

UMAR HADI

ID # 7974

Section 'B'

Subject # Fluid Mechanics

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①

QUESTION #01

Ans:-

Energy Head:-

"Energy head is the sum of all energy heads at the point in a fluid."

Forms OF ENERGY Head:-

There are various form of energy mentioned as follow.

- Kinetic Head.
- Potential Head.
- Pressure Head.

:Kinetic Head:

"Kinetic head is the kinetic energy per unit weight of the fluid."

2

Mathematical Form:

$$\frac{K.E}{\omega} = \frac{\frac{1}{2} m v^2}{m g}$$

$$\frac{K.E}{\omega} = \frac{1}{2} \frac{v^2}{g}$$

* "Kinetic head is also known as velocity Head".

: Unit:

"Meter" (m)

Potential Head:

"Potential head is the Potential energy per unit weight of the fluid"

Mathematically:

$$\frac{P.E}{\omega} = \frac{m g h}{m g} = h$$

3

Pressure Head:-

"The vertical height of the free surface above any point in a liquid at rest is called pressure head".

Other definition:

"Level of fluid due to pressure exerted by fluid"

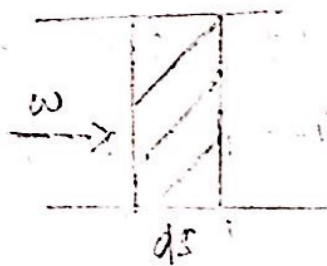
Mathematically:

$$= \frac{F \cdot ds}{w}$$

$$= \frac{P \cdot A \cdot ds}{w}$$

$$= \frac{P \cdot V}{w} = \frac{P}{\gamma}$$

Pressure head



is pressure.

④

(Part - b)

Ans:-

Hydraulic grade line:

"Hydraulic grade line refers to the profile of water streaming in an open channel or a pipe streaming in part full."

When a pipe is under pressure, the pressure driven review line is the level to which the water would ascend to in a little, vertical tube associated with the pipe

Equation of hydraulic grade line:

$$HGL = \frac{P}{\gamma} + z$$

⑤ Where, z is the height above the datum level and distance is $\frac{P}{\gamma}$.

⇒ EGL refer to a line that represent to the height of energy head of water streaming in a pipe, course, or channel. The line is drawn over the pressure hydraulic grade line (inclination) a separation equivalent to the speed head ($\frac{V^2}{2g}$) of water streaming at every area or point along the pipe/channel.

Equation of EGL:

$$EGL = h_0 = \frac{P}{\gamma} + \frac{V^2}{2g} + z$$

⇒ This equation of energy grade line:

→ The hydraulic grade line and energy grade line

Figure-'a' is shown as below.

6

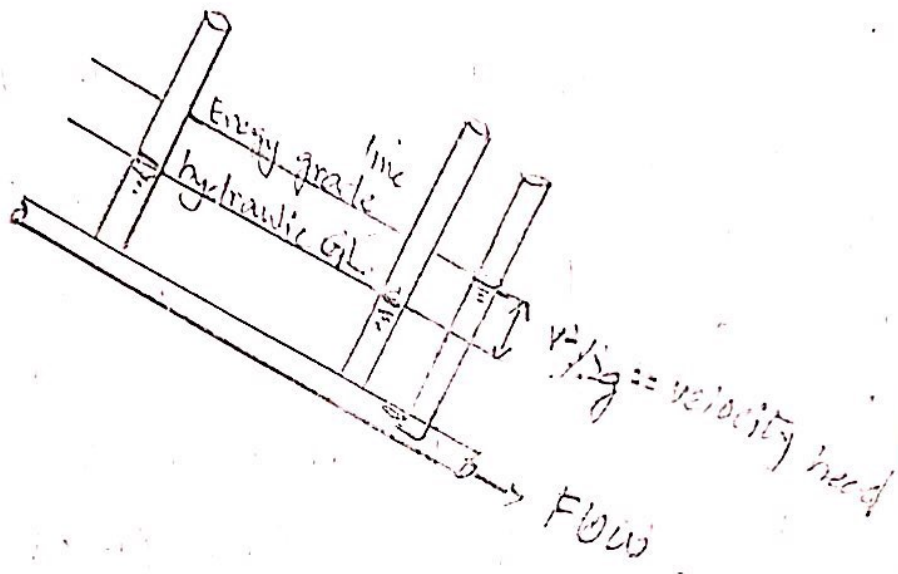


Figure : a1

7

QUESTION # 02

Solution :-

Given Data :-

$$\rightarrow \text{Velocity} = 2 \text{ m/s}$$

$$\rightarrow \text{Pressure} = 300 \text{ kPa} = 300 \times 10^3 \text{ N/m}^2$$

$$\rightarrow \text{datum} = z = 5 \text{ m}$$

$$\rightarrow H = \text{pressure head} + K.E + P.E$$

Required :-

"Total energy per unit weight of water = ?"

$$H = \frac{P}{\gamma} + \frac{V^2}{2g} + z$$

$$H = \frac{300 \times 10^3}{9810} + \frac{2^2}{2 \times 9.81} + 5$$

$$H = 30.58 + 0.101 + 5$$

$$H = 35.785 \text{ N/m/N}$$

8

(QUESTION # 02 Part-b)

