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Paper

Bio Statistics

Submitted to

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Questions

Pg 1

Question No 3

a) Ungroup:-

No of Children	No of women (F)	(C.F)	Tally:-
0	1	1	
1	4	5	
2	8	13	
3	11	24	
4	8	32	
5	5	37	
6	4	41	
7	3	44	
8	2	46	
9	1	47	
10	3	50	
Total	= 50		

B part

Group data

In this group we find out

1) frequency

2) C. frequency.

3) boundaries.

4) Class Mark

Solution:- finding class interval

$$n = 50$$

$$x_{\min} = 0$$

$$x_{\max} = 10$$

$$10 - 0 \div 5$$

$$10/5 = 2.$$

$$\text{Class Interval} = 2.$$

Classes	Enfours	frequency	c. frequency	Class Boundries	Mid Mark
0 - 2	2, 2, 2, 2. 0, 1, 1, 1, 1, 2, 2, 2, 2	13	13	0.5 - 2.5	1
3 - 5	3, 3, 3, 3, 3, 3, 3, 3, 3, 3 4, 4, 4, 4, 4, 4, 4, 4, 5, 5, 5, 5, 5.	24	37	2.5 - 5.5	4
6 - 8	4, 4, 4, 4, 7, 7, 7, 8, 8	9	46	5.5 - 8.5	7
9 - 11	9, 10, 10, 10.	4	50	8.5 - 11.5	10
Total		50			

Pg 3

a) Question No 1

Calculate the Correlation
b/w x & y .

x	3	4	5	6	7	8	9	10	11	13
y	25	24	20	20	19	17	16	13	10	8

Solution:-

Let us change the origin
of x & y .

So Hence,

$$u = x - 7 \quad \& \quad v = y - 19,$$

then

$$\delta xy = \delta uv$$

the calculation needed to
find r are given below.

x	y	u	v	u ²	v ²	uv
3	25	-4	6	16	36	-24
4	24	-3	5	9	25	-15
5	20	-2	1	4	1	-2
6	20	-1	1	1	1	-1
7	19	0	0	0	0	0
8	17	1	-2	1	4	-2
9	16	2	-3	4	9	-6
10	13	3	-6	9	36	-18
11	10	4	-9	16	81	-36
13	8	6	-11	36	121	-66
76	172	6	-18	96	314	-170

So Now,

We know that

$$r = \frac{\sum uv - (\sum u)(\sum v)}{n}$$

$$\sqrt{\left[\frac{\sum u^2 - (\sum u)^2}{n} \right] \left[\frac{\sum v^2 - (\sum v)^2}{n} \right]}$$

Putting the values.

$$r = \frac{-170 - (6)(-18)}{10}$$

$$\sqrt{\left[\frac{96 - (6)^2}{10} \right] \left[\frac{314 - (-18)^2}{10} \right]}$$

$$r = \frac{-170 + 108/10}{\sqrt{\left[96 - \frac{36}{10}\right] \left[314 - \frac{(324)}{10}\right]}}$$

$$\sqrt{\left[96 - \frac{36}{10}\right] \left[314 - \frac{(324)}{10}\right]}$$

$$r = \frac{-170 + 10.8}{\sqrt{(96 - 3.6)(314 - 32.4)}}$$

$$\sqrt{(96 - 3.6)(314 - 32.4)}$$

$$r = \frac{-159.2}{\sqrt{26019.84}}$$

$$\sqrt{26019.84}$$

$$r = \frac{-159.2}{161.30}$$

$$r = -0.98 \text{ Ans.}$$

B part

Given the following
Set of values.

x	20	11	15	10	17	18	21	25	28
y	5	15	14	17	8	9	12	16	18

Part (a)

Pg-7

a) Determine the equation of least square regression.

Solution:-

The necessary calculation for determining the equation of least square regression line are given below.

