

NAME

HAISER SIDDIQUE

ID

7863

SECTION

B

Assignment

02

SUBJECT

DRCD-I

SUBMITTED TO.

ENGR FAWAD KHAN.

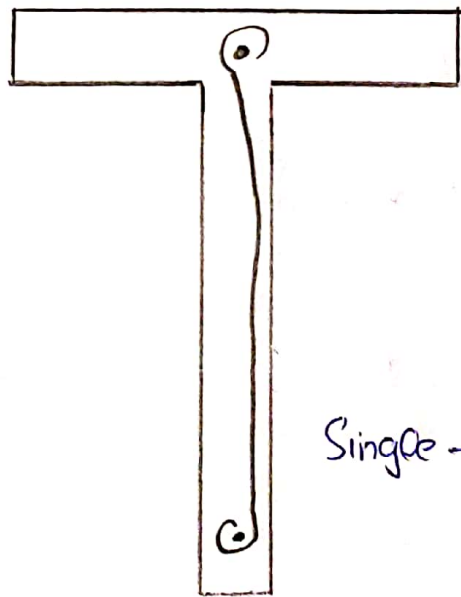
Q<sub>1</sub> Explain in detail types of stirrups with figures & also explain ACI codes for shear design?

Ans Following are the types of stirrups.

- Single legged stirrups.
- Two legged or double legged stirrups.
- Four legged stirrups.
- Six legged stirrups.

### 1- SINGLE LEGGED STIRRUPS:-

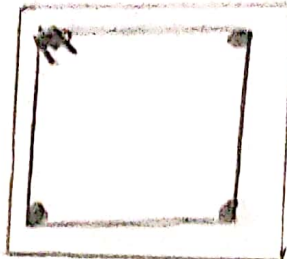
These type of stirrups are used to hold the longitudinal bars in position,  $E_c$  prevent buckling.



Single-legged stirrups.

### 2- DOUBLE LEGGED STIRRUP:-

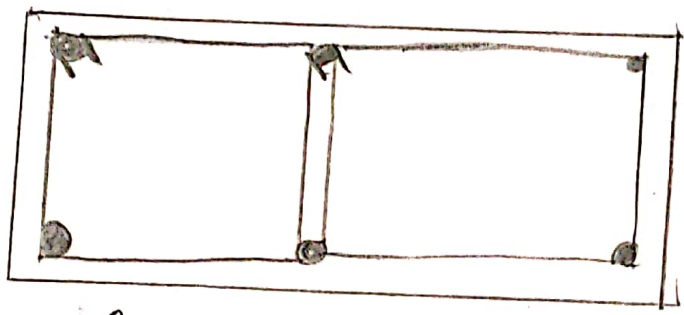
We use a single stirrup to tie a beam or a column at a time, we say it is two legged stirrups - Double legged stirrups are adequate for typical beams with relatively short widths.



Two-legged stirrups

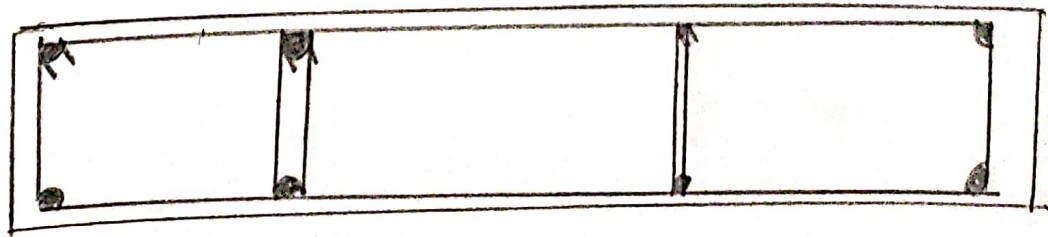
### 3- FOUR LEGGED STIRRUP:

We use double to the tie of beam or column at a time, we say it is Four legged stirrup - For legged stirrup - For beam having longer widths multiple legged or four legged or four legged stirrups are required.



### 4- SIX LEGGED STIRRUP:

These six legged stirrups are generally used for a continuous beam structure, it consists of regular upholding of structure at each junction while joints at the joining of beam & column.



# ACI CODES FOR SHEAR DESIGN

- 1- Compute the design shear force,  $V_u$  at appropriate location.
- 2- Compute shear strength capacity of concrete,  $V_c = 2 \times \sqrt{f_c} \times b_w \times d$
- 3- Compute Minimum web reinforcement.  
 $\phi V_u \leq \phi V_c$  So no web reinforcement needed.

If it is not applicable then min area of web reinforcement equal to.

$$A_v = 0.75 \sqrt{f_c'} \times \frac{b_w \times s}{f_y} \quad \text{OR} \quad A_{min} = \frac{50 \times b_w \times s}{f_y}$$

→ Max spacings can be found by these formula's.

$$S_{max} = \frac{A_v \times f_y}{0.7 \times \sqrt{f_c'} \times b_w} \quad \text{OR} \quad S_{max} = \frac{A_v \times f_y}{50 \times b_w}$$

4 If  $V_u \leq \frac{\phi V_c}{2}$ , if its true no stirrups are required

5 First stirrup is provided at a distance  $s/2$

6 Between " $V_u$ " and " $\phi V_c$ " spacing b/w web reinforcement is found by formula.

$$s = \frac{\phi \times A_v \times f_y \times d}{V_u - \phi V_c}$$

7 If  $V_u \leq 4 \times \sqrt{f_c'} \times b_w \times d$  - then max spacing of stirrups will be smallest of the following.

