

Name :- Zulkifal  
ID :- 13856  
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Submitted to :- "Sir Anwar  
Shamim"

Q.1 (a)

S.no	x	y	$x_i - \bar{x}$	$(y_i - \bar{y})^2$	$(2x)_i$	$(2y)_i$	$(2x)_i(2y)_i$
1	3	25	2.46	6.084	-1.44	1.39	-2.00
2	4	24	12.98	46.24	<del>-0.13</del>	1.21	-1.36
3	5	20	6.78	7.84	-0.81	0.5	-0.40
4	6	20	2.56	7.84	-0.5	0.5	-0.25
5	7	19	0.36	3.24	-0.19	0.32	-0.06
6	8	17	0.11	0.04	0.11	-0.03	-0.003
7	9	16	1.96	1.44	0.44	-0.21	-0.009
8	10	13	5.76	17.64	0.75	-0.75	0.56
9	11	10	11.56	51.84	1.06	-1.29	-1.36
10	13	8	29.16	84.64	1.67	-1.64	-2.73

$\bar{x} = 7$   $\sum x = 77.4$   $\sum x^2 = 3.21$   $\sum y = 56$

$\sum = -881$

$$S_x = \sqrt{\frac{\sum (x_i - \bar{x})^2}{n-1}} = \sqrt{10.2} = 3.2$$

$$S_y = \sqrt{\frac{\sum (y_i - \bar{y})^2}{n-1}} = \sqrt{31.29} = 5.6$$

$$(2x)_i = \frac{\sum (x_i - \bar{x})}{S_x}$$

$$(2y)_i = \frac{\sum (y_i - \bar{y})}{S_y}$$

$$r = \frac{\sum (2x)_i (2y)_i}{n-1} = \frac{-881}{9}$$

$$r = 0.978$$

Part B Question no 1

S.No	x	y	$x^2$	$xy$
1	20	5	400	100
2	11	16	121	176
3	15	14	225	210
4	10	17	100	170
5	17	8	289	136
6	18	9	324	162
7	21	12	441	252
8	25	16	625	400
9	28	18	784	504

$\Sigma x = 165$     $\Sigma y = 114$     $\Sigma x^2 = 2699$     $\Sigma xy = 2099$

a) For y on x

$y = mx + b \rightarrow (A)$

$$m = \frac{N \Sigma(xy) - \Sigma x \Sigma y}{N \Sigma(x^2) - (\Sigma x)^2}$$

$$\Rightarrow \frac{9 \times 2099 - 165 \times 114}{9 \times 2699 - 27225} = \frac{18891 - 19810}{42291 - 27225}$$

$$m = \frac{81}{-2934} = -0.027$$

For b

$$b = \frac{\Sigma y - m \Sigma x}{N} = \frac{114 - (-0.027)(165)}{9}$$

$$b = 118.45$$

Now eq A becomes

$$y = mx + b$$

$$y = 0.027x + 118.45$$

For x on y

$$y = mx + b$$

$$x = \frac{y - b}{m}$$

$$x = \frac{y - 118.45}{-0.027}$$

Q No 2 (Part-A)

A fair coin is tossed 5 times. Find the probability of obtaining various numbers of heads.

Ans

- Let us regard the tossing of coin as an experiment. Then we observe that:
- i) Each toss can have two possible outcomes head and tail.
  - ii) The probability of a head success is  $p = \frac{1}{2}$
  - iii) The successive tosses of the coin are independent.
  - iv) The coin is tossed 5 times.

Therefore the r.v.  $x$ , which denotes the number of heads (successes) has a binomial probability distribution with  $p = \frac{1}{2}$  and  $n = 5$  the possible values of  $x$  are 0, 1, 2, 3, 4 and 5 hence.

$$P(\text{no head}) = P(x=0) = \binom{5}{0} \left[\frac{1}{2}\right]^0 \left[\frac{1}{2}\right]^{5-0} = 1 \times \left[\frac{1}{2}\right]^5 = \frac{1}{32}$$
$$P(1 \text{ head}) = P(x=1) = \binom{5}{1} \left[\frac{1}{2}\right]^1 \left[\frac{1}{2}\right]^{5-1} = 5 \times \left[\frac{1}{2}\right]^5 = \frac{5}{32}$$
$$P(2 \text{ head}) = P(x=2) = \binom{5}{2} \left[\frac{1}{2}\right]^2 \left[\frac{1}{2}\right]^{5-2} = 10 \times \left[\frac{1}{2}\right]^5 = \frac{10}{32}$$
$$P(3 \text{ head}) = P(x=3) = \binom{5}{3} \left[\frac{1}{2}\right]^3 \left[\frac{1}{2}\right]^{5-3} = 10 \times \left[\frac{1}{2}\right]^5 = \frac{10}{32}$$
$$P(4 \text{ head}) = P(x=4) = \binom{5}{4} \left[\frac{1}{2}\right]^4 \left[\frac{1}{2}\right]^{5-4} = 5 \times \left[\frac{1}{2}\right]^5 = \frac{5}{32}$$
$$P(5 \text{ head}) = P(x=5) = \binom{5}{5} \left[\frac{1}{2}\right]^5 \left[\frac{1}{2}\right]^0 = 1 \times \left[\frac{1}{2}\right]^5 = \frac{1}{32}$$

These probabilities can also be obtained by expanding the binomial  $(\frac{1}{2} + \frac{1}{2})^5$ . The binomial p.d for the number of head obtained in 5 tosses of fair coin is.

