

IQRA NATIONAL UNIVERSITY



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| <i>Paper:</i> | <i>Communication system</i> |
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Department of Electrical Engineering

Final Assignment Summer 2020

Subject: Communication Systems

Question 1 (10)

A signal $x(t)$ band limited by 250 Hz is sampled by an impulse train with angular frequency of ω_s

- a. Determine the Nyquist rate required for perfect reconstruction of signal.
- b. Considering $x(t)$ and impulse train in figure below, construct all the signals involved in sampling.
- c. Determine the cut off frequency of reconstruction filter $H(f)$ to be used for the signal given in question.
- d. If the frequency of sampler is 800 s f Hz , draw the resulting sampled signal $s(f)$

Date (1)



QUESTION 1:-

a, Nyquist rate required for a signal:-

Solution:-

As we know Nyquist rate \Rightarrow
 $f_s \geq 2f_m$.

$$f_m = 250 \text{ Hz}$$

So

$$f_s \geq 2 \times 250 \text{ Hz}$$

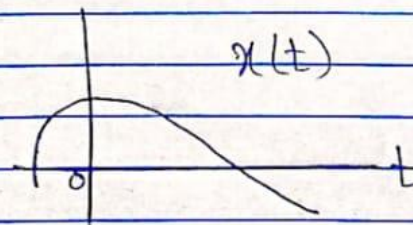
$$f_s \geq 500 \text{ Hz}$$

$$\boxed{\text{Nyquist rate} = 500 \text{ Hz}}$$

Now,

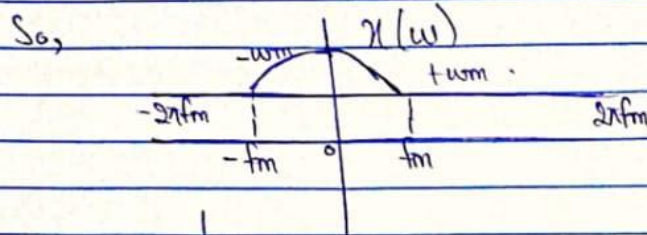
b,

$$x(t) =$$



If we take Fourier transform of signal.

Date (2)



↓
Spectrum of continuous signal

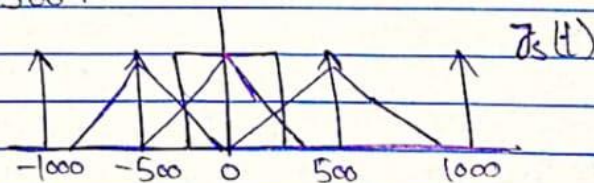
$$W_m = \frac{2\pi}{T_s}$$

T_s shows impulse train.

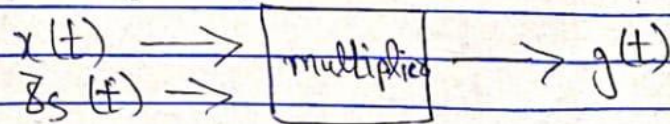
$$T_s = \frac{1}{f_s}$$

$$= \frac{1}{500}$$
$$= 0.002$$

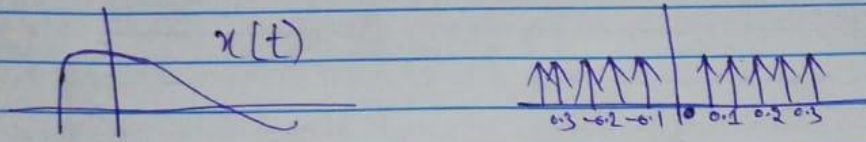
As $f_s = 500$.



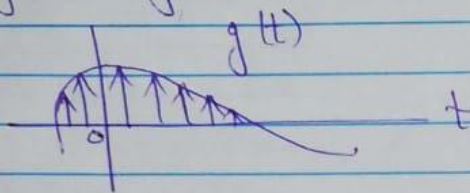
Now if we multiply the $x(t)$ and $\delta_s(t)$ we get sampling signal.