# Four Conditions:

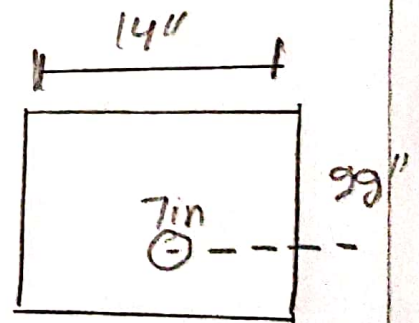
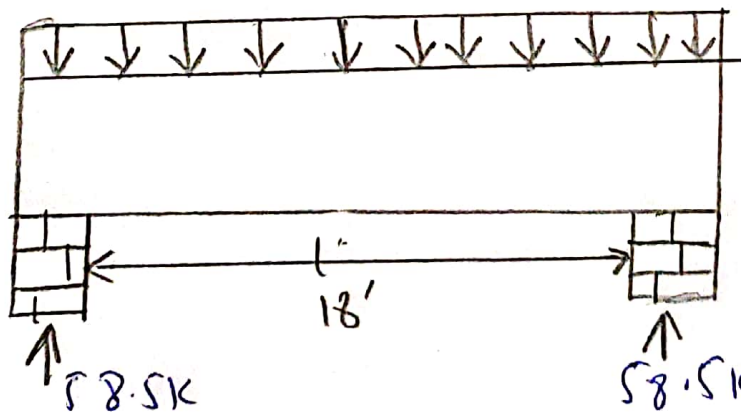
1-  $24''$     2-  $d/a$     3-  $S_{max} = \frac{A_u \times f_y}{0.75 \times f_c \times b_w}$     4-  $S_{max}$

$$\frac{A_u \times f_y}{S_o \times b_w}$$

8 If  $V_s > 4 \times \sqrt{f_c} \times b_w \times d \rightarrow$  then max spacing will be halved

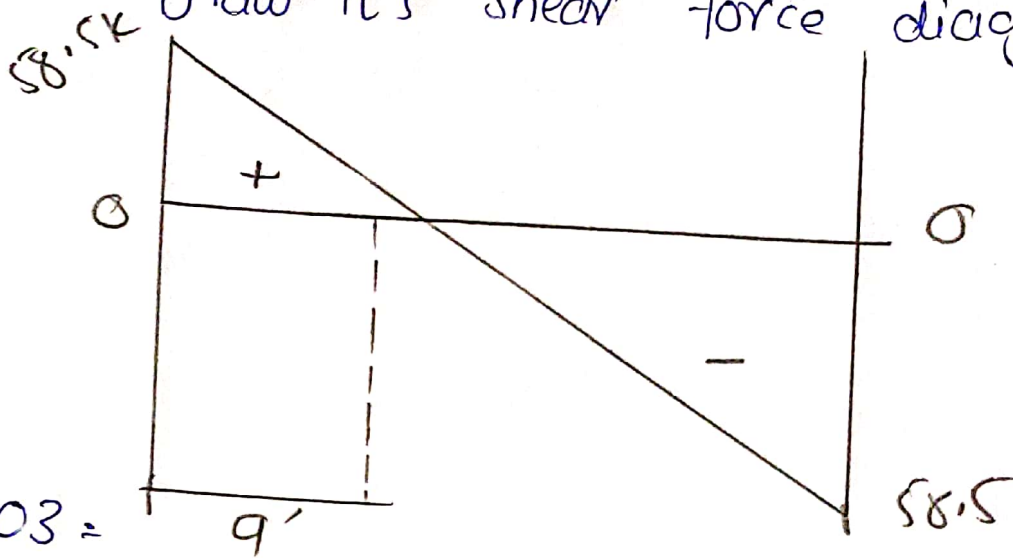
If  $V_s > 8 \times \sqrt{f_c} \times b_w \times d$  then increase cross-sectional dimensions or increase " $f_c$ "

Q-2 A simply supported rectangular beam 14" wide having an effective depth 22" to carry a lateral load of 6.5 k/ft on a 18' simple span. It is reinforced with 7 in of tensile steel area, if  $f_c$  is 4k &  $f_y$  is 60ksi then design the beam for shear.  $w_v = 6.5 \times l / f$

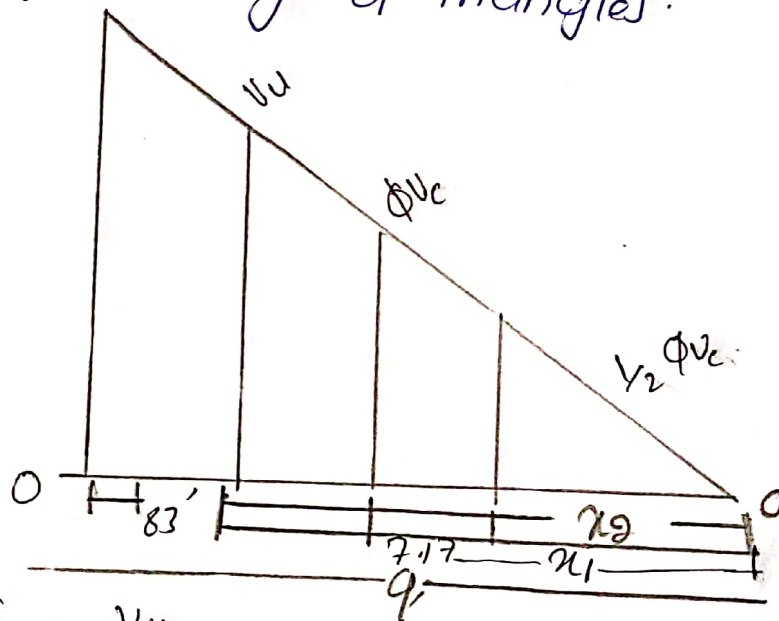


Step 01: Find the reaction on support.  
 total load =  $\frac{6.5 \times 18}{2} = 58.5 \text{ k}$

Step 02 = Draw it's Shear force diagram.



