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BE Civil

Section B

Q No 1 A Yarn - - - - -

$$u + 2y + z = 160$$

$$2u + y + z = 200$$

$$2u + 0y + 2z = 240$$

Ratios = 1:2:1, 2:1:1, 2:0:2

SOLUTION:

Since Ratio are

1:2:1, 2:1:1 & 2:0:2

of Pak, Egypt & America

Let

$$\frac{1}{4}u + \frac{2}{4}y + \frac{1}{4}z = 40$$

$$\Rightarrow \text{A } u + 2y + z = 160 \text{ --- (i)}$$

also

$$\frac{2}{4}u + \frac{1}{4}y + \frac{1}{4}z = 50$$

~~2u + y + z = 200~~

$$2u + y + z = 200 \text{ --- (ii)}$$

Now

$$\frac{2x}{4} + \frac{0y}{4} + \frac{2z}{4} = 60$$

$$2x + 2y = 240 \quad \text{--- (3)}$$

$$x + 0y + z = 120 \quad \text{--- (4)}$$

Now from i, ii & iv

$$\begin{bmatrix} 1 & 2 & 1 \\ 2 & 1 & 1 \\ 1 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 120 \\ 240 \\ 120 \end{bmatrix}$$

$$Ax = b$$

By Cramer's Rule

$$A = \begin{bmatrix} 1 & 2 & 1 \\ 2 & 1 & 1 \\ 1 & 0 & 1 \end{bmatrix}$$

$$|A| = 1 - 2(2-1) + 1(0-1)$$

$$|A| = -2$$

$$k = \frac{|Au|}{|A|}$$

$$Au = \begin{bmatrix} 160 & 2 & 1 \\ 200 & 1 & 1 \\ 120 & 0 & 1 \end{bmatrix} \quad |Au| =$$

$$|Au| = -120$$

$$k = \frac{-120}{-2} = 60$$

$$y = \frac{|Ay|}{|A|}$$

$$Ay = \begin{bmatrix} 1 & 160 & 1 \\ 2 & 200 & 1 \\ 1 & 120 & 1 \end{bmatrix}$$

$$|Ay| = -40$$

$$y = \frac{-40}{-2} = 20$$

$$z = \frac{|A_2|}{|A|}$$

$$A_2 = \begin{bmatrix} 1 & 2 & 160 \\ 2 & 1 & 200 \\ 1 & 0 & 220 \end{bmatrix}$$

$$|A_2| = -120$$

$$z = \frac{|A_2|}{|A|} = \frac{-120}{-2} = 60$$

Value of $x, y, z = (60, 20, 60)$ and

these are value of cotton in

Pakistan, Egypt and America respectively

①

Q No 2 (i)

$$\frac{dy}{dx} = \frac{x^3 + y^3}{x^2y + xy^2}$$

SOLUTION:

$$= \frac{x^3 + y^3}{x^2y + xy^2} \rightarrow \text{① homogenous}$$

Let

$$y = vx \quad y/x = v$$

Diff w.r.t x

$$\frac{dy}{dx} = v \cdot 1 + x \frac{dv}{dx}$$

$$= v + x \frac{dv}{dx}$$

$$v + x \frac{dv}{dx} = \frac{x^3 + v^3x^3}{x^2vx + xv^2x^2}$$

$$= \frac{x^3 + v^3x^3}{x^3v + x^3v^2} = \frac{x^3(1+v^3)}{x^3(v+v^2)}$$

(2)

$$V + u \frac{dv}{du} = \frac{1+V^3}{V+V^2}$$

$$\frac{u dv}{du} = \frac{1+V^3}{V+V^2} - V$$

$$= \frac{1+V^3 - V(V+V^2)}{V+V^2}$$

$$= \frac{1+V^3 - V^2 - V^3}{V+V^2}$$

$$= \frac{1-V^2}{V+V^2} = \frac{(1-V)(\cancel{1+V})}{V(\cancel{1+V})}$$

$$u \frac{dv}{du} = \frac{1-V}{V}$$

Separating Variable

$$\frac{V}{1-V} dv = \frac{du}{u}$$

(3)

$$- \frac{v}{v-1} dv = \frac{du}{u}$$

$$\frac{v}{v-1} = - \frac{du}{u}$$

integrating b.s

$$\int \frac{v}{v-1} = - \int \frac{du}{u}$$

$$\int \left(\frac{v-1+1}{v-1} + \frac{1}{v-1} \right) dv = -\ln u + \ln c$$

$$\Rightarrow \int \left(1 + \frac{1}{v-1} \right) dv = \ln c - \ln u$$

$$\int 1 dv + \int \frac{1}{v-1} dv = \ln c - \ln u$$

$$v + \ln(v-1) = \ln c - \ln u$$

$$y/u + \ln |y/u - 1| = \ln c - \ln u$$

$$y^u = \ln(y^u - 1) = \ln y^u \quad (4)$$

QNO 2(b)

$$(y - u + 5) dy = (y - u + 1) du$$

SOLUTION:

$$\begin{aligned} \frac{dy}{du} &= \frac{y - u + 1}{y - u + 5} \\ &= \frac{-u + y + 1}{-u + y + 5} \quad \text{--- (1)} \end{aligned}$$

$$\frac{a_1}{a_2} = \frac{-1}{-1} = 1, \quad \frac{b_1}{b_2} = \frac{1}{1} = 1$$

Put $z = -u + y$

Diff w.r.t u

$$\frac{dz}{du} = -1 + \frac{dy}{du}$$

$$\frac{dz}{du} + 1 = \frac{z+1}{z+5} \quad (5)$$

(1) \Rightarrow

$$\frac{dz}{du} + 1 = \frac{z+1}{z+5}$$

$$\frac{dz}{du} = \frac{z+1}{z+5} - 1$$

$$= \frac{z+1 - (z+5)}{z+5}$$

$$\frac{\cancel{z}+1 - \cancel{z}-5}{z+5}$$

$$\frac{dz}{du} = \frac{-4}{z+5}$$

Separating variable

(6)

$$(z+s)dz = -4du$$

integrating bs

$$\int (z+s)dz = -4 \int du$$

$$\int z dz + s \int dz = -4u + c$$

$$\frac{z^2}{2} + sz = -4u + c$$

$$\frac{(-u+y)^2}{2} + s(-u+y) = -4u + c$$

$$\frac{(y-u)^2}{2} - su + sy + 4u = c$$

$$\frac{y^2 + u^2 - 2uy}{2} - \frac{u}{1} + \frac{sy}{1} = c$$

$$\frac{u^2 + y^2 - 2uy - 2u + 2sy}{2} = c$$

$$u^2 + y^2 - 2uy - 2u + 2sy = 2c$$