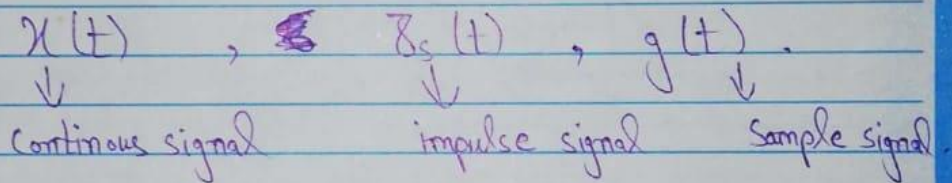
Date (3)



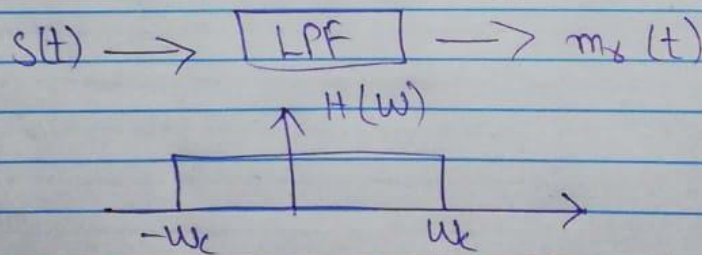
Sampling signal :-



So these are the signals which involve in sampling.

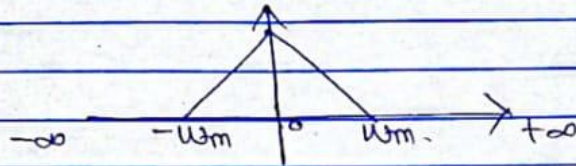


↳ When we pass a signal from LPF.



So, cut off frequency :-

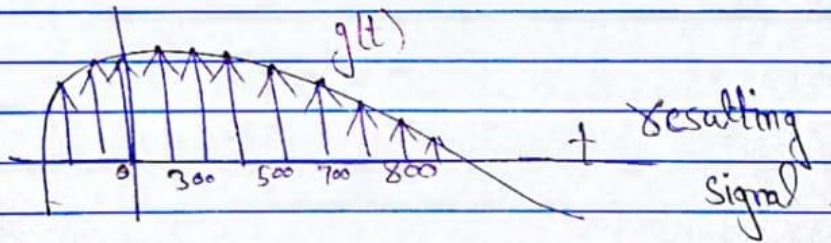
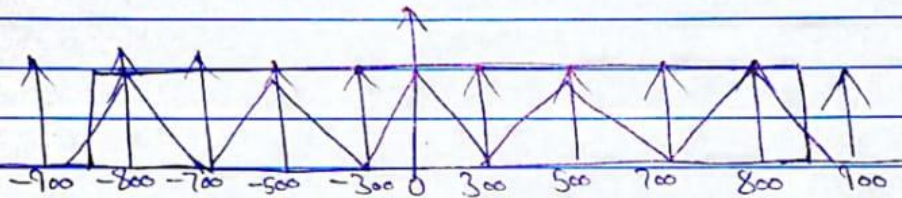
Date (4)



d, i.

if $f_s = 800 \text{ Hz}$

Resulting sample signal.



Question 2 (10)

$x(t)$ be a signal with Nyquist rate

f_s

determine the Nyquist rate for following

i. $(1 - \cos(\pi t))x(t)$

Date (1)



QUESTIONS 2 :-

PART A :-

i) $x(t) + x(t-1)$

Solution:-

Given Nyquist rate = f_s

So,

$$m(t) = x(t) + x(t-1)$$

↓

This is our message signal.

$$x(t) = \text{Nyquist rate} = f_s$$

So,

$$x(t) = f_s$$

When we do time shifting.

$$x(t) \xrightarrow{\text{T.S.}} x(t-1)$$

We get $x(t-1)$ after time shifting.

Therefore,

$$\text{Nyquist rate for } x(t-1) = f_s$$

So,

$$\boxed{x(t) = f_s}$$
$$\boxed{x(t-1) = f_s}$$

Therefore

$$\boxed{m(t) = f_s}$$

Answer

ii. $\int dx t$

Date (2)

ii) $\frac{dx(t)}{dt}$

Now,

$$m(t) = \frac{dx(t)}{dt}$$

So if $x(t) = f_s$

Nyquist rate $x(t) = f_s$

So,

after derivation

$$\frac{dx(t)}{dt} = f_s$$

So the Nyquist rate of $\frac{dx(t)}{dt}$ is also f_s .

$$\frac{dx(t)}{dt} = f_s$$

Answer

dt b. Let $x(t) = 10\sin(400\pi t)$ is sampled at 300Hz and reconstructed using an ideal low pass filter with a cut off frequency of 150Hz. What are the frequency/frequencies present in the reconstructed signal $y(t)$