Step 03 = Finding the value of critical stress " $V_u$ " and it's from the face of supports  $d = 99' = 1.83'$  using similarity of triangles.



$$\frac{58.5}{9} = \frac{V_u}{1.83}$$

$$V_u = \frac{58.5 \times 1.83}{9} = 11.83 \text{ k}$$

Step 04: Finding the value of " $V_u$ " and " $\frac{1}{2} \phi V_c$ " and also it's distance from zero shear to right side.

By Formula,

$$\Rightarrow \phi V_c = \phi \times 2 \times \sqrt{F_c} \times b_w \times d$$

$$= 0.75 \times 2 \times \sqrt{4000} \times 14 \times 22$$

$$= 29.21 \text{ k}$$

\* Location of " $\phi V_c$ " by Similar triangles.

$$\frac{58.5}{9} = \frac{\phi V_c}{x_1} \Rightarrow \frac{58.5}{9} = \frac{99.21}{x_1}$$

$$x_1 = 4.49'$$

Now,

$$\frac{1}{2} \phi V_c = \frac{99.21}{9} = 14.60k$$

location of  $\frac{1}{2} \phi V_c$  will be

$$\frac{58.5}{9} = \frac{14.60}{x_2}$$

$$x_2 = 2.24'$$

Step 05: Finding the value of " $\phi V_s$ "

$$\begin{aligned} \phi V_s &= V_u - \phi V_c \\ &= 46.605 - 99.21 \end{aligned}$$

$$\phi V_s = 17.395$$

Step 06: Check on section adequacy

By Formula

$$= \phi \times 8 \times \sqrt{f'_c} \times bw \times d$$

$$= 0.75 \times 8 \times \sqrt{4000} \times 14 \times 99$$

$$= 116.87k$$

As  $\phi \times 8 \times \sqrt{f'_c} \times bw \times d > \phi V_s$  thus section is adequate.

Step 07 :- Check on Max spacing for stirrups

By Formula:

$$= \phi \times 4 \times \sqrt{f'_c} \times bw \times d = 0.75 \times 4 \times \sqrt{4000} \times 14 \times 99$$

$$= 58.43k$$

As  $\phi \times 4 \times \sqrt{f'_c} \times bw \times d > \phi V_s$

So max spacing will be selected from the following 4 condition.

1 -  $24''$       2 -  $\frac{d}{2} = \frac{22}{2} = 11''$       3 -  $S_{max} = \frac{A_u \times f_y}{0.75 \times \sqrt{f'_c} \times b_w}$

Let's suppose we use #3 stirrups, dia =  $\frac{3}{8} = 0.375''$

Area =  $\frac{\pi}{4} (0.375)^2 = 0.11 \text{ in}^2$

For - 2 legged stirrup Area  $\times 2$   
 $= 0.11 \times 2 = 0.22 \text{ in}^2$

3 -  $S_{max} = \frac{0.22 \times 60000}{50 \times 14} = 18.25''$

4 -  $S_{max} = \frac{A_u \times f_y}{50 \times b_w} = \frac{0.22 \times 60000}{50 \times 14} = 19.87''$