$x$	0	1	2	3	4	5
$f(x)$	$\frac{1}{32}$	$\frac{5}{32}$	$\frac{10}{32}$	$\frac{10}{32}$	$\frac{5}{32}$	$\frac{1}{32}$

Part B (Question no 2)

Therefore the binomial probability list with  $n=10$

$$p = 2/3$$

$$q = 1-p$$

$$q = 1 - 2/3$$

$$q = 1/3$$

Let  $x$  denote the number of by  
A then

$$i) P(x > 4) = 1 - P(x < 4)$$

$$= 1 - \sum_{x=0}^3 \binom{10}{x} \left(\frac{2}{3}\right)^x \left(\frac{1}{3}\right)^{10-x}$$

$$= 1 - \left[ \left(\frac{1}{3}\right)^{10} + 10 \left(\frac{2}{3}\right)^1 \left(\frac{1}{3}\right)^9 + 45 \left(\frac{2}{3}\right)^2 \left(\frac{1}{3}\right)^8 + 120 \left(\frac{2}{3}\right)^3 \left(\frac{1}{3}\right)^7 \right]$$

$$= 1 - \frac{1}{59049} [1 + 20 + 180 + 960]$$

$$\frac{1 - 0.0197}{P(x > 4) = 0.9803}$$

$$ii) P(x=4) = \binom{10}{4} \left(\frac{2}{3}\right)^4 \left(\frac{1}{3}\right)^6$$

$$= 210 \left(\frac{16}{81}\right) \left(\frac{1}{729}\right)$$

$$= \frac{3360}{59049} \Rightarrow \boxed{P(x=4) = 0.056}$$

iii)  $P(x=11) = f(0) =$  because  $x$  can only take values  $0, 1, 2, 3, \dots, 9, 10$

iv) 6 or more

$$P(x \geq 6) = \sum_{x=6}^{10} \binom{10}{x} \left(\frac{2}{3}\right)^x \left(\frac{1}{3}\right)^{10-x}$$

$$= \binom{10}{6} \left(\frac{2}{3}\right)^6 \left(\frac{1}{3}\right)^4 + \binom{10}{7} \left(\frac{2}{3}\right)^7 \left(\frac{1}{3}\right)^3 + \binom{10}{8} \left(\frac{2}{3}\right)^8 \left(\frac{1}{3}\right)^2 + \binom{10}{9} \left(\frac{2}{3}\right)^9 \left(\frac{1}{3}\right)^1 + \binom{10}{10} \left(\frac{2}{3}\right)^{10} \left(\frac{1}{3}\right)^0$$

$$P = 0.228 + 0.261 + 0.196 + 0.087 + 0.018$$

$$\boxed{P(x \geq 6) = 0.79}$$

b) Predictive values

for  $x = 20, 11, 15, 25, 28$

$$x = 20$$

$$y = mx + c = 0.027(20) + (118.45) = 117.94$$

$$x = 11$$

$$y = (0.027)(11) + 118.45 = 118.15$$

$$x = 15$$

$$y = 118.04$$

$$x = 25$$

$$y = 117.77$$

$$x = 28$$

$$y = 117.69$$

Given data

1	6	1	5	4	3	3	8	10	1
4	3	3	0	5	2	1	4	10	3
5	3	3	6	3	3	2	2	7	4
1	4	2	4	4	4	6	8	10	7
7	5	6	3	3	2	3	9	2	2

Ungrouped frequency distribution

un-grouped women	Tally	frequency	No
0		1	0
1		4	1
2		8	2
3		11	3
4		8	4
5		5	5
6		4	6
7		3	7
8		2	8
9		1	9
10		3	10
		50	

Question No 3 Part B

2	6	1	5	4	3	3	8	10	1
4	3	3	0	5	2	1	4	3	3
5	3	3	6	3	3	2	2	10	4
1	4	2	4	4	4	6	8	7	7
7	5	6	5	3	2	3	9	10	2

Ungrouped frequency distribution for given data

$$N = 50 \quad x_0 = 1, \quad x_m = 10$$

$$R = x_m - x_0$$

$$R = 10 - 1 = 9$$

$$K = 1 + 3.3 \log N = 1 + 3.3 \log (50) = 1 + 3.3(1.698)$$

$$K = 1 + 5.6066 = 6.6066 = 6$$

$$n = \text{Class interval} = \text{Range} / K$$

$$n = 9 / 6 = 1.5 = 2$$

we find out the information from data

classes	frequency	class boundary	Mid point
0-1	5	0.5-1.5	1
2-3	19	1.5-3.5	2.5
4-5	13	3.5-5.5	4.5
6-7	7	5.5-7.5	6.5
8-9	3	7.5-9.5	8.5
10-11	3	9.5-10.5	11