

FINAL TERM EXAM:

SUBMITTED FO:-

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Roll NO:

79 56

SECTION:-

B

Paper:

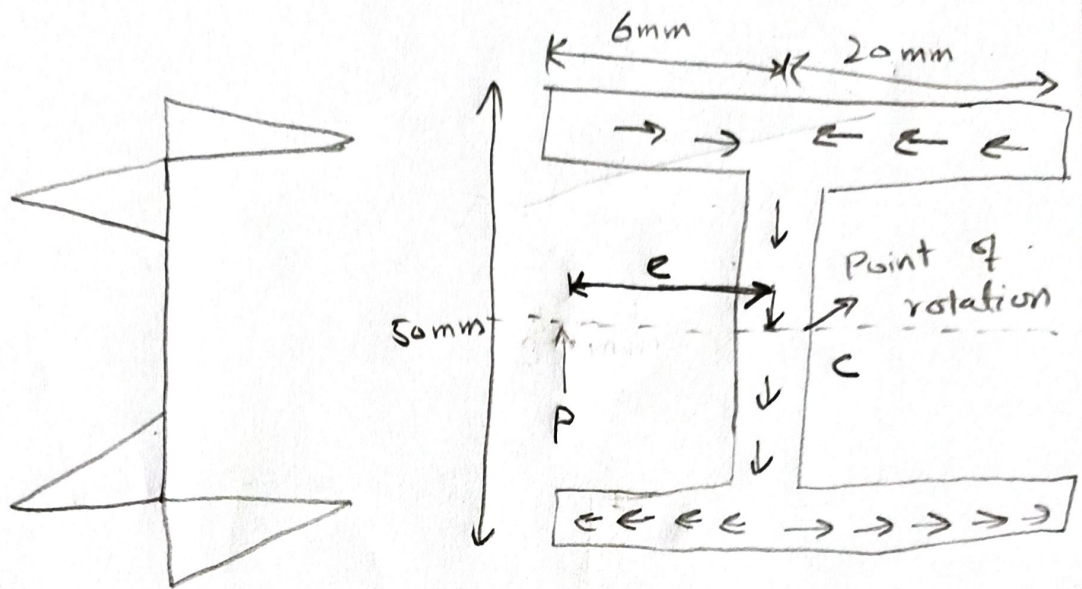
TMOS-II

Department:- CIVIL ENGG.

Q: No: 01

Part (a)

CLO: 2



→ The section is symmetrical about x -axis & not y -axis

So, any external force on section will create twisting in the section.

So in order to avoid twisting we will find out plane where external load will balance, the internal shear flow in the section.

→ As the section is symmetrical only about u-axis the shear center must lie somewhere on u-axis

→ Clockwise moment = Anticlockwise moment

$$V_{xe} + f_f \times 50 = f_f \times 50$$

$$e = \frac{f_f \times 50 - f_f \times 50}{V}$$

Now we will find out I_x and I_y

$$I = \sum (\bar{I} + Ad^2)$$

$$I = 2 \left[\frac{26 \times 2^3}{12} + 26 \times 2 \times (25-1)^2 \right] + \left[\frac{2 \times 50^3}{12} + 0 \right]$$

$$I_{xx} = 59938.66 + 20833.34$$

$$I = 80771.99 \text{ mm}^4$$

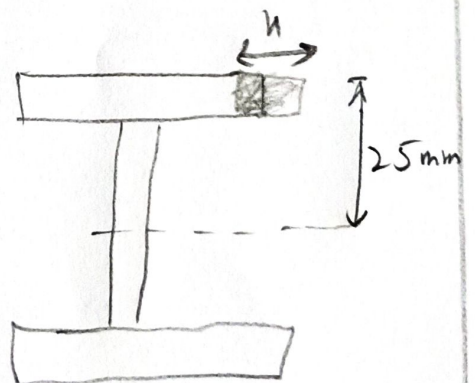
$$\Sigma y = 25 \text{ mm}$$

Now for flange

$$F_f = \int_0^u q_f dx$$

$$= \int_0^u \frac{VQ}{I} du$$

$$= \int_0^u \frac{V \times 50}{80772.9} dx$$



$$\frac{25V}{40386} \int_0^u u \cdot du$$

$$F_f = \frac{25V}{40386} \left| \frac{u^2}{2} \right|_0^u$$

$$\begin{aligned} & \left(\frac{1}{2} \right) A \bar{y} \\ & (2 \times u) \times 25 \\ & = 50u \\ & \text{eq (2)} \end{aligned}$$