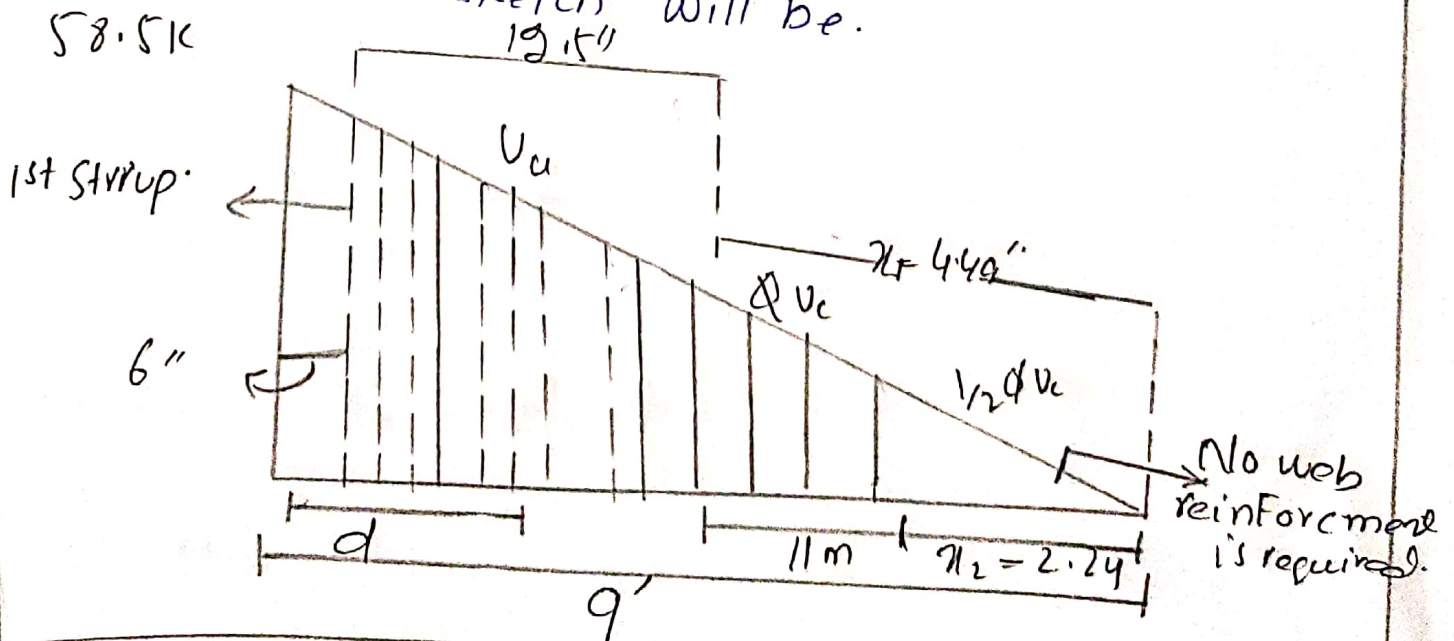
So we choose the last value from the above values  
 $S_{max} = 11''$

Step 08: Stirrups spacing from critical section.

By Formula  $S = \frac{\phi \times A_u \times f_y \times d}{V_u - \phi V_c} = \frac{0.75 \times 0.22 \times 80 \times 22}{48.605 - 29.21}$   
 $S = 12.52 \approx 12.5''$

So 13.5" c/c.

Step 09: Final sketch will be.





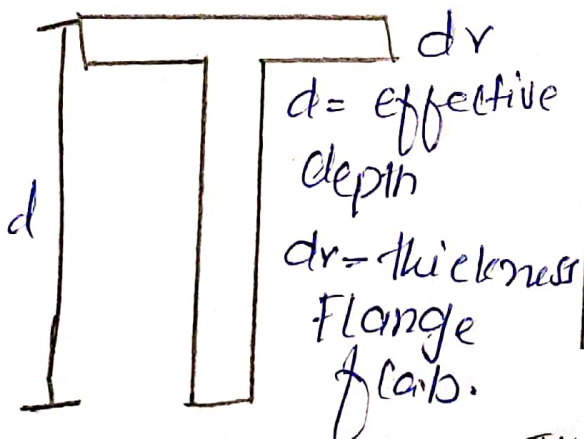
First Startup From Face of Support.

$$s/2 = \frac{12.5}{2} = 6.25 \approx 6''$$

Q<sub>3</sub> Define both the T-beam and L-beam with the help of diagram - Also explain flexural strength analysis for T-beam

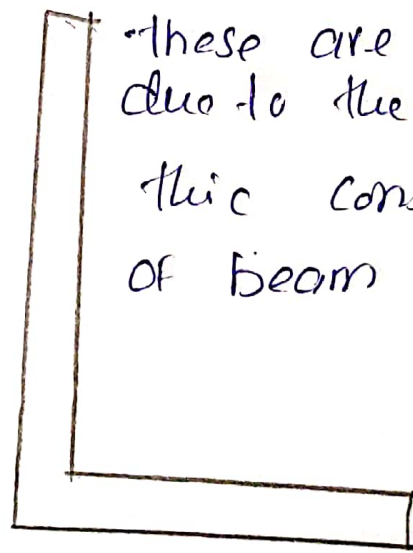
### T BEAM

- It is local bearing structure of reinforcement concrete, wood or metal, with a T-shaped cross-section
- the top of the T-shaped serves as flange or compression member in resisting compressive stress



### L-BEAM

- A beam whose section has the form of an inverted L, usually placed so that its top flange forms part of the edge of a floor.



• these are produced due to the moment this construction of beam & slab.

### FLEXURE STRENGTH ANALYSIS FOR T-BEAM.

• Find the ultimate factored load (moment) by the formula -

$$m_u = \frac{w_u \times l^2}{8}$$

Effective depth 'be' for T-beam is computed as formula.

- i)  $16(h_f) + b_w$
  - ii) c/c distance
  - iii)  $\text{Span} / 4 \times \frac{\text{ivctS} + h}{2}$
- Select last value from the above values.

Check whether Rectangular or T-beam analysis is required.

- i) If  $a > h_f$  then T-beam analysis required.
- ii) If  $a < h_f$  then Rectangular analysis is required.

Find the Area of Steel.

$$A_{st} = m_u$$

$$\frac{\phi \times f_y \times (d - a/2)}{0.85 \times f_c' \times b_w} \quad , \quad a = \frac{A_{st} \times f_y}{0.85 \times f_c' \times b_w}$$

Check the range of reinforcement ratio

$$f_{max} = 0.85 \times B \times \frac{f_c'}{f_y}$$

$$f_{min} = \frac{200}{f_y} \left( \frac{e_u}{\epsilon_{st}} \right)$$

$$f = \frac{A_{st}}{b \times d}$$

Find the bars - No of bars =  $A_{st} / (A_b)$ .