Date (3)



QUESTION 2 :-

(PART B)

Solution :-

Given :-

$$m(t) = 10 \sin 400\pi t$$

$$f_s = 300 \text{ Hz}$$

$$\text{Cutt off frequency} = 150 \text{ Hz}$$

frequency of frequencies present in reconstructed signal = ?

$$m(t) = 10 \sin 400\pi t$$

So,

$$\omega_m = 400\pi \text{ rad/sec}$$

Now,

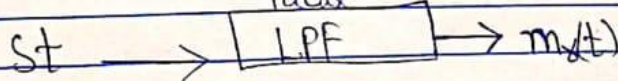
$$f_m = \frac{\omega_m}{2\pi}$$
$$= \frac{400\pi}{2\pi}$$

$$f_m = 200 \text{ Hz}$$

$$f_s = 300 \text{ Hz}$$

$$f_c = 150 \text{ Hz}$$

ideal



Date (4)



$$n f_s \pm f_m$$

Now,

finding frequency component of
reconstructed signal.

$$n = 0,$$

$$n = 0 \Rightarrow \pm f_m = \pm 200 \text{ Hz}$$

$$n = 1 \Rightarrow \pm f_s \pm f_m = 500 \text{ Hz}, 100 \text{ Hz}$$

$$n = -1 \Rightarrow -f_s \pm f_m = -100 \text{ Hz}, -500 \text{ Hz}$$

Frequency component of input is b/w
-150 Hz to +150 Hz

So

the reconstructed signal frequency
component is b/w
-100 Hz to 100 Hz.

So,

frequency present in reconstructed signal is

$$y(t) = 100 \text{ Hz}$$

Question 3 (15)

Consider the bit sequence (0 1 1 0 1 1 0 0 0 1 1) and draw the PCM waveform for following modulation schemes

- a. NRZ-S b. Polar-RZ c. Split Phase Manchester d. Bi- ϕ -L e. Dicode - NRZ

Date (1)

QUESTION 3 :-

Sequence :- (0 1 1 0 1 1 0 0 0 1 1)

PCM waveform :-

(i) For NRZ-S :-

NRZ-S (Differential Encoding)

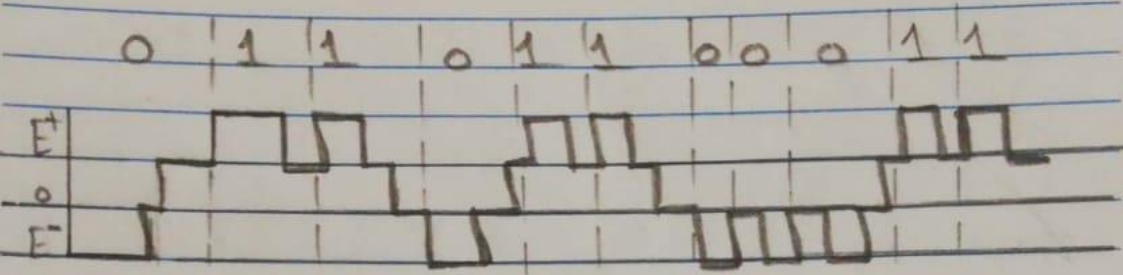
-> "One" is represented by no change in level.

-> "Zero" is represented by a change in level.

Date (2)

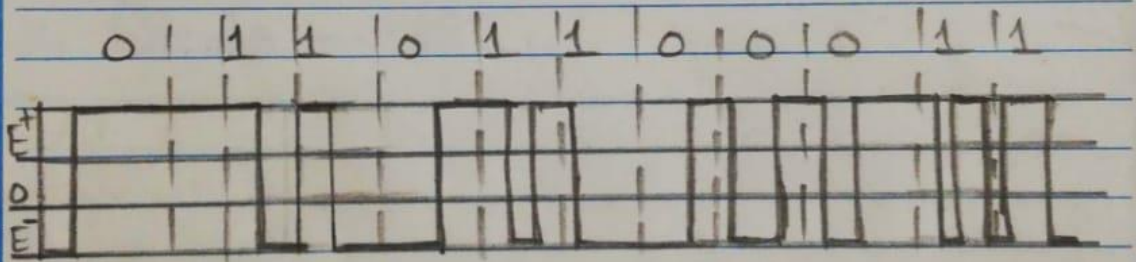


(ii) Polar R-Z.



