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Program:- M.S (CEM)

Subject:- Advanced Mechanics of Materials.

Paper:- Final Term

Date:- 29/09/2020

Q No (02)

①

Ans :-

① Given data:-  $AE = 20070 \text{ GPa}$

② Cross sectional Area of AB =  $50 \text{ mm}^2$

③ link CD = steel made.  $E = 200 \text{ GPa}$

Cross sectional Area of link CD =  $600 \text{ mm}^2$

$F = \text{Roll no} = 15367$

$F = \text{1st two digits of R} = 15 \text{ kN}$

Required :-

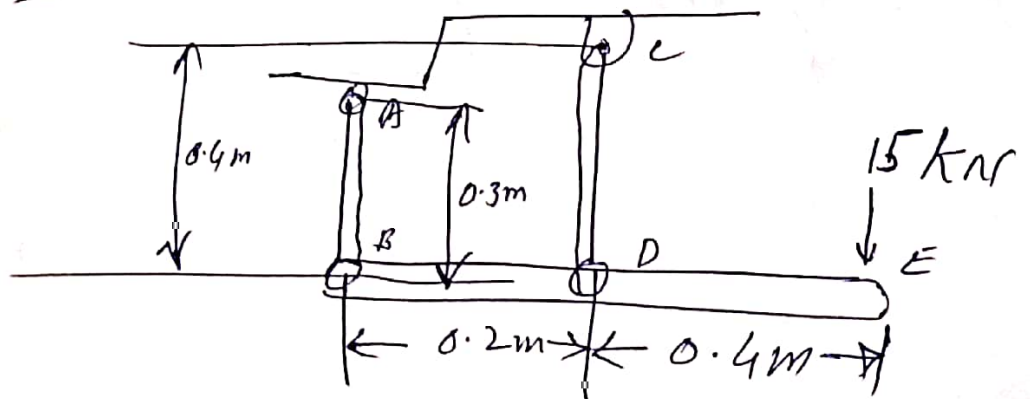
deflection at

① of B

② of D

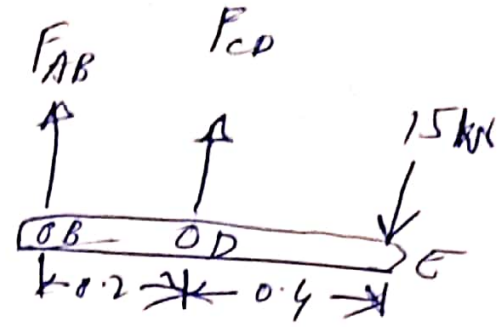
③ of E

Diagram :-



(2)

bar BDE as F.B. Diagram



$$\sum M_B = 0$$

$$F_{CD} \times (0.2) - 15 \times (0.6) = 0$$

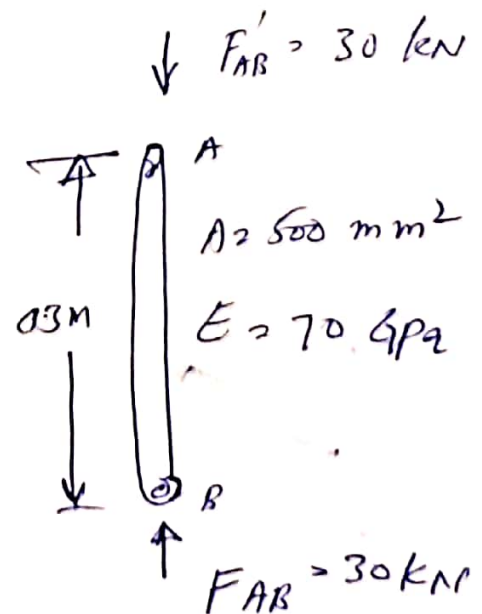
$$F_{CD} = \frac{15 \times 0.6}{0.2} \text{ kN}$$

$$F_{CD} = \frac{9.00}{0.2} = +45 \text{ kN}$$

$$\uparrow \sum F_y = 0 \rightarrow F_{AB} + F_{CD} - 15 = 0$$

$$F_{AB} = 15 - 45 = -30 \text{ (comp)}$$

(a) Deflection of B



P.T.O

(3)

$$\delta_B = \frac{PL}{AE} = \frac{(-30 \times 10^3)(0.3)}{(70 \times 10^9)(5 \times 10^{-6})}$$