Check min width for bar accommodation ( $b_{min} = 22 \times \text{dia of bar} + \text{No of bars (dia of bar)} + \text{spacing b/w bars (dia of bar)}$ )

Design moment is given as  $m_d = \phi \times f_y \times A_{st} \times (d - a/2) = 1F a c h f$

$$m_e = \phi \times [A_{st} \times f_y \times (d - h_f / 2) (A_s - A_{st}) + F \times (d - a/2)] \quad \text{if } a > h_f$$

What is the difference b/w CASE-I & Case-II in the design of T-beam.

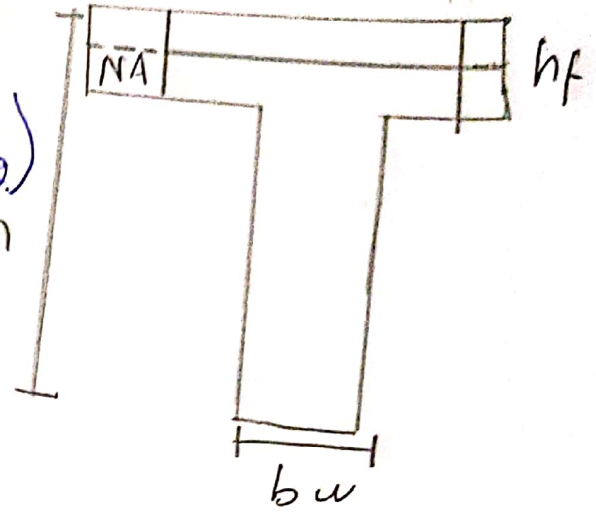
CASE - I:

From the figure

$$a < h_f$$

So in this case, rectangular beam analysis is required so the design moment formula will be.