→ "One" and zero are represented by opposite level polar pulses that are one half-bit in width.

(iii) Split Phase Manchester :-



Split Phase Manchester :-

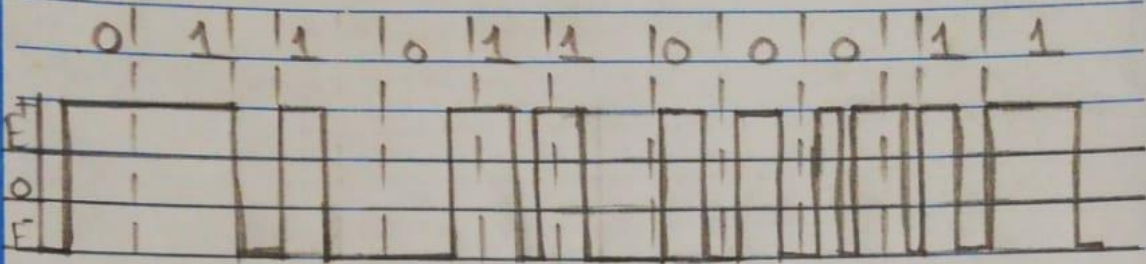
→ "One" is represented by 10.

→ "Zero" is represented by 01.

Date (3)



iv, Bi \oplus L :-

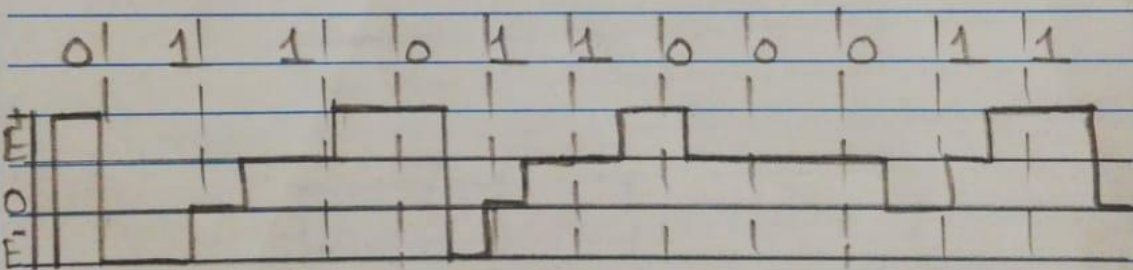


Bi \oplus L :-

-> "one" is represented by 10.

-> "Zero" is represented by 01.

v, Dicode - NRZ :-



\Question 4 (15)

a. A carrier wave is represented by the equation $e_c(t) = 7.5 \sin(20 \times 10^3 \pi t)$. If the modulation index of wave is 0.5, draw the waveform of AM modulated waveform. b. A sinusoidal carrier $5 \cos(50 \times 10^3 \pi t)$ is amplitude modulated by the sinusoidal voltage of $35 \cos(628 \times 10^3 \pi t)$ over a load resistance of 50Ω .

- a. Find the depth of modulation and calculate the transmission efficiency
- b. Plot the AM wave in time domain as well as its frequency domain spectrum
- c. Calculate the total power in spectrum
- d. Calculate the percentage power in USB

Date 4



QUESTION 4 :- (PART A)

Solution :-

Given :-

$$m = 0.5 \quad e_c = 7.5 \quad \therefore E_c = 7.5 \text{ volts}$$

Let us evaluate E_m from E_c . Since $m = \frac{E_m}{E_c}$

Therefore,

$$\begin{aligned} E_m &= m \times E_c \\ &= 0.5 \times 7.5 \\ &= 3.75 \text{ Volt} \end{aligned}$$

$$\begin{aligned} E_{\max} &= E_c + E_m \\ &= 7.5 + 3.75 \\ &= 11.25 \text{ volt} \end{aligned}$$

$$\begin{aligned} E_{\min} &= E_c - E_m \\ &= 7.5 - 3.75 \\ &= 3.75 \text{ volt} \end{aligned}$$