Now for $n = 20$ (from right side)

$$F_f = \frac{25V}{40386} \left(\frac{20^2}{2} - 0 \right)$$

$$F_f = 0.123V$$

From left side

$$n = 6$$

eq (2)

$$F_f = \frac{25V}{40386} \left[\frac{n^2}{2} \right]_0^6$$

$$f_f = \frac{25V}{40386} \left(\frac{6^2}{2} - 0 \right)$$

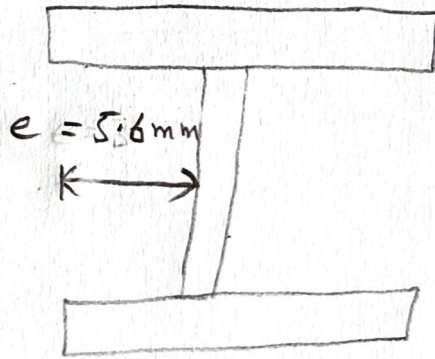
$$f_f = 0.011V$$

Now putting value in eq (1)

$$e = \frac{-0.011V \times 50 + 0.123 \times 50}{V}$$

$$e = 5.6 \text{ N/A}$$

$$e = 5.6 \text{ mm}$$



Question No. 01

Part: "B" (CLO 2)

Given data:

Circumferential stress = $\sigma_c \leq 6000 \text{ psi}$

$$\gamma = 62.4 \text{ lb/ft}^3$$

$$D = 22 \text{ ft}$$

$$\text{Height} = 26 \text{ ft}$$

Required:

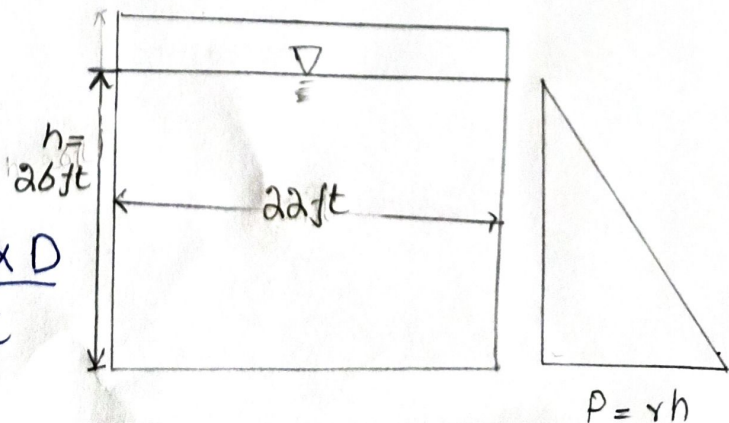
Determine the thickness of the wall of a water tank = ?

Solution:

As we know that the

Pressure developed by water = $P = \gamma h$

$$\sigma_c = \frac{PD}{2t}$$
$$\sigma_c = \frac{\gamma h \times D}{2t}$$



$$t = \frac{\gamma h \times D}{\alpha \times \sigma_c}$$

$$t = \frac{(62.4 \times 26) \times 22}{\alpha \times (6000 \times 12^2)} = 0.02 \text{ ft} = 0.24 \text{ inches}$$

Question No: 02

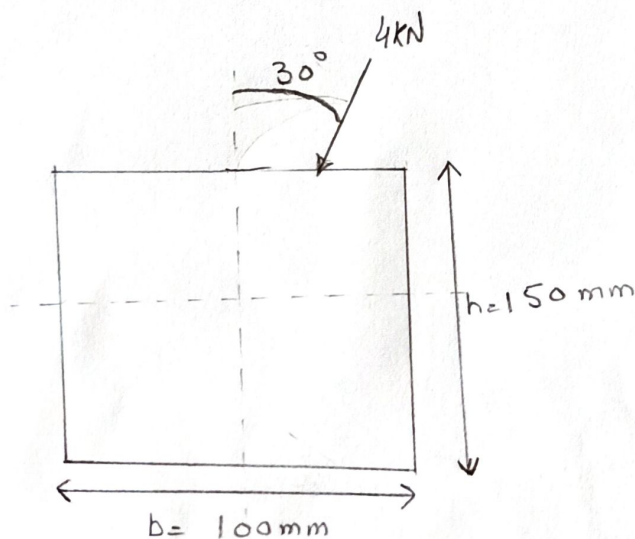
Part (a) (CLO-3)

