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Subject # PRCD

Section # A

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(1)
Ans

Given data :-

$$\begin{aligned} \text{Height} &= 20'' \\ \text{Dead load D.L} &= \frac{1005}{247} \text{ kips/ft} \\ \text{Width (b)} &= 10'' \\ \text{Span} &= 18' \\ \text{Live load} &= \text{L.L. } 8.47 \text{ kips/ft} \\ f'_c &= 4000 \text{ psi} = 4 \text{ ksi} \\ f_y &= 60,000 \text{ psi} = 60 \text{ ksi} \end{aligned}$$

Solution :-

As we know that

Step # 1

$$\begin{aligned} \text{Effective depth } d &= h - 3 \\ &= 20 - 3 = 17'' \end{aligned}$$

$$\text{Effective cover } d = 2.5''$$

Reinforcement Ratio.

$$\rho_{\max} = 0.85 \times \beta \times \frac{f'_c}{f_y} \times \left(\frac{\epsilon_u}{\epsilon_u + \epsilon_y} \right)$$

$$= 0.85 \times 0.85 \times \frac{4}{60} \times \left(\frac{0.003}{0.003 + 0.005} \right)$$

$$\rho_{\max} = 0.0180$$

Step # 2

finding Area of steel

$$f_{max} = \frac{A_{st}}{b \times d}$$

$$f_{max} = \frac{A_{st}}{b \times d}$$

$$A_{st} = f_{max} \times b \times d$$

$$A_{st} = 0.0180 \times 10 \times 17$$

$$A_{st} = 3.06 \text{ in}^2$$

Step # 3

By formula of design moment

$$M_{u2} = \phi \times A_{st} \times f_y \times \left(d - \frac{a}{2}\right)$$

$$a = \frac{A_{st} \times f_y}{0.85 \times f_c' \times b}$$

$$a = \frac{3.06 \times 60}{0.85 \times 4 \times 10}$$

$$a = 5.4''$$

$$M_{u2} = 0.90 \times 3.06 \times 60 \times \left(17 - \frac{5.4}{2}\right)$$

$$M_{u2} = 2362.93 \text{ kip inch}$$

Page #3

Moment due to loads

$$\text{Beam self weight} = \frac{10}{12} \times \frac{20}{12} \times 150$$

$$= 208.33 \text{ lb/ft}$$

$$\text{total factor load} = 1.2(1050 + 208.33) + 1.6(2470)$$

$$= 5461.99 \text{ lb/ft}$$

$$= 5.46 \text{ kips/ft}$$

$$\text{ultimate factored moment} = \frac{wL^2}{8}$$

$$M_U = \frac{5.46 \times (18)^2}{8} \times 12$$

$$M_U = 2653.56$$

Now as

$$M_{U2} < M_U$$

$$2362.92 < 2653.56$$

Doubly Reinforcement Required.

Step #4

$$M_{U1} = M_U - M_{U2}$$

$$M_{U1} = 2653.56 - 2362.92$$

$$M_{U1} = 290.64 \text{ kip/ftch}$$

Step # 5

Steel area in compression zone will be

$$M_{U1} = \phi \times A_{st}' \times f_y \times (d - d')$$

$$A_{st}' = \frac{M_{U1}}{\phi' \times f_y \times (d - d')}$$

$$A_{st}' = \frac{290.64}{0.90 \times 60 \times (17 - 2.5)}$$

$$A_{st}' = 0.37 \text{ in}^2$$

Step # 6

$$A_s = A_{st} + A_{st}'$$

$$A_s = 3.06 + 0.37$$

$$A_s = 3.43 \text{ in}^2$$

Step # 7

we use #8 bar

$$\text{dia} = \frac{8}{8} = 1''$$

$$\text{Area} = \frac{\pi d^2}{4}$$

$$\text{Area} = 0.785 \text{ in}^2$$

No. of bars

$$\frac{A_{st}}{\text{Area of 1 bar}}$$

$$= \frac{3.43}{0.785}$$

$$\text{No. of bars} = 4.36 \approx 5 \text{ bars}$$

So 5 # 8 bar

for Tensile zone.

compression steel

we # 6 bars

$$\text{dia } (6/8) = 0.75''$$

$$\text{Area} = 0.44 \text{ ft} \quad 0.44 \text{ in}^2$$

$$\text{No. of bars} = \frac{A_{st}}{\text{Area of 1 bar}}$$

$$\frac{0.37}{0.44} = 0.84$$

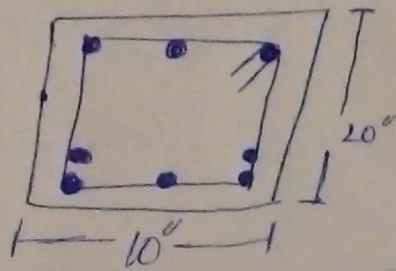
$$0.84 \approx 1 \text{ bar}$$

So 1 # 6 bars in compression zone

Step # 8

Beam minimum width

$$\begin{aligned}
 b_{\min} &= 2(1.5) + 2\left(\frac{3}{8}\right) + 5\left(\frac{8}{8}\right) + 4\left(\frac{8}{8}\right) \\
 &= 12.75 > 10'' \\
 &\text{in multiple layer.}
 \end{aligned}$$



$$\begin{aligned}
 \text{Effective depth } (d) &= 20 - 15 - \frac{3}{8} - \frac{8}{8} - \frac{1}{2}\left(\frac{8}{8}\right) \\
 d &= 16.62''
 \end{aligned}$$

$$\begin{aligned}
 \text{Effective cover } = d' &= 1.5 + \frac{3}{8} + \frac{1}{2}\left(\frac{6}{8}\right) \\
 &= 2.25''
 \end{aligned}$$