A tapping pipe negligible

: Solution :

Given Data

$$\text{Pressure} = P_1 = 300 \text{ kPa} = 300 \times 10^3 \text{ N/m}^2$$

$$\text{Diameter, } d_1 = 300 \text{ mm} = 0.3 \text{ m}$$

$$\text{Diameter, } d_2 = 200 \text{ mm} = 0.2 \text{ m}$$

$$P_2 = 120 \text{ kPa} = 120 \times 10^3 \text{ N/m}^2$$

$$\text{Flow rate, } Q = \frac{4000}{1000} \text{ m}^3/\text{sec} = 0.04 \text{ m}^3/\text{sec}$$

Required:

$$\text{Datum} = z$$

Now Solution

We know that

$$A_1 = \frac{\pi d^2}{4}$$

9

$$= \frac{3.14 \times (0.3)^2}{4}$$

$$A_1 = 0.07065 \text{ m}^2$$

$$A_2 = \frac{\pi d_2^2}{4}$$

$$A_2 = \frac{3.14 \times (0.2)^2}{4}$$

$$A_2 = 0.0314 \text{ m}^2$$

Now As we know that

$$Q = V_1 A_1$$

$$V_1 = \frac{Q}{A_1}$$

$$V_1 = \frac{0.04}{0.0706}$$

$$V_1 = 0.5661 \text{ m/s}$$

10

And

$$V_2 = \frac{Q}{A_2}$$

$$V_2 = \frac{0.04}{0.0314}$$

$$V_2 = 1.2738 \text{ m/s}$$

Now

$$\frac{P_1}{\gamma} + \frac{V_1^2}{2g} + Z_1 = \frac{P_2}{\gamma} + \frac{V_2^2}{2g} + Z_2$$

where $Z_1 = 0$

$$\gamma = 9810$$

\Rightarrow Putting values

$$\frac{300 \times 10^3}{9810} + \frac{(0.566)^2}{2(9.81)} + 0 = \frac{120 \times 10^3}{9810} + \frac{(1.27)^2}{9810} + Z_2$$

$$\Rightarrow 30.598 = 12.314 + Z_2$$

$$Z_2 = 30.597 - 12.314$$

$$Z_2 = 18.282 \text{ m}$$

Hence $Z_2 = 18.282 \text{ m}$

11

QUESTION # 03

Ans.

⇒ GIVEN DATA:-

Length of pipe, $L = 500\text{m}$

Diameter, $d = 0.2\text{m}$

Specific gravity of oil = 0.9

Flow rate, $Q = 0.06\text{ m}^3/\text{s}$

Viscosity, $\mu = 6 \times 10^{-5}\text{ N s/m}^2$

Density, $\rho = 0.9 \times 1000 = 900\text{ kg/m}^3$

⇒ Required DATA:

Pressure loss, $\Delta P = ?$

⇒ Solution:

As we know that

$$\Rightarrow \gamma = \frac{H}{\rho}$$

$$\Rightarrow \gamma = \frac{6 \times 10^{-5}}{900}$$

(g)

$$\Rightarrow v = 6.67 \times 10^{-8} \text{ m}^2/\text{s}$$

Now we have to find "v"

$$v = \frac{Q}{A} \quad \text{--- (1)}$$

Now for circular pipe

$$A = \frac{\pi d^2}{4}$$

$$\Rightarrow A = \frac{3.14 (0.2)^2}{4}$$

$$\Rightarrow A = 0.0314 \text{ m}^2$$

Put value in eq (1)

$$v = \frac{0.06}{0.0314}$$

$$v = 1.91 \text{ m/s}$$

\Rightarrow Now we know that

$$R = \frac{v \times d}{\gamma}$$

$$R = \frac{1.91 \times 0.2}{6.67 \times 10^{-8}}$$

(12) (13)

$$R = 5.72 \times 10^6$$

Now

$$f = 0.0032 + \frac{0.221}{(5.72 \times 10^6)^{0.237}}$$

$$\Rightarrow f = 0.0032 + (5.532 \times 10^{-3})$$

$$\Rightarrow f = 8.73209 \times 10^{-3}$$

\Rightarrow : Now From Bernoulli's Equation:

$$\text{Head Loss, } HF = \frac{fLV^2}{2gD}$$

putting values

$$HF = \frac{fLV^2}{2gD}$$

$$= \frac{(8.73209 \times 10^{-3})(500)(1.91)^2}{2 \times (9.81)(0.2)}$$

(14) $HF = 4.0590$

⇒ Now we know by pressure loss and Head loss relation,

$$\Rightarrow h_f = \frac{\Delta P}{\rho g}$$

$$\Rightarrow h_f = \frac{\Delta P}{\rho g}$$

$$\Rightarrow \Delta P = h_f \rho g$$

$$\Rightarrow \Delta P = 4.0590 \times 9000 \times 9.81$$

$$\Rightarrow \Delta P = 35837.47 \text{ Pa}$$

$$\Rightarrow \Delta P = 35.837 \text{ kPa}$$

Result:

Hence pressure loss

$$\boxed{\Delta P = 35.837 \text{ kPa}}$$