$$M_d = \phi \times f_y \times A_{st} \times (d - a/2)$$



CASE II

From the figure

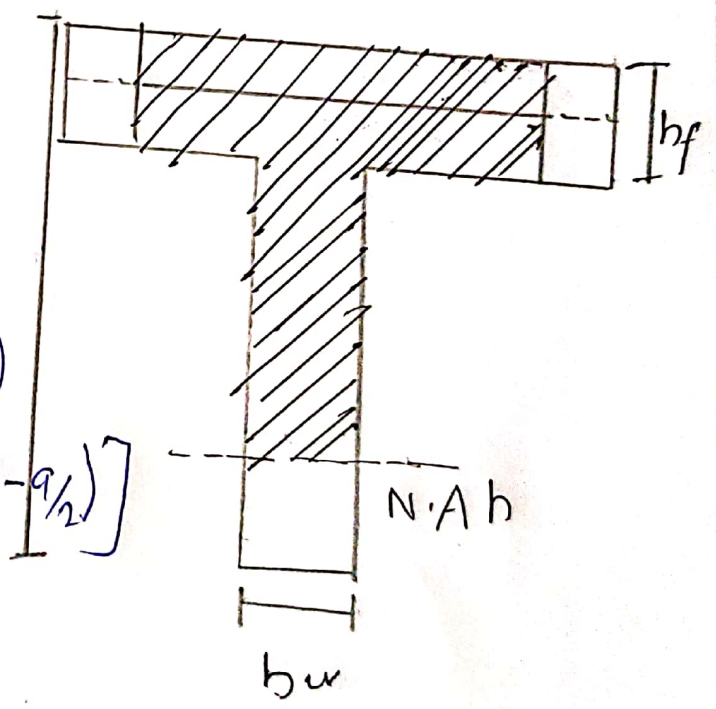
$$a > h_f$$

So in this, special beam analysis is required

So design moment

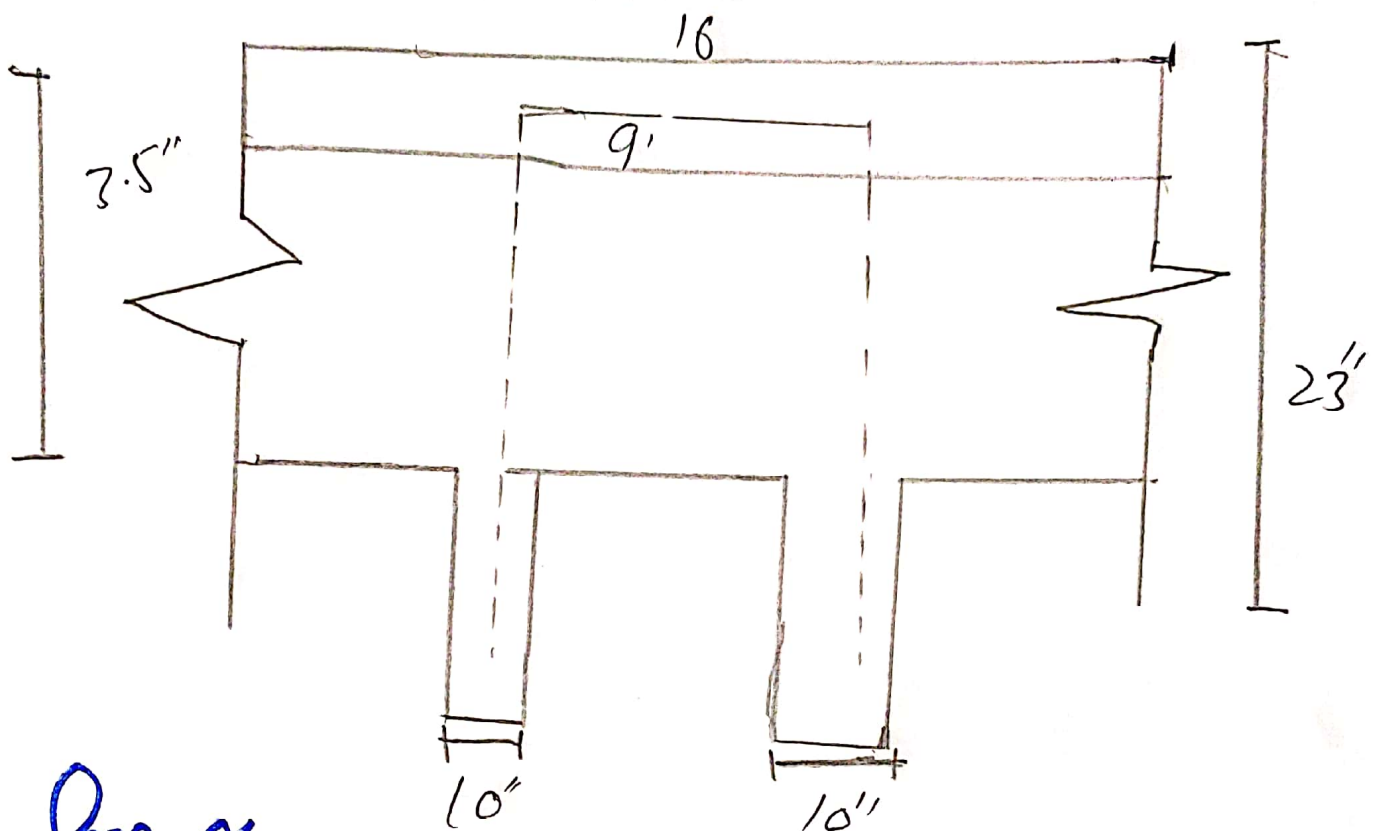
will be.

$$M_d = \phi \times [A_s \times f_y \times (d - h_f/2) + (A_s - A_{st}) \times f_y \times (d - a/2)]$$



A floor consists of 3.5" concrete slab supported by 16 simple span spaced at 9' c/c, the beam having a web width of 10" and effective

depth of 18" and total height is 23"  
 Calculate the necessary flexural reinforcement  
 + applied moment is 5800k-in use  $f_c'$   
 = 3ksi and  $f_y$  60ksi



**STEP 01:**

Calculate the effective width ( $b_e$ )  
 for T-beam -

- 1-  $16 h_f + b_w = 16(3.5) + 10 = 66"$
- 2- etc distance =  $9 \times 12 = 108"$
- 3- span / 4 =  $16 / 4 \times 12 = 48"$

Selecting the last value of  $b_e = 48"$

**STEP 02:**

Check the whether rectangular or T-beam angles is required.

**Trial # 1**

let  $a = h_f = 3.5"$

$$A_s = \frac{m_u}{\phi \times f_y \times (d - a/2)} = \frac{5800}{0.9 \times 60 \times (18 - 3.5/2)} = 6.6 \text{ in}^2$$

Trial # 2

$$a = \frac{A_{ST} \times f_y}{0.85 \times f_c \times b_e} = \frac{6.61 \times 60}{0.85 \times 3 \times 148} = 3.25$$

$$A_{ST} = \frac{M_u}{\phi \times b \times (d - a/2)} = \frac{5800}{0.90 \times 60 \times (18 - \frac{3.24}{2})} = 6.56 \text{ in}^2$$

Trial # 3

$$a = \frac{A_{ST} \times f_y}{0.85 f_c \times b_e} = \frac{6.56 \times 60}{0.85 \times 3 \times 48} = 3.21 \text{ in}$$

$$A_{ST} = \frac{M_u}{\phi \times f_y \times (d - a/2)} = \frac{5800}{0.90 \times 60 \times (18 - \frac{3.21}{2})} = 6.52 \text{ in}^2$$

thus rectangular beam analysis is required

STEP 03:

Check  $f_{max} \leq f_{min}$

$$f_{max} = 0.85 \times \beta \times \frac{f'_c}{f_y} \times \left( \frac{\epsilon_u}{\epsilon_u + \epsilon_t} \right)$$

$$= 0.85 \times 0.85 \times \frac{3}{60} \times \left( \frac{0.003}{0.003 + 0.005} \right)$$

$$= 0.014$$

$$f_{min} = \frac{200}{f_y} = \frac{200}{80000} = 0.003$$

$$f_r = \frac{A_{ST}}{b \times d} = \frac{6.55}{10 \times 18} = 0.036$$

thus the value of  $f_{max} < f_r < f_{min}$  so we have to

$$f_{min} < f_r < f_{max}$$

calculate  $A_{ST}$  again

$$0.03 < 0.036 < 0.014$$

$$A_{ST} = f_{max} \times b \times d$$

$$A_{ST} = 0.014 \times 10 \times 18$$

$$A_{ST} = 2.52 \text{ in}^2$$

### STEP 04: Selection and No of Bars.

let's use #8 So dia (8/8) = 1"

By formula:-

$$Area = \pi/4 (1)^2 = 0.785 \text{ in}^2$$

$$No \text{ of bars} = \frac{A_{ST}}{A_b} = \frac{2.59}{0.785} = 3.21 \approx 4 \text{ bars}$$