Given data:

$$W = 4 \text{ kN}$$

$$L = 3 \text{ m}$$

$$\theta = 30^\circ$$

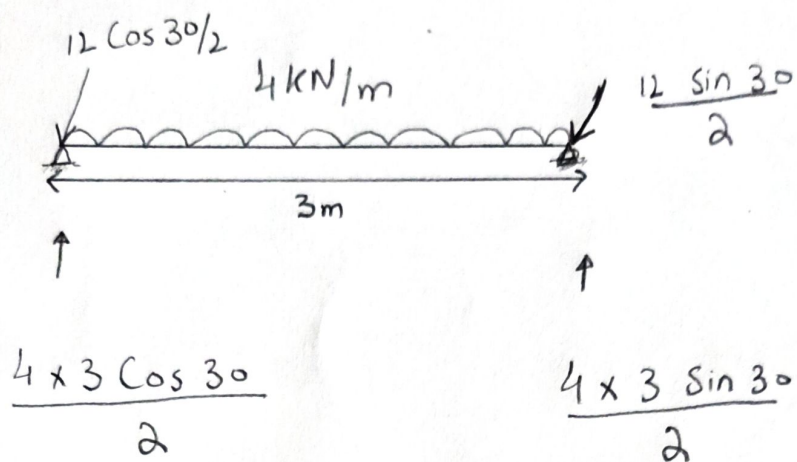


Required:

a) Max bending stresses at mid span = ?

b) Locate neutral axis = ?

Solution:



For UDL max moment M_{max} at mid section.

$$M_z = \frac{WL}{2} \times \frac{L}{4} = \frac{WL^2}{8}$$

$$M_z = \frac{4 \cos 30 \times 3^2}{8} = \boxed{3.9 \text{ kN/m}}$$

Now for M_y

$$M_y = \frac{4 \sin 30 \times 3^2}{8}$$

$$M_y = 2.25 \text{ kN}\cdot\text{m} \rightarrow \boxed{2.25 \text{ kN}\cdot\text{m}}$$

$$I_y = \frac{0.150 \times 0.1^3}{12} = 1.25 \times 10^{-5} \text{ m}^4$$

$$I_z = \frac{0.100 \times 0.150^3}{12} = 2.81 \times 10^{-5} \text{ m}^4$$

As we know that total bending stress at mid span

$$\sigma_c = \frac{M_z}{I_z} y + \frac{M_y}{I_y} z$$

$$y = 0.075 \text{ m} \quad z = 0.05 \text{ m}$$

$$I_z = 2.81 \times 10^{-5} \text{ m}^4, \quad I_y = 1.25 \times 10^{-5} \text{ m}^4$$

$$\sigma_z = \frac{M_z y}{I_z}$$

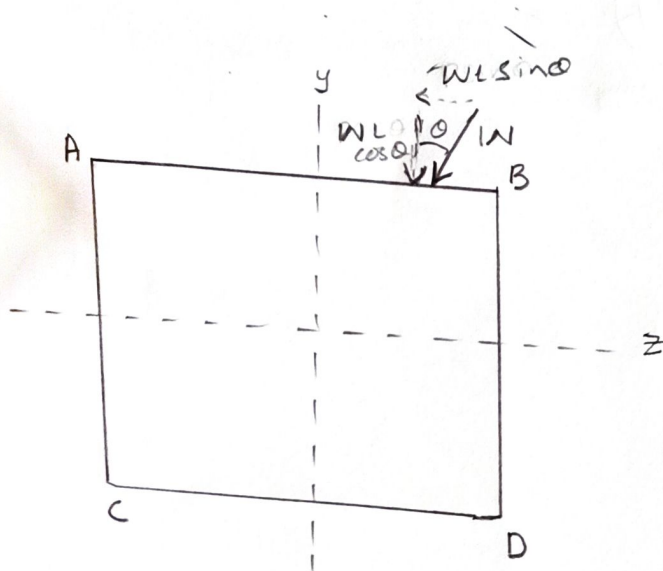
$$\sigma_z = \frac{3.9 \times 0.075}{2.81 \times 10^{-5}}$$

$$\sigma_z = 10409.25 \text{ KN/m}^2$$

$$\sigma_y = \frac{M_y z}{I_y}$$

$$\sigma_y = \frac{2.25 \times 0.05}{1.25 \times 10^{-5}}$$

$$\sigma = 9000 \text{ KN/m}^2$$



Maximum bending stress at the extreme fiber.