Step # 9

Design moment is given by

$$M_d = \phi \times \left[A_{st}' \times f_{y'} \times (d - d') + A_{st} - A_{st}' \times f_y \times \left(d - \frac{a}{2}\right) \right]$$

$$\cancel{M_d} \Rightarrow a = \frac{A_{st} - A_{st}' \times f_y}{0.85 \times f_c' \times b}$$

$$a = \frac{5 \times 0.785 - 1 \times 0.44 \times 60}{0.85 \times 4 \times 10}$$

$$a = 6.15''$$

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$$m_d = 0.90 \times \left[(1 \times 0.44) \times 60 \times (16.62 - 2.25) + \right. \\ \left. (5 \times 0.785 - 1 \times 0.44) \times 60 \times \right. \\ \left. (16.62 - \frac{6.15}{2}) \right]$$

$$m_d = 2890.46$$

$$m_d = 2890.46 > 2653.56$$

Design is OK

Question 2Ans.(a) Bond Stress:-

The stress which is acting on the outer underface of steel is the surrounding concrete is called bond stress.

The stress help in keeping bond b/w reinforcement and concrete together. Bond stress resists any force that tries to pull out the rods from the concrete.

Development length-

Development length can be define as.

The length of the bar required for transferring the stress into the concrete.

In other word Development length is the quantity of the rebar length that is actually required to be enclosed into the concrete to make the desired bond strength b/w two materials and furthermore to produced required stress in the steel at that area. Why are providing development length because of

*To develop a safe bond between the bar surface and concrete so that no failure due to slippage of bar occur during the ultimate loading condition.

(b) Doubly Reinforced Beam

Beam reinforced with steel in compression zone and tension zone are called Doubly Reinforced Beam

condition when Doubly Reinforced Beam used we can use the doubly Reinforced Beam on that condition when the restriction occur in the size beam.

for example:

if someone said that the depth of the beam should not be greater than 12" and the external load on beam is very much which can not resist a beam of singly Reinforcement is that condition we used doubly Reinforced Beam

(c) T Beam

(1) T beam having beam and slab composite section.

(2) A T-beam is more economical than Rectangular Beam

(3) T-beam are more often used for more heavy duty or larger space such as

Rectangular Beam

(1) A rectangular Beam is one which is generally used as compression in top fibre and Tension in bottom fibre of that beam

(2) Rectangular Beam is less economical than T Beam

(3) Rectangular beam are more often used in office or commercial buildings.

These can be cost in sites

T-beam bridges These are almost always present using prestress reinforcement

Rectangular beam insite using standard reinforcement.

(d) Effect of Strength Reduction factor on flexural strength

in the design of flexural strength. the strength reduction factor decrease from tension control section to compression controlled section to increase safety with decreasing ductility this show to determine the reduction factor for flexural strength of reinforcement concrete.

(e) Design method.

Two methods are widely used for the designing of concrete structure member. and different

(1) ASD method

(2) USD method.

(1) ASD method -

ASD method is also known as working stress design method It is based on the principle that stresses developed in the structural member.

Should not exceed a certain limit friction of elastic limit.

- (*) In this method all load are taken as service load and no factor is applied to increase these services load.

USD Method:-

ultimate strength design method is also known as load factor method for the structural subjected to large external load the ultimate strength is determine by the weleastic analysis.

- (*) USD method is best for designing different structure method because of the following Reason

- (1) As the ultimate strength of the material is considered we will get much standard section for column and beam compare a other method

Question #3

Ans.