Modulated waveform :-

So,

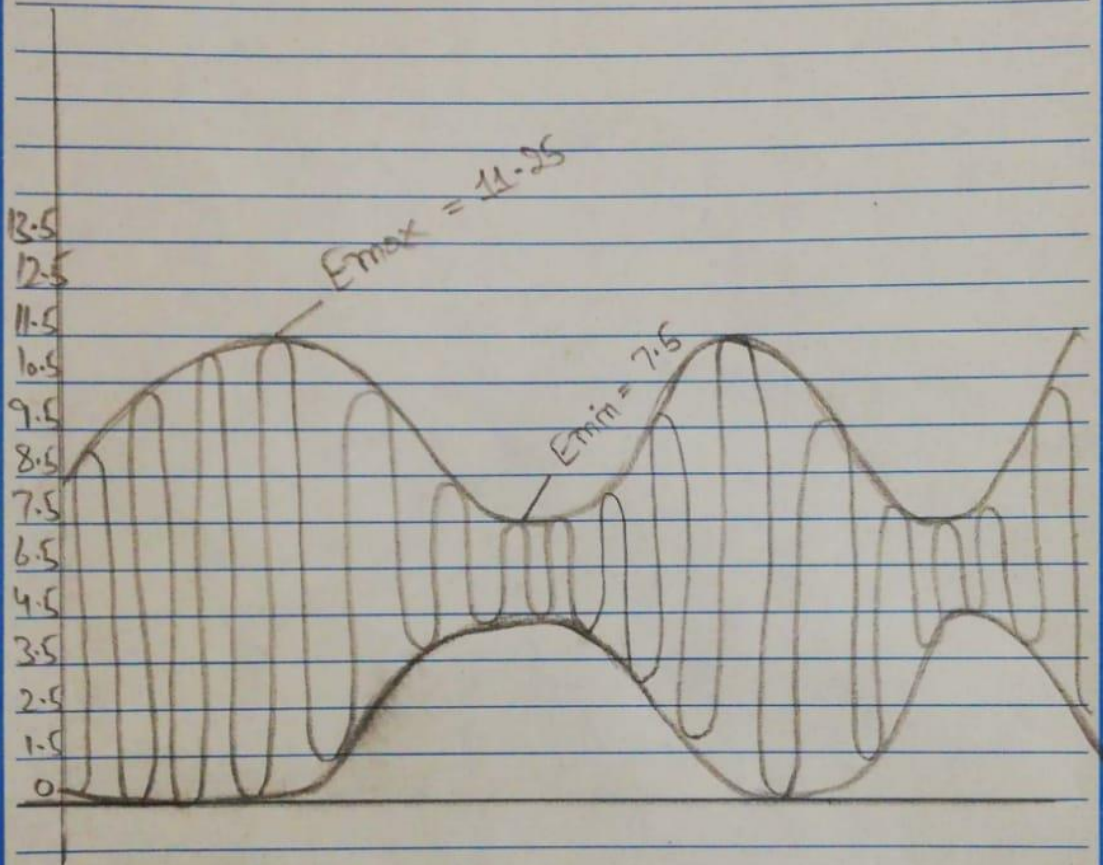
As we know,

$$m = 0.5$$

$$E_{\max} = 11.25$$

$$E_{\min} = 3.75$$

Date 5



Date _____



PART B QUESTION 4 :-

Solution :-

$$\begin{aligned} \text{Carrier signal} &= 10 \cos 50 \times 10^5 t \\ \text{Message} &= 5 \cos 628 \times 10^3 t \\ R &= 50 \Omega \end{aligned}$$

a, Depth :-

$$\begin{aligned} m &= \frac{50 \times 10^5}{628 \times 10^3} \\ &= 7.96 \end{aligned}$$

Power of both side.

$$P_{LSB} = P_{USB} = P_c \frac{\mu^2}{4}$$

$$P_c = \frac{A_c^2}{2R} = \frac{(10)^2}{2 \times 50}$$

$$\begin{aligned} P_c &= 1 \text{ W} \\ &= \frac{1 \times 7.96}{4} \end{aligned}$$

$$P_{LSB} = P_{USB} = \boxed{1.99 \text{ W}}$$

Efficiency of AM :-

$$\eta = \frac{P_{LSB} + P_{USB}}{P_t} = \frac{\mu^2}{2 + \mu^2} = \frac{(7.96)^2}{2 + 7.96} = \boxed{6.1}$$

Date _____



c, Total power:-

$$P_t = \frac{P_{cu}^2}{2}$$
$$= \frac{1 \times (7.96)^2}{2}$$

$$= 31.68 \text{ W}$$

d,

Power in USB %.

$$\text{Power in USB} = 1.99 \text{ W}$$

$$\% \text{ power in USB} = \frac{1.99}{100} = 0.0199\%$$