$$\sigma_A = -\sigma_z + \sigma_y$$

$$\sigma_B = -\sigma_z - \sigma_y$$

$$\sigma_C = +\sigma_z + \sigma_y$$

$$\sigma_D = -\sigma_z - \sigma_y$$

Note $\rightarrow \sigma_z = 10409.25 \text{ KN/m}^2$

$$\sigma_y = 9000 \text{ KN/m}^2$$

Now Max. Bending Stresses:

$$\sigma_A = -10409.25 + 9000 = \overset{\text{Compression}}{(-1409.25 \text{ KN/m}^2)}$$

$$\sigma_B = -10409.25 + (-9000) = \overset{\text{Compression}}{(-1940.25 \text{ KN/m}^2)}$$

$$\sigma_C = 10409.25 + 9000 = \overset{\text{Tension}}{(1940.25 \text{ KN/m}^2)}$$

$$\sigma_D = 10409.25 + (-9000) = \overset{\text{Tension}}{(1409.25 \text{ KN/m}^2)}$$

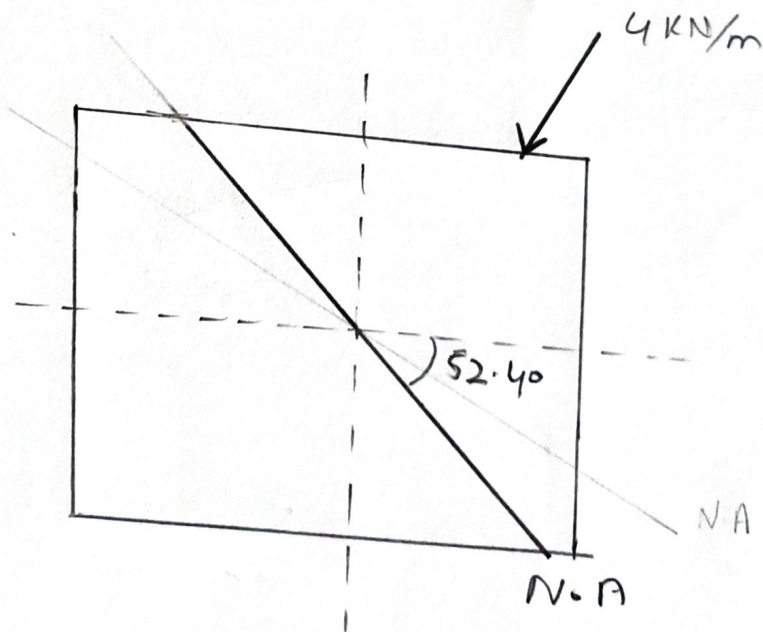
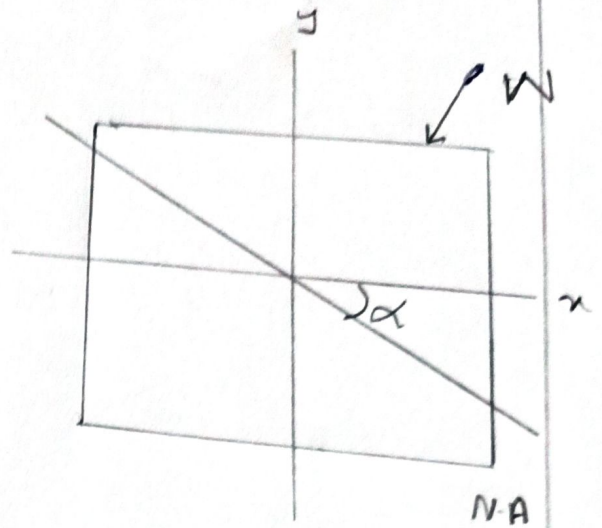
Location of neutral axis:

$$\tan \alpha = \frac{I_z}{I_y} \times \tan \theta$$

$$\tan \alpha = \frac{2.81 \times 10^5}{1.25 \times 10^5} \times \tan 30$$

$$\tan \alpha = 1.29$$

$$\alpha = 52.40$$



Question No. 02 Part (b) CLO. 3

Given data:

$$\bar{y} = 3.07 \text{ in}$$

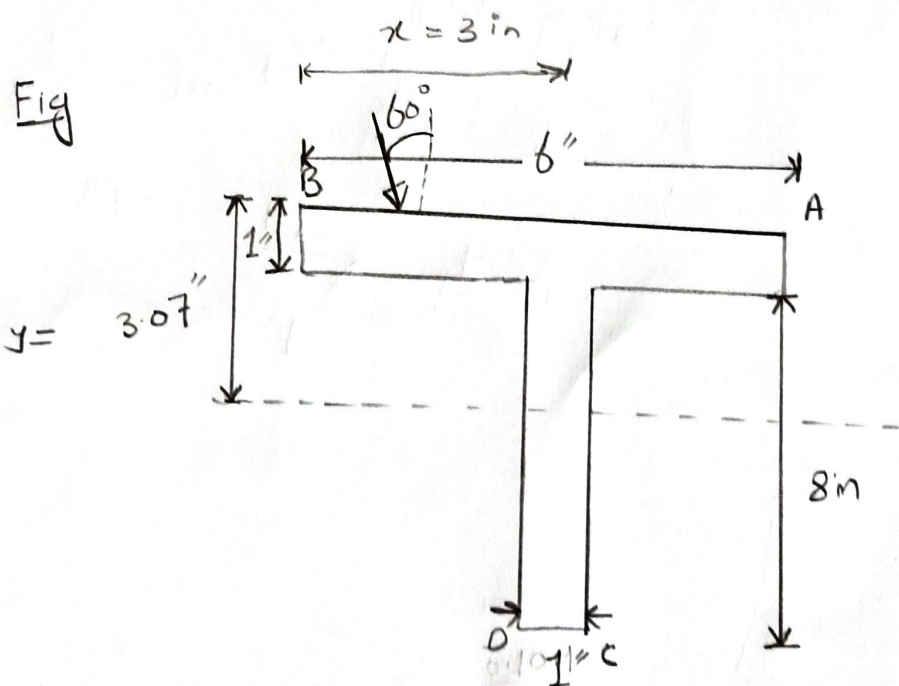
$$x = 3 \text{ in}$$

$$I_x = 112.6 \text{ in}^4$$

$$I_y = 18.7 \text{ in}^4$$

Compressive stress $\leq 12000 \text{ psi}$

Tensile stress $\leq 5000 \text{ Psi}$



Required:

Max load that will not overstress the beam.?

2

Solution:

The maximum bending stresses occur at the mid section due to the maximum bending moment, so that the critical section is the mid section where the compressive and tensile stresses can exceed the limiting values.

" We also know that at any given section the maximum stress occur at the extreme fiber. For example point A, B, C, D.

We know that for point load at mid section is;

$$M = \frac{PL}{4}$$

$$M_x = \frac{P \cos 60 \times 16 \times 12}{4} = \underline{\underline{24P}}$$

$$M_y = \frac{P \sin 60 \times (16 \times 12)}{4}$$

$$M_y = 41.57 P$$

Stresses at point A, B, C and D

Point A:

$$\begin{aligned} \sigma_z &= \frac{M_x y}{I_x} + \frac{M_y x}{I_y} \\ &= -\frac{24 \times 3.07}{112.6} + \frac{41.57 \times 3}{18.7} \end{aligned}$$

$$= -0.654 + 6.667$$

$$\sigma_z = 6.014 \text{ (Tension)}$$

δ Tension ≤ 5000 psi

$$P = \frac{5000}{6.014} = 831.94 \text{ lb}$$

For point B.