Given data :-

$$\text{slab thickness} = 6''$$

$$\text{Total depth (h)} = 28''$$

$$\text{web width} = 14''$$

$$\text{Effective depth} = 28'' - 3 = 25''$$

$$\text{Span} = 32'$$

$$\text{c/c distance} = 10'$$

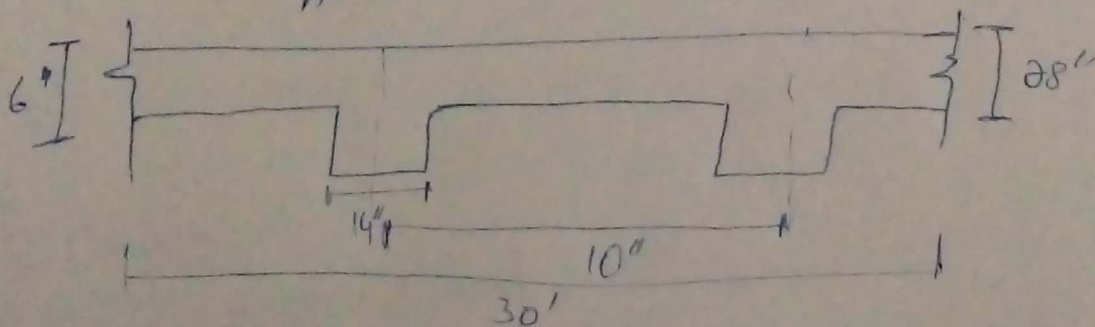
$$D.L = 50 \text{ lb/ft}^2$$

$$S.S = 225 \text{ lb/ft}^2$$

$$f_y = 60,000 \text{ psi}$$

$$f'_c = 4000 \text{ psi}$$

Solution:- As we know that



Step #1

$$M_U = \frac{w_u \times L^2}{8}$$

① Beam self weight per foot

$$w_t = b \times t \times \gamma_c$$

$$= \frac{14}{12} \times \frac{28}{12} \times 150$$

$$w_t = 408.33 \text{ Lb/ft}$$

Total factored load:-

$$= 1.2 (50 + 408.33) + 1.6 (225)$$

$$= 909.99 \text{ Lb/ft}$$

$$= 0.909 \text{ Kip/ft}$$

Moment:-

$$\frac{wL^2}{8}$$

$$\frac{0.909 \times (32)^2}{8} \times 12$$

$$= 1396.23 \text{ Kip/inch}$$

Effective Breadth

$$\textcircled{1} \quad 16 h_f + b_w = 16(6) + 14 = 110''$$

$$\textcircled{2} \quad \text{c/c distance} = 10(12) = 120''$$

$$\textcircled{3} \quad \text{Span}/4 = \frac{32}{4} \times 12 = 96''$$

Step # 3

Rectangular or T-Beam

Trail # 1. let $\alpha - h_f = 6''$

$$A_{st} = \frac{M_u}{\phi \times F_y \times (d - a/2)}$$

$$A_{st} = \frac{1396.23}{0.90 \times 60 \times (25 - 6/2)}$$

$$A_{st} = \frac{1396.23}{0.90 \times 60 \times (25 - 6/2)}$$

$$A_{st} = 1.17 \text{ in}^2$$

Trial #2

$$a = \frac{A_{st} \times f_y}{0.85 \times f_c' \times b}$$

$$a = \frac{1.17 \times 60}{0.85 \times 4 \times 96}$$

$$a = 0.2" < 6"$$

So Rectangular Beam design.

$$A_{st} = \frac{1396.23}{0.90 \times 60 \times (25 - \frac{0.2}{2})}$$

$$A_{st} = 1.03 \text{ in}^2$$

Step #3

$$a = \frac{1.03 \times 60}{0.85 \times 4 \times 96}$$

$$a = 0.18"$$

$$A_{st} = \frac{1396.23}{0.90 \times 60 \times (25 - \frac{0.18}{2})}$$

$$A_{st} = 1.03 \text{ in}^2$$

Step #4

Check f_{max} and f_{min}

$$f_{max} = 0.85 \times 0.85 \times \frac{4}{60} \left(\frac{0.003}{0.003 + 0.005} \right)$$

$$f_{max} = 0.018$$

$$f_{min} = \frac{200}{F_y}$$

$$f_{min} = \frac{200}{60,000} = 0.003$$

$$f = \frac{A_{st}}{b \times d} = \frac{1.03}{14 \times 25} = 0.0029$$

$$f_{min} < f < f_{max}$$

$$0.003 < 0.0029 < 0.018$$

As

f is less than f_{min}

So

$$f = \frac{A_{st}}{b \times d}$$

$$A_{st} = f_{min} \times b \times d$$

$$A_{st} = 0.003 \times 14 \times 25$$

$$A_{st} = 1.05 \text{ in}^2$$

Step #5

No and selection of Bar

let use #8 then

$$\text{dia } (8/8) = 1''$$

$$\text{Area} = 0.785 \text{ in}^2$$

$$\text{no. of bar} = \frac{1.05}{0.785} = 1.3 \approx 2$$

So we use 2 #8 bars.

Step #6

Minimum width.

$$b_{\min} = 2(1.5) + 2(3/8) + 2(8/8) + 1(8/8)$$

$$= 6.75'' < 14''$$

So good is one layer

Step #7 Design moment

$$M_d = \phi \times f_y \times A_{st} \times (d - a/2)$$

$$\text{Area of steel} = \text{Area of 1 bar} \times \text{No. of bars}$$

$$= 0.785 \times 2 = 1.57 \text{ in}^2$$

$$a = \frac{1.57 \times 60}{0.85 \times 4 \times 96} = 0.2''$$

$$M_d = 0.90 \times 60 \times 1.57 \times (25 - 0.2/2)$$

$$= 2111.02 \text{ kip-in.}$$

$$A_s \quad 2111.02 > 1396.23 \quad \text{Design is OK!}$$