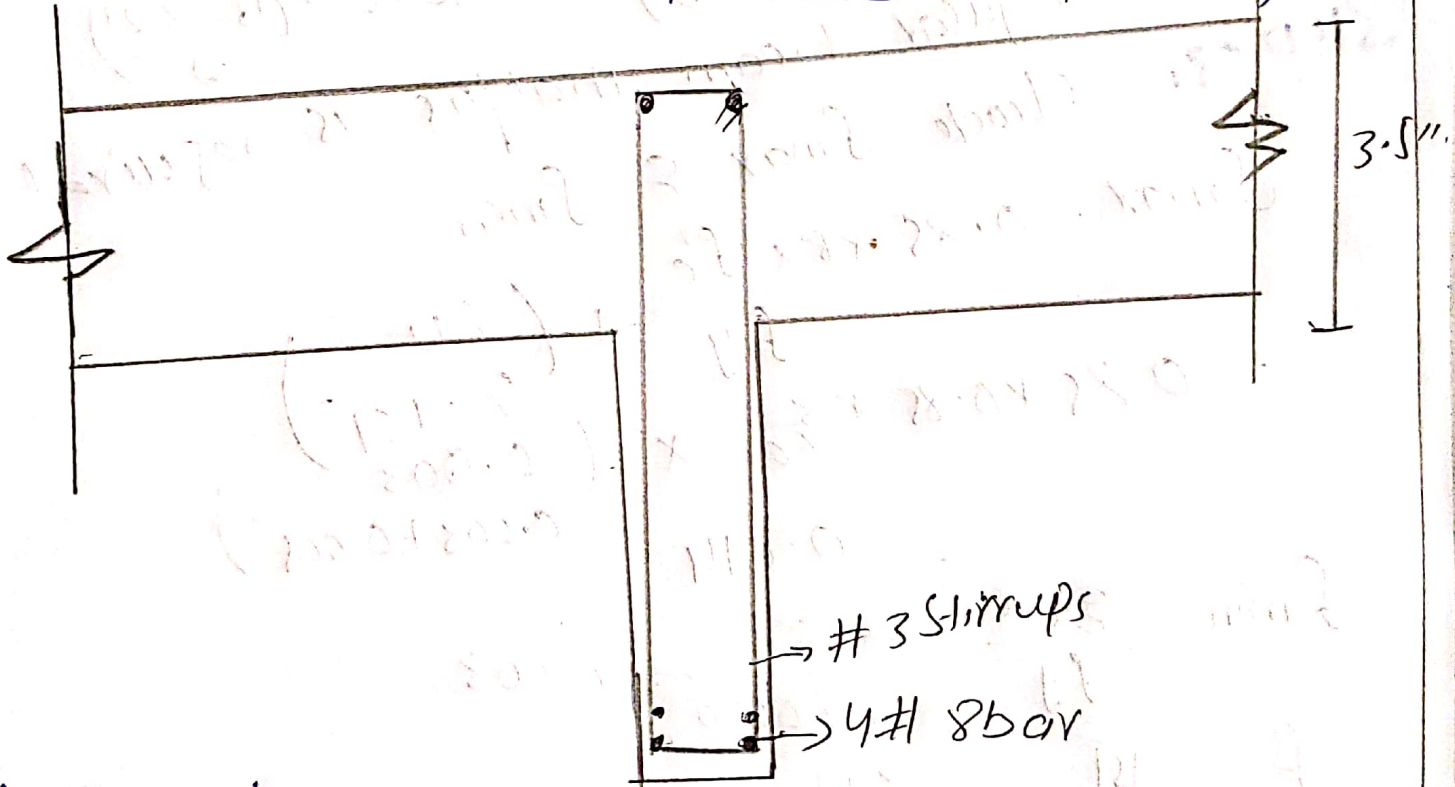
### STEP 05:

Check on minimum width

$$b_{min} (2 \times 1.5) + (2 \times 3/8) + (4 \times 8/8) + 3 (8/8) = 10.75"$$

$$As \ 10.75" > 10"$$

So it should be provided in two layers.



### STEP 06: design moment $M_u$

By using Formula

$$M_u = \phi \times f_y \times A_{ST} (d - a/2)$$

$$\therefore A_{ST} \Rightarrow \text{No of bars} \times \text{Area of single bar}$$

$$= 4 \times 0.785$$

$$= 3.14 \text{ in}^2$$

$$a = \frac{A_{st} \times f_y}{0.85 \times f_{c'} \times b} = \frac{3.14 \times 60}{0.85 \times 3 \times 14} = 1.54$$

$$M_d = 0.90 \times 60 \times 3.14 \times (18 - \frac{1.54}{2})$$

$$M_d = 2921.52 \text{ k-in}$$

$2921.52 < 5800$  thus design is ok!