X	Y	X ²	Y ²	XY
20	5	100	25	100
11	15	121	225	165
15	14	225	196	210
10	17	100	289	170
17	8	289	64	136
18	9	324	81	162
21	12	441	144	252
25	16	625	256	400
28	18	784	324	504

The estimate linear regression line Y on X is

$$\hat{Y} = a + bx$$

(cont.... Q 1 part B (a).

where a and b are the least square estimate of β the parameter α and ϵ_i are respectively given by

As we know that.

$$b = \frac{n \sum xy - (\sum x)(\sum y)}{n \sum x^2 - (\sum x)^2} \text{ and}$$

$$a = \bar{y} - b\bar{x}$$

Substituting the sum, we get

Putting value.

$$b = \frac{(9)(2099) - (165)(114)}{(9)(3309) - (27225)}$$

$$b = \frac{18891 - 18810}{29781 - 27225}$$

$$b = \frac{81}{2556}$$

$$b = 0.031$$

Hence we know that

$$a = \bar{y} - b\bar{x}$$

putting values

$$a = \frac{114}{9} - 0.031 \left(\frac{165}{9} \right)$$

$$a = 12.66 - 0.568$$

$$a = 12.09$$

$$y = \boxed{12.09 + 0.031x}$$

Answer

The estimate linear regression line
x on y.

$$x = a + b\bar{y}$$

As we know that

$$b = \frac{n \sum xy - (\sum x)(\sum y)}{n(\sum xy) - (\sum y)^2}$$

Putting the values.

$$b = \frac{(9)(2099) - (165)(114)}{(9)(1604) - (114)^2}$$

$$b = \frac{18891 - 18810}{14436 - 12996}$$

$$b = \frac{81}{1440}$$

$$b = \boxed{0.056}$$

Hence

$$a = \bar{x} - b\bar{y}$$

$$a = \frac{165}{9} - (0.056)(\frac{114}{9})$$

$$a = 18.33 - 0.709$$

$$a = \boxed{17.62} \quad \text{Answers}$$

Part B:-

Solution:-

predicated value of
 Y 20, 11, 15, 25, 28.

The predicated values of y are found value by substituted the in the estimated equation.

Thus $x = \dots$

As we know that.

$$\bar{y} = 12.09 + 0.031(20)$$

$$\bar{y} = 12.09 + 0.62$$

$$\bar{y} = 12.71.$$

Cont -- Question 1(B) Pg 12.

$$\bar{y} = 12.09 + 0.031(11)$$

$$\bar{y} = 12.09 + 0.341$$
$$\bar{y} = 12.43$$

$$\bar{y} = 12.09 + 0.031(15)$$
$$\bar{y} = 12.09 + 0.465$$
$$\bar{y} = 12.55$$

$$\bar{y} = 12.09 + 0.031(25)$$
$$\bar{y} = 12.09 + 0.775$$
$$\bar{y} = 12.86$$

$$\bar{y} = 12.09 + 0.031(28)$$
$$\bar{y} = 12.09 + 0.86$$
$$\bar{y} = 12.95$$

* Predicted values.

$$x = 5, 15, 19, 12, 16, 18.$$

$$\bar{x} = 17.62 + 0.056$$

$$\bar{x} = 17.62 + 0.28$$

$$\bar{x} = 17.9$$

$$\bar{x} = 17.9$$

$$\bar{x} = 17.62 + 0.056(15)$$

$$\bar{x} = 17.62 + 0.84$$

$$\bar{x} = 18.46$$

$$\bar{x} = 17.62 + 0.056(9)$$

$$\bar{x} = 17.62 + 0.504$$

$$\bar{x} = 18.124$$

$$\bar{x} = 17.62 + 0.056(19)$$

$$\bar{x} = 17.62 + 0.50$$

$$\bar{x} = 18.1$$

Question :- 2

part (a)

tossing of a coin as an experiment we know that

(i) Each toss of a coin has two possible outcomes (head & tails).

(ii) The probability of the coin are tossed independently.

(iii) The successive tosses of the coin are independent.

(iv) The coin is tossed 5 times. x denotes the number of the heads.

The possible value of x are 0, 1, 2, 3, 4, 5.