$$\sigma_B = \frac{M_x y}{I_x} + \frac{M_y x}{I_y}$$

$$\sigma_B = -0.554 + (-6.667)$$

$$\sigma_B = -7.231 \text{ (Compression)}$$

∴ Compression ≤ 12000 psi

$$P = \frac{12000}{7.231}$$

$$P = 1659.52$$

So, Controlling value b/w A & B is

$$831.94 \text{ lb}$$

for point "C"

$$\sigma_c = 0.654 + 6.667$$

$$\sigma_c = 7.321 \rightarrow \text{Tension}$$

$$\Sigma \text{Tension} \leq 5000 \text{ psi}$$

$$P = \frac{5000}{7.321}$$

$$7.321$$

$$P = 682.97 \text{ lb}$$

for point "D"

$$\sigma_D = -\cancel{7.321} + 0.654 + (-6.667)$$

$$\sigma_D = -\cancel{7.321}$$

$$\sigma_D = -6.013 \text{ (Compression)}$$

$$\Sigma \text{Compression} \leq 12000$$

$$P = \frac{12000}{6.013}$$

$$6.013$$

$$P = 1995.67 \text{ lb}$$

So, Controlling value b/w C, D is

$$682.97 \text{ lb}$$

Q: No: 3 : CLO:3

Given data:

$$L = 10 \text{ ft}$$

$$E = 10.3 \times 10^6 \text{ psi}$$

$$\text{Factor of safety} = 2$$

$$n = 2 \text{ (Center, braced)}$$

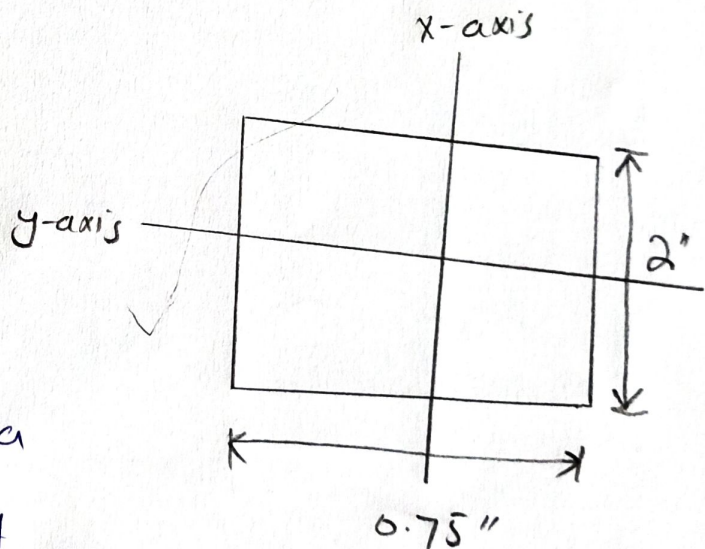
Strut is a compression member act as a column.

Required:

P_{safe} ?

Solution:

Case: 01



Strut act as a hinge column about an axis perpendicular to the 2 in dimension.

$$I_x = \frac{bh^3}{12} \Rightarrow \frac{0.75 \times 2^3}{12}$$

$$I_x = 0.5 \text{ in}^4$$

As we know that

$$P_{cr} = \frac{n^2 EI \pi^2}{L_e^3}$$

For hinged ended column $L_e = L$

$$P_{cr} = \frac{(2)^2 \times (10.3 \times 10^6) \times (0.5) (3.14)^2}{(10 \times 12)^2}$$

$$P_{cr} = 14104.70 \text{ lb}$$

Now safe,

$$P_{safe} = \frac{P_{cr}}{FOS} = \frac{14104.70 \text{ lb}}{2}$$

$$P_{safe} = 7052.35 \text{ lb}$$

Case: II

Structs or column acts as a fixed end column about an axis parallel to 2 in size.

So,

$$I_y = \frac{bh^3}{12} + \frac{hb^3}{12}$$

$$I_y = \frac{2 \times 0.75^3}{12}$$

$$I_y = 0.0703 \text{ in}^4$$

$$L_e = L/2 \text{ (For fixed ended column)}$$

Then;

$$P_{cr} = \frac{n^2 EI \pi^2}{L_e^2}$$

$$= \frac{(2)^2 \times (10.3 \times 10^6) \times (0.0703) \times (3.14)^2}{\left(\frac{10}{2} \times 12\right)^2}$$

$$= 7932.48 \text{ lb}$$

$$P_{\text{safe}} = \frac{P_{\text{cr}}}{\text{FOS}}$$

$$= \frac{7932.48}{2}$$

$$= 3966.24 \text{ lb}$$

"In both cases"

we will take smaller value
of P_{safe} .

$$P_{\text{safe}} = 3966.24 < 7052.35$$

So, we will consider $P_{\text{safe}} = 3966.24 \text{ lb}$