

Q NO 3

Aus

$$1^2 + 2^2 + 3^2 + \dots + n^2 = \frac{n(n+1)(2n+1)}{6}$$

$$n \geq 1$$

Sol

Put (1) is true

for $n=1$

$$\text{L.H.S } P(1) = n^2$$

$$P(1) = (1)^2$$

$$1 = 1$$

Now take R.H.S

$$P(1) = \frac{n(n+1)(2n+1)}{6}$$

Put value of $n=1$

$$\Rightarrow P(1) = 1(1+1)(2(1)+1)$$

$$\Rightarrow P(1) = \frac{1(2)(2+1)}{6}$$

$$P(1) = \frac{6}{6} = 1$$

So

$$\text{L.H.S} = \text{R.H.S}$$

of $P(1)$

Hence $P(1)$ is true.

Q No 4

The six different types of relations are

- (i) Reflexive relation
- (ii) Symmetric relation
- (iii) transitive relation
- (iv) Equivalence relation
- (v) identity relation
- (vi) inverse relation.

Let let us discuss the above different types of relations in detail

Reflexive Relation.

The rule for reflexive relation is given below

Every element is related to itself"

Let R be a reflexive relation defined on the set A and $a \in A$, then $R = \{(a, a) \mid \forall a \in A\}$

that is, every element of A has to be related to itself.

Example.

Let $A = \{1, 2, 3\}$ and R be a reflexive relation defined on set A

Then, $R = \{(1, 1), (2, 2), (3, 3)\}$

Symmetric Relation.

Let R be a symmetric relation defined on the set A and

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discrete structure.

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Q1

Sol

Formula $a_n = a_1 + (n-1)d$

Given data.

$$a_3 = 7$$

$$a_8 = 17$$

Required Data

$$a_{36} = ?$$

Now

Sol $a_3 = a_1 + (3-1)d$

$$7 = a_1 + 2d$$

$$7 = a_1 + 2d$$

$$a_1 + 2d = 7 \quad \text{Eq (1)}$$

and

$$a_8 = a_1 + (8-1)d$$

$$17 = a_1 + 7d$$

$$a_1 + 7d = 17 \quad \text{Eq (2)}$$

Subtract (i) from (2).

$$- a_1 + 7d = 17$$

$$- a_1 + 2d = 7$$

$$10d = 10$$

$$d = 1$$

Now put value of $d = 1$
in Eq (1)

$$a_1 + 6d = 7$$

$$a_1 + 6(1) = 7$$

$$\boxed{a_1 = 1}$$

Now find

$$a_{36}$$

$$a_{36} = a_1 + (36 - 1)d$$

$$a_{36} = a_1 + 35d$$

Put value of $d = 1$

$$a_{36} = 1 + 35(1)$$

$$a_{36} = 36 \rightarrow \text{Ans}$$

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Q No 2.

Find $f \circ g(x)$ and $g \circ f(x)$

$$\text{if } f(x) = 2x + 3$$

$$g(x) = x^2 + 5$$

Sol

$$f \circ g(x) = g \circ f(x)$$

take L.H.S

$$f \circ g(x) = 2(x^2 + 5) + 3$$

$$f \circ g(x) = -2x^2 + 10 + 3$$

$$f \circ g(x) = -2x^2 + 13 \Rightarrow \text{L.H.S}$$

Now the

$$g \circ f(x) = -(2x + 3)^2 + 5$$

$$g \circ f(x) = -(4x^2 + 9 + 12x) + 5$$

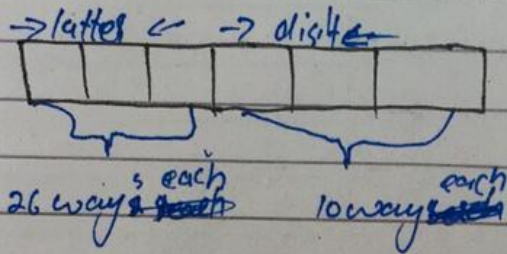
$$g \circ f(x) = -4x^2 - 12x - 4$$

$$f \circ g(x) = -2x^2 + 13$$

$$g \circ f(x) = -4x^2 - 12x - 4$$

Q NO (5)

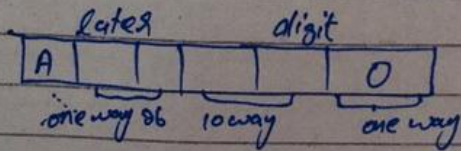
Sol



a)

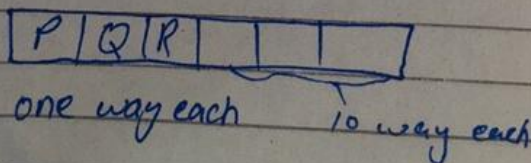
Hence by the products Rule other is a total of
 $26 \times 26 \times 26 \times 10 \times 10 \times 10 = 17,576,000$ different license plate possible

(b) How many license plate could begin with 'A' and end with '0'.



c) $1 \times 26 \times 26 \times 10 \times 10 \times 1 = 67600$
different license could be possible

c) How many license plate begin with PQR.



$$1 \times 1 \times 1 \times 10 \times 10 \times 10 = 1000$$

license plate are possible