{N}\right)^2}$
6	36	
2	4	
1	1	
7	49	
5	25	
$\sum x = 24$	$\sum x^2 = 124$	S. D = $\sqrt{\frac{124}{6} - \frac{576}{36}}$

$$S.D = \sqrt{47}$$

$$S.D = 2.2$$

Second Data:

11, 17, 9, 7, 19, 15

$$\text{Mean} = \frac{11+17+9+7+19+15}{6}$$

$$\text{Mean} = \frac{78}{6} = \boxed{13}$$

$$\text{S. Deviation} = \sqrt{\frac{\sum x^2}{N} - \left(\frac{\sum x}{N}\right)^2}$$

x	x^2	
11	121	$\text{S.D} = \sqrt{\frac{1126}{6} - \frac{6084}{36}}$
17	289	
9	81	$\text{S.D} = \sqrt{\frac{6756}{36} - \frac{6084}{36}}$
7	49	
19	361	$\text{S.D} = \sqrt{\frac{672}{36}}$
15	225	
$\Sigma: 78$	$\Sigma = 1126$	$\text{S.D} = \sqrt{18.7}$

1st data mean = 4

1st data S.D = 2.2

2nd data mean = 13

2nd data S.D = 4.3

The required relation is that
→ Mean of 2nd data is greater than mean of 1st data and standard deviation of 2nd data is double the standard deviation of 1st data.

Q 5-

Ans Comment:-

NO, it is not obviously that all the people have height 5 feet can easily cross it if he did not know swimming and river 8 feet at some points so, he will cross it.

Ans (B):-

Comment:-

NO, it does not mean every student is hopeless. Those students whose marks are less than 30, some have 30 marks.

and some students have greater than 30 marks. There can be a few students whose marks may be 60 or more.

Ans (e) -

No, it is not true, that all the household servants must be paid. Average pay does not mean everyone get paid same. The king's income will be much more than servants.

End