

Assignment

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Section: B

Batch: 2016

Dept: BE (CE)

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Date: 7/9/2020

Q.1

①

Review of integration Concept

Ans It contain some major
concept integration including

- 1) Substitution method
- 2) Integration by parts
- 3) Integration Rational
function

Substitution method:

$$\rightarrow \int f(g(x)) g'(x) dx = \int f(u) du$$

If the function $f(u)$ has an
easily ~~identif~~ identification

anti derivatives ⁽²⁾ then all is well -
If not another substitution method
may be needed

③ Integration by Parts:

$$\rightarrow [u(x)v(x)]' = u'(x)v(x) + u(x)v'(x)$$

$$= u(x)v'(x) = [u(x)v(x)]' - u'(x)v(x)$$

$$= \int u(x)v'(x) dx = u(x)v(x) - \int v(x)u'(x) dx$$

$$= \int u dv = uv - \int v du$$

In case of definite integral we have

$$\int_a^b u(x)v'(x) dx = [u(x)v(x)]_{x=a}^{x=b}$$

$$\int_a^b v(x)u'(x) dx$$

Integrating Rational function ⁽⁴⁾

$$= \frac{3x+2}{2x^2+x-3} = \frac{3x+2}{(2x+3)(x-1)}$$

To integrate such a function, we use the method of partial fraction to split the function into easily integrable pieces -

$$\frac{3x+2}{(2x+3)(x-1)} = \frac{1}{2x+3} + \frac{1}{x-1}$$

Now

$$\int \frac{3x+2}{2x^2+x-3} dx = \frac{1}{2} \log(2x+3) + \log(x-1) + C$$

Q.2) Application of Trapezoidal Rule and Simpson's Rule in engineering

Ans" Application of Trapezoidal Rule "

- The trapezoidal rule is one of the family member of numerical integration formula
- The trapezoidal rule has faster convergence
- Moreover the trapezoidal rule tends to become extremely accurate than periodic functions

Application of Simpson's Rule

- Simpson's Rule is a numerical method for approximating the integral of a function between two limits a & b . It is based on knowing the area under a parabola, or a plane curve.

- It includes the calculation of a vessel's displacement, total wetted surface area, and the calculation of the longitudinal center of buoyancy of the hull.

- It is a $\textcircled{7}$ weighted average that results in an even more accurate approximation.