Q6 A beam is revised to developed and ultimate moment of 6000 k-m limited to 14 x 26 inch size use  $f_c'$  is 4ksi and  $f_y$  is 60ksi. Determine flexural reinforcement and effective depth of beam is 22".

$$\text{Breadth} = 14''$$

$$\text{Height} = 26''$$

concrete compression strength ( $f_c'$ ) = 4ksi

$$f_y = 60\text{ksi}$$

$$M_u = 6000 \text{ k-in}$$

$$d = 22''$$

$$\text{Assume } d' = 2.5''$$

**Step 01:** Reinforcement Ratio

$$f_{max} = 0.85 \times \frac{f_c'}{f_y} \times \left( \frac{\epsilon_u}{\epsilon_u + \epsilon_y} \right)$$

$$= 0.85 \times 0.85 \times \frac{4}{60} \times \left( \frac{0.003}{0.003 + 0.005} \right)$$

$$f_{max} = 0.0120$$

**Step 02:** Area of Steel

As we know that

$$f_{max} = \frac{A_{st}}{b \times d} \Rightarrow A_{st} = f_{max} \times b \times d$$

$$= 0.0120 \times 14 \times 22$$

$$\text{Area } 5.54 \text{ in}^2$$

15  
Step 03 : Design Moment  
Using Formula

$$M_{u2} = \phi \times A_{st} \times f_y \times (d - a/2)$$

$$a = \frac{A_{st} \times f_y}{0.85 \times f'_c \times b} = \frac{5.54 \times 60}{0.85 \times 4 \times 14} = 6.48''$$

$$M_{u2} = 5537.4 \text{ k-in}$$

As  $5537.4 < 6000$

So we have to design a section as double reinforcement beam

Step 04: Difference in moment.

$$M_{u1} = M_u - M_{u2}$$

$$= 6000 - 5537.4$$

$$M_{u1} = 462.6 \text{ k-in}$$

Step 05: Area of Steel

$$M_{u1} = \phi \times A_{st} \times f_y \times (d - d')$$

So Area of Steel in Compression Zone will be

$$A_{st} = \frac{M_{u1}}{\phi \times f_y \times (d - d')} = \frac{462.6}{0.9 \times 60 \times (22 - 2.5)} = 0.44 \text{ in}^2$$

Step 06: Selection and No of bars used.

Steel and tension zone

We use #7 bar.

$$\text{dia } (7/8) = 0.875'', \text{ Area } \pi/4 (0.875)^2 = 0.60 \text{ in}^2$$

So, No of bars in compression

$$\frac{A_s}{A_b} = \frac{5.98}{0.601} = 9.9 \approx 10 \text{ bar}$$

So, 10 #7 bars.



9 - Steel in Compression Zone.

Let's use # 5 bar

So, dia  $\frac{5}{8} = 0.625''$ ,  $A = \frac{\pi}{4} (0.625)^2 = 0.306 \text{ in}^2$

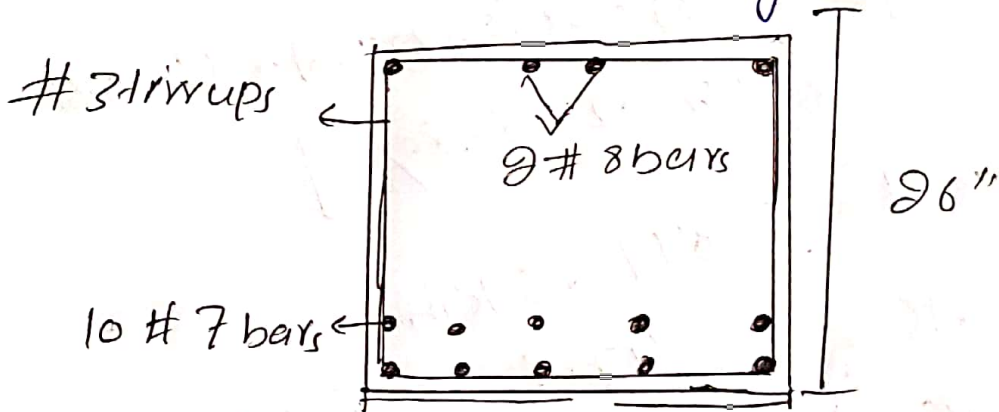
No of bars =  $\frac{A_s}{A_b} = \frac{0.44}{0.306} = 1.43 \approx 2 \text{ Bars}$

So 2 # 5 bars.

STEP 08: Minimum width of beam

Mini =  $(2 \times 1.5) + (2 \times \frac{3}{8}) + 10 (\frac{7}{8}) + 9 (\frac{7}{8})$   
 $b_{\text{min}} = 20.37 > 14''$

So not good in one layer



Now,

→ Effective depth  $(d) = 26 - 1.5 - \frac{3}{8} - \frac{7}{8} - \frac{1}{2}$   
 $(\frac{7}{8})$

= 22.28"

= Effective cover  $(d') = 1.5 + \frac{3}{8} + (\frac{5}{8}) \cdot \frac{1}{2}$

= 2.18"

Step 09: Design Moment.

$$M_d = \phi \times [A_{sT} \times f_y \times (d - d') + (A_{sT} - A_{sT}) \times f_y \times (d - a/2)]$$

$$a = \frac{(A_{sT} - A_{sT}) \times f_y}{0.85 \times f_c' \times b} = \frac{(10 \times 0.601 - 2 \times 0.306) \times 60}{0.85 \times 4 \times 14}$$

$$a = 8.80''$$

$$M_d = 0.90 \left[ (2 \times 0.306) \times 60 \times (22.82 - 2.18) + (10 \times 0.601 - 2 \times 0.306) \times 60 \times (22.82 - 8.80/2) \right]$$

$$M_d = 7047.6 \text{ Kin}$$

$$A_s = 7047.6 > 6000$$

Design is ok!