Hence

$$\Rightarrow P = (\text{no head}) = P(X=0) \\ = \binom{5}{0} \left(\frac{1}{2}\right)^0 \left(\frac{1}{2}\right)^5 = 1 \left(\frac{1}{2}\right)^5 = \frac{1}{32}$$

$$\Rightarrow P = (1 \text{ head}) = P(X=1) = \binom{5}{1} \\ \left(\frac{1}{2}\right)^1 \left(\frac{1}{2}\right)^{5-1} = 5 \times \left(\frac{1}{2}\right)^5 = \frac{5}{32}$$

$$\Rightarrow P = (2 \text{ head}) = P(X=2) = \binom{5}{2} \\ \left(\frac{1}{2}\right)^2 \left(\frac{1}{2}\right)^{5-2} = 10 \times \left(\frac{1}{2}\right)^5 = \frac{10}{32}$$

$$\Rightarrow P = (3 \text{ head}) = P(X=3) = \binom{5}{3} \left(\frac{1}{2}\right)^3 \left(\frac{1}{2}\right)^{5-3} \\ = 10 \times \left(\frac{1}{2}\right)^5 = \frac{10}{32}$$

$$P = (4 \text{ head}) = P(X=4) = \binom{5}{4} \\ \left(\frac{1}{2}\right)^4 \left(\frac{1}{2}\right)^{5-4} = 5 \times \left(\frac{1}{2}\right)^5 = \frac{5}{32}$$

$$P = (5 \text{ head}) = \binom{5}{5} \left(\frac{1}{2}\right)^5 \left(\frac{1}{2}\right)^0 \\ 1 \times \left(\frac{1}{2}\right)^5 = \frac{1}{32}$$

The ^{pro} ~~probability~~ mobility distribution for the number of heads obtained in 5 tosses of a fair coin.

x	0	1	2	3	4	5
$f(x)$	$1/32$	$5/32$	$10/32$	$10/32$	$5/32$	$1/32$

Question 2 part B:-

Therefore the binomial distribution

$$n = 10$$

$$p = 2/3$$

$$q = 1 - p$$

$$q = 1 - 2/3$$

x denote the number of won by A. Then

$$(i) P(x \geq 4) = 1 - P(x < 4)$$

$$\begin{aligned}
 & 1 - \sum_{k=0}^3 \binom{10}{k} \left(\frac{2}{3}\right)^k \left(\frac{1}{3}\right)^{10-k} \\
 & \quad + 45 \left(\frac{2}{3}\right)^2 \left(\frac{1}{3}\right)^8 \\
 & \quad + 120 \left(\frac{2}{3}\right)^3 \left(\frac{1}{3}\right)^7 \\
 & 1 - \frac{1}{59049} [1 + 20 + 180 + 960] \\
 & 1 - 0.0197.
 \end{aligned}$$

$$P(x > 4) = 0.9803.$$

$$\begin{aligned}
 \text{(ii)} \quad P(x = 4) &= \binom{10}{4} \left(\frac{2}{3}\right)^4 \left(\frac{1}{3}\right)^6 \\
 &= 210 \left(\frac{16}{81}\right) \left(\frac{1}{729}\right)
 \end{aligned}$$

$$P(x = 4) = 6.056.$$

iii)

$P(x = 11) = f(0) =$ because
 x take only values
 $0, 1, 2, 3, 4, \dots, 10.$

(iv) 6 or more games

$$P(X=6) = \sum_{n=6}^{10} \binom{10}{n} \left(\frac{2}{3}\right)^n \left(\frac{1}{3}\right)^{10-n}$$

$$= \binom{10}{6} \left(\frac{2}{3}\right)^6 \left(\frac{1}{3}\right)^4 + \binom{10}{7}$$

$$\left(\frac{2}{3}\right)^7 \left(\frac{1}{3}\right)^3 + \binom{10}{8} \left(\frac{2}{3}\right)^8$$

$$\left(\frac{1}{3}\right)^2 + \binom{10}{9} \left(\frac{2}{3}\right)^9 \left(\frac{1}{3}\right)^1$$

$$+ \binom{10}{10} \left(\frac{2}{3}\right)^{10} \left(\frac{1}{3}\right)^0$$

$$= 0.228 + 0.261 + 0.196$$

$$+ 0.089 + 0.018$$

$$P(X \geq 6) = 0.79$$