$$\delta_B = \frac{-9000}{350000}$$

$$\delta_B = -0.02571 \text{ m.}$$

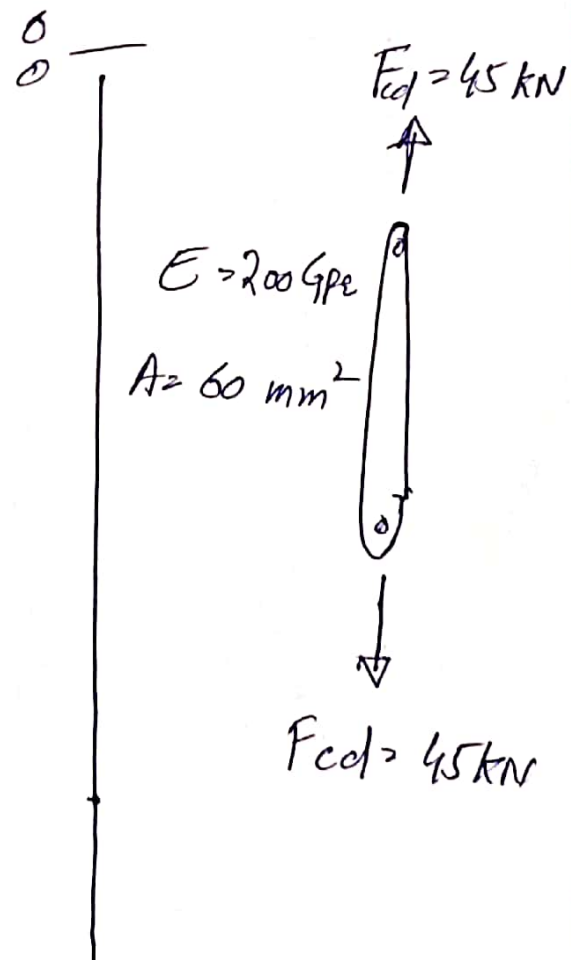
$$\boxed{\text{or } \delta_B = -25.71428 \text{ mm}} \text{ Ans}$$

(B) Deflection of D

$$\delta_D = \frac{PL}{AE} = \frac{(45 \times 10^3)(0.4)}{(200 \times 10^9)(60 \times 10^{-6})}$$

$$\Rightarrow \frac{18000}{12000000}$$

p.f.o



(4)

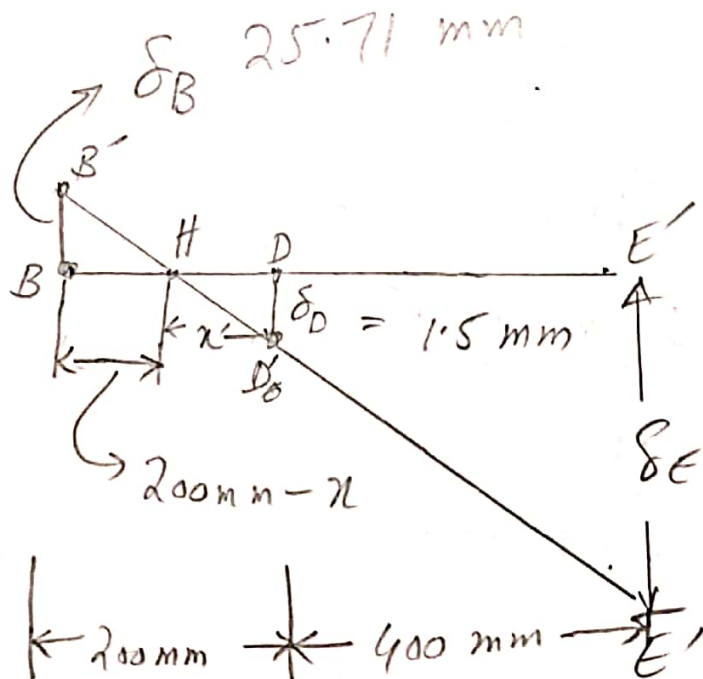
$$\delta_D = \frac{18000}{12000000} = 0.0015 \text{ m}$$

$$\delta_D = 0.0015 \text{ m}$$

PR  $\delta_D = 1.5 \text{ mm}$  Ans-

© Deflection of E :-

Diagram



We denote by  $B'$  &  $D'$  the displaced positions of points  $B$  &  $D$ .

Since the bar  $BDE$  is rigid, points  $B'$ ,  $D'$  and  $E'$  lie in a straight line and we write

$$\frac{BB'}{DD'} = \frac{BH}{HD} = \frac{25}{1.5} = \frac{200 - x}{x}$$

$$x = 11.32 \text{ mm}$$

$$\frac{EE'}{DD'} = \frac{HE}{HD}$$

$$\frac{\delta E}{\cancel{HD} \cdot 1.5} = \frac{400 + 11.32}{11.32}$$

$$\delta E = \frac{411.32 \times 1.5}{11.32} = 54.5 \text{ mm}$$

$$\boxed{\delta E = 54.5 \text{ mm} \downarrow \text{Ans.}}$$

(8)

Q. No 04

Given Data: -

$$b = 4 \text{ in} \quad h = 6 \text{ in}$$

$$t = 0.15 \text{ in}$$

$V =$  1st two digits of  $R + 3$  kips

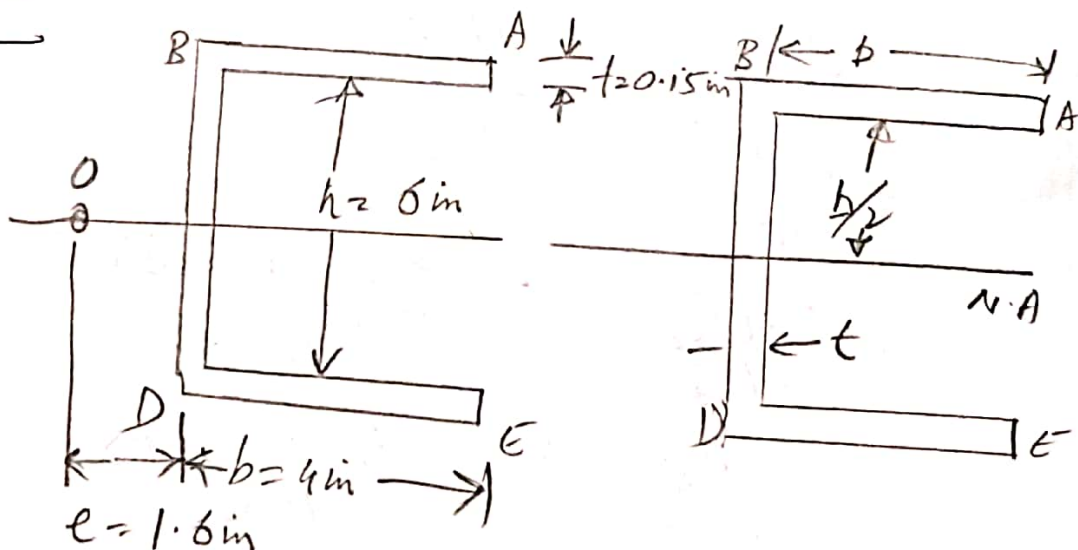
$R = \underline{\underline{15367}}$

So  $V = 15 + 3 = \underline{\underline{18 \text{ kips.}}}$

Required: -

Determine Shear Stress Distribution for  $V$

Diagram: -



(7)

① shear stress distribution in flange.

$$\tau = \frac{vQ}{It}$$

From Diagram

$$\tau_B = \frac{vQ}{It} = \frac{v}{It} (st) \frac{h}{2} = \frac{vh}{2I} s$$

$$\tau_B = \frac{vhb}{2 \left( \frac{th^2}{12} \right) (6b+h)}$$

$$\tau_B = \frac{6vb}{th(6b+h)} \text{ ————— (A)}$$

putting values in eq (A)

$$\tau_B = \frac{6 \times 18 \times 4}{(0.15)(6)(6 \times 4 + 6)}$$

$$\boxed{= 16 \text{ ksi}}$$

$$\tau_B =$$

Ans



8

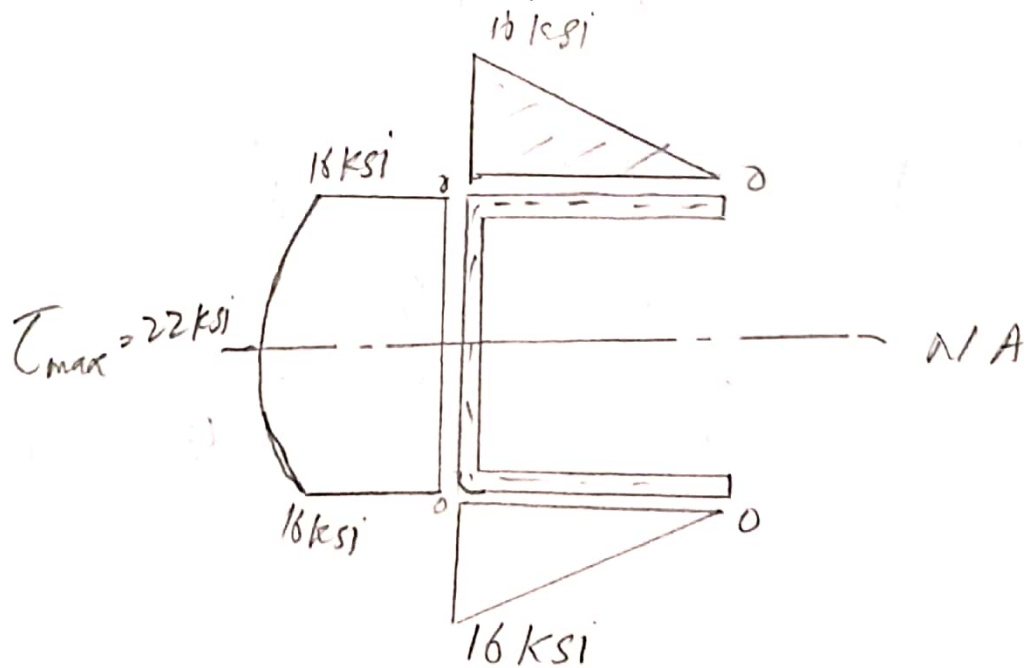
(ii) Shear stress in web

$$\tau_{max} = \frac{VQ}{IE} = \frac{v \left( \frac{ht}{8} \right) (4b+h)}{\frac{1}{2} + h^2 (6b+h)t}$$

$$\tau_{max} = \frac{3v (4b+h)}{2+h (6b+h)}$$

$$\tau_{max} = \frac{3 \times 18 (4 \times 4 + 6)}{2 (0.15) (6) (4 \times 6 + 6)}$$

$\tau_{max} = 22 \text{ ksi}$  Ans



Q No 03

(9)

Ans :-

Given Data.

$$G = \text{1st two digits of } R \times 10^6 \text{ psi}$$

$$R = 15367$$

$$G = 15 \times 10^6 \text{ psi}$$

Required  $\rightarrow$  largest torque  $T_0$  of shaft AB

Solution :-

Denoting by  $F$  the magnitude of tangential force between gear teeth we have

$$\text{Gear B: } \Sigma M_B = 0$$

$$\Rightarrow F \times (0.875 \text{ m}) - T_0 = 0$$

$$\text{Gear C: } \Sigma M_C = 0$$

$$= F \times (2.45 \text{ m}) - T_{CD} = 0$$

$$T_{CD} = 2.8 T_0 \quad \text{--- (A)}$$

$$R_C = 2.45 \text{ in}$$

$$R_B = 0.875 \text{ in}$$

$$\gamma_B \phi_B = \gamma_C \phi_C$$

$$\phi_B = \phi_C \frac{\gamma_C}{\gamma_B}$$

$$\Rightarrow \phi_C \times \frac{2.45}{0.875 \text{ in}} = 2.8 \phi_C \rightarrow \textcircled{B}$$

① Torque  $T_0$  of shaft AB

with  $T_{AB} = T_0$  and  $c = 0.375 \text{ in}$

with max shearing stress of 8000 psi

$$\tau = \frac{T_{AB} c}{J} = 8000 \text{ psi} = \frac{T_0 (0.375 \text{ in})}{\frac{1}{2} \pi A^2 (0.375 \text{ in})^4}$$

$T_0 = 663 \text{ lb}\cdot\text{in}$

Q5)

11

Ans

Given Data.

Ball 1st two Digits of Ro: No + 4 ksi

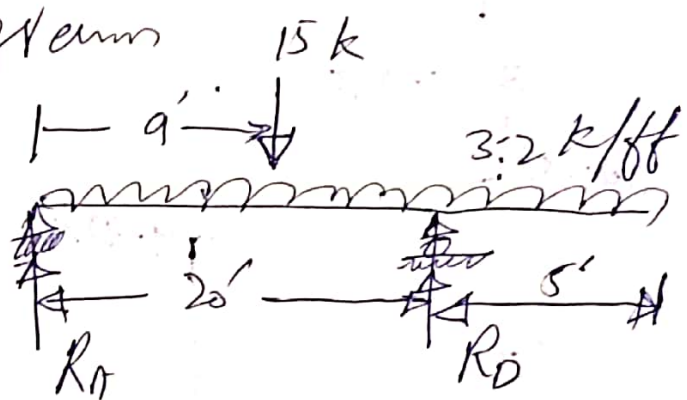
$$R = 15367$$

$$\delta_{all} = 15 + 4 \text{ ksi} = 19 \text{ ksi}$$

$$\tau_{all} = 15 + 1 = 16 \text{ ksi}$$

Solution:

Diagram



① Reactions at A & D

$$\sum M_A = 0 \quad (\text{clockwise})$$

$$R_D \times 20 = 15 \times 9 + 3.2 \times 25 \times \frac{25}{2}$$

$$R_D = 56.75 \text{ k}$$

p.d.o

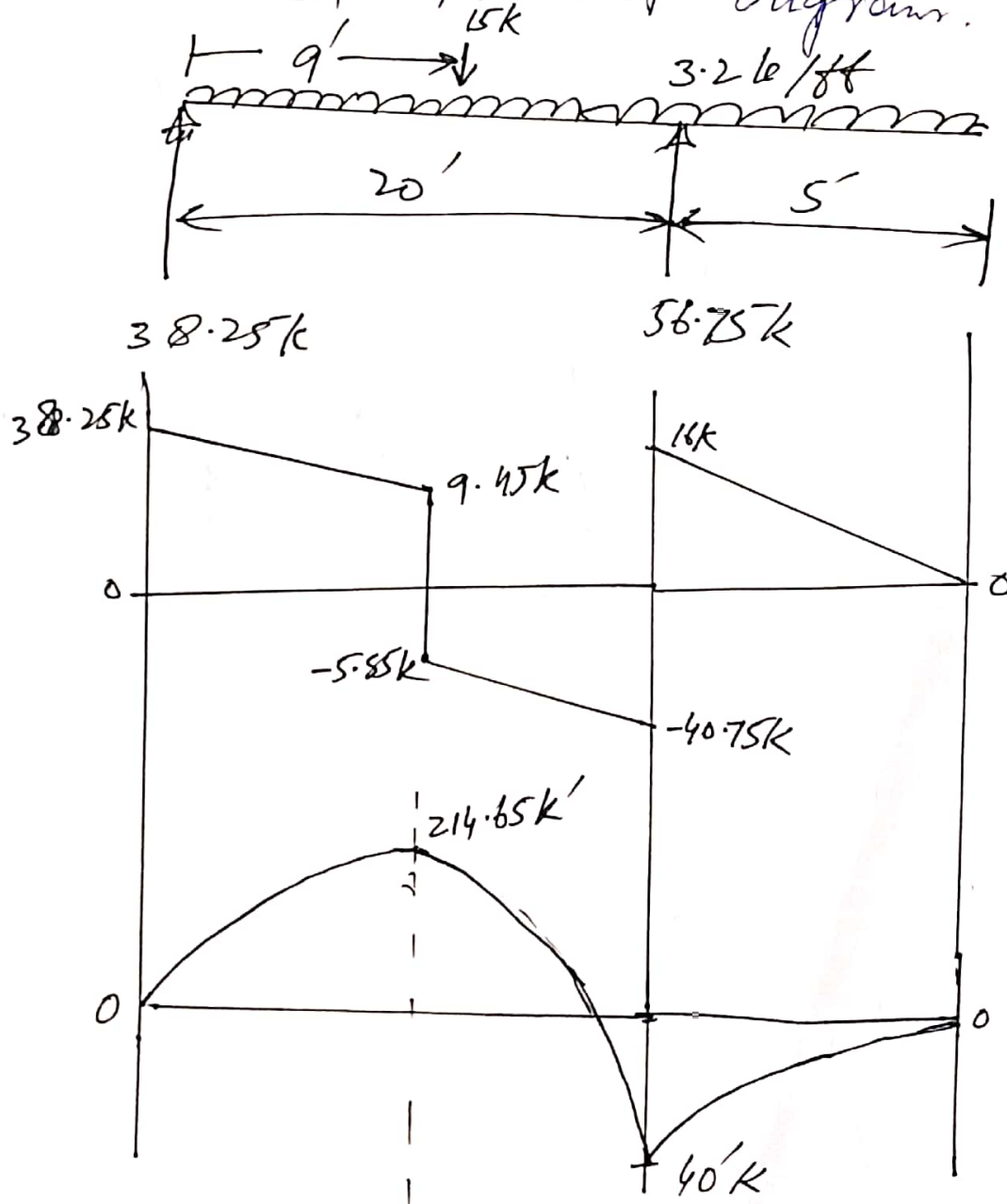
$$\sum F_y = 0 \quad \uparrow + \quad \underline{\underline{12}}$$

$$R_A + R_D = 15 + 3.2 \times 25 = 95$$

$$R_A = 95 - 56.75 = 38.25 \text{ k}$$

$$R_A = 38.25 \text{ k}$$

② Shear and moment diagrams.



### ③ Section Modulus - 13

$$I_{min} = \frac{M_{max}}{S_{all}} = \frac{214.65 \times 12}{19}$$

$$I_{min} = 135.5684 \text{ in}^3$$

referring to Appendix B, selecting

W 24 x 68 with  $S_x = 154 \text{ in}^3$  as  
a lightest section for the  
given beam.

④ Max. normal stress

$$\sigma_{max} = \frac{M_{max}}{S} = \frac{214.65 \times 12}{154}$$
$$\sigma_{max} = 16.73 \text{ ksi}$$

p.f.o

5

# Max shear stress

14

$$\tau_{max} = \frac{3}{2} \frac{V}{A}$$

$$V_{max} = 40.75 \text{ kips} \quad \text{from table}$$

$$A = 20.0 \text{ in}^2$$

$$\tau_{max} = \frac{3}{2} \times \frac{40.76}{20.0} = 3.06 \text{ ksi}$$

$$\tau_{max} = 3.06 \text{ ksi}$$

Q No of

Solutions

Given Data

(1)  $F = R = 15367 \text{ N}$

$E_{ult} = 207000 \text{ kpa}$

$E = 223 \times 10^6 \text{ kpa}$

$n = 0$

Factor of Safety  $N = 1$

$\alpha =$  1st two digits of  $R + 5 \text{ cm}$

$R = 15367$

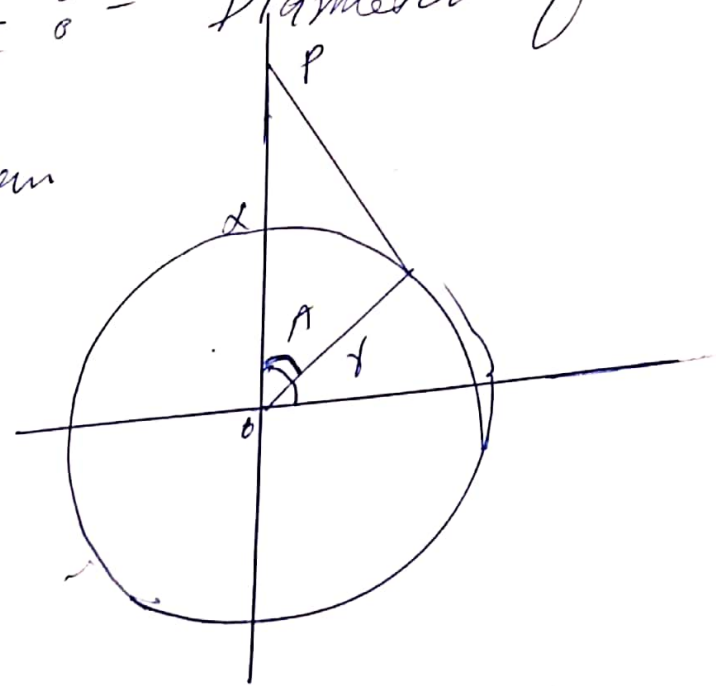
$\bar{X} = 15 + 5 = 20 \text{ cm}$

$\bar{Y} = 15 \text{ cm}$

Required

Diameter of the shaft

Diagram





$$M_c = \frac{\pi}{32} d (d_c)^3 \times S_b$$

$$d_c = \frac{M_c}{\frac{\pi}{32} d \times S_b}$$

$$\cancel{D_c} = M_c = K_1 \times b_2 =$$

$$83.83 \times 69.6 = \underline{5834.53 \text{ kN}\cdot\text{mm}}$$

$$d_c = \frac{5834.53}{\frac{\pi}{32} \times 3.1415} \times \frac{1}{103}$$

$$d_c = 89.46 \text{ mm} \quad \text{Say } \cancel{80} \text{ } 90 \text{ mm}$$

$D_c = 90 \text{ mm}